

Exam final - 2003 - 4

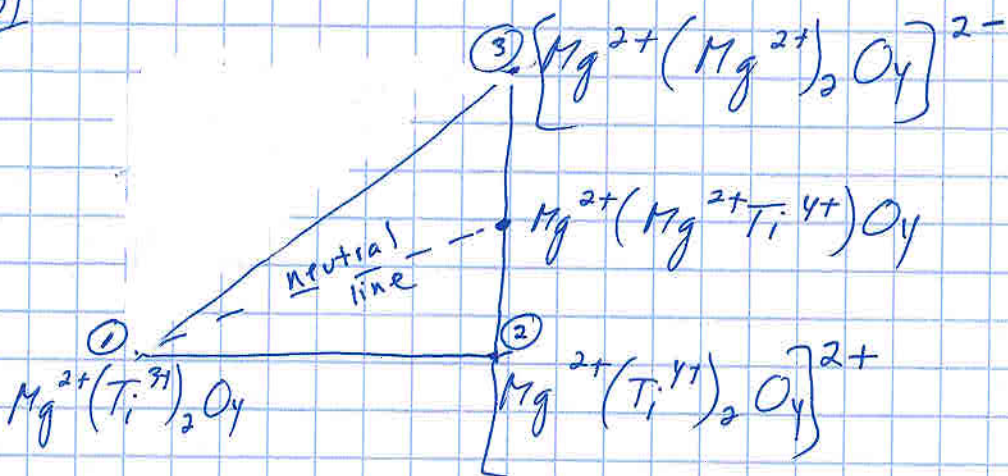


$$a_{MgTi_2O_4} = (1) \left(\frac{2x}{2}\right)^2 = x^2 = \left(x_{Ti^{3+}_B}\right)^2$$

$$a_{Mg_2TiO_4} = \frac{(1) \left(\frac{1-x}{2}\right) \left(\frac{1-x}{2}\right)}{\left(\frac{1}{2}\right) \left(\frac{1}{2}\right)} = (1-x)^2 = \left(x_{Mg^{2+}_B} x_{Ti^{4+}_B}\right)$$

→ Value for pure Mg_2TiO_4

(b)

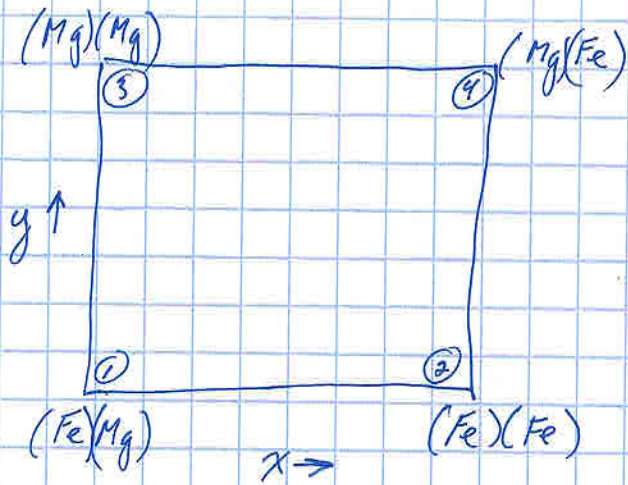


$$G = (n_1 g_1^0 + n_2 g_2^0 + n_3 g_3^0) + RT (n_1 + n_2 + n_3) \left(\frac{2x}{2} \ln \frac{2x}{2} + \frac{(1-x)}{2} \ln \left(\frac{1-x}{2} \right) \right)$$

where: $\frac{n_2 + n_3}{2} = n_{Mg_2TiO_4}$

$$g_{Mg_2TiO_4}^0 = \frac{1}{2} (g_2^0 + g_3^0) + RT \left(\frac{1}{2} \ln \frac{1}{2} + \frac{1}{2} \ln \frac{1}{2} \right)$$

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$$g = ((1-x)(1-y)g_1^0 + x(1-y)g_2^0 + y(1-x)g_3^0 + xyg_4^0) + RT(x \ln x + (1-x) \ln(1-x) + y \ln y + (1-y) \ln(1-y))$$

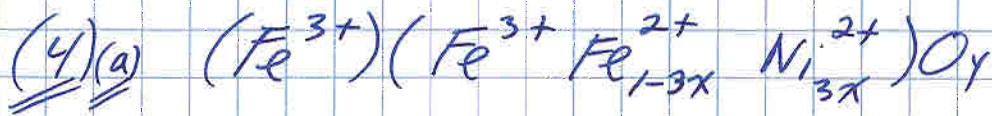
$$\begin{cases} g_3^0 = g_{\text{Mg}_2\text{SiO}_4}^0 \\ g_2^0 = g_{\text{Fe}_2\text{SiO}_4}^0 \end{cases}$$

$$(g_4^0 + g_1^0) - (g_2^0 + g_3^0) = \Delta G^{\text{Exchange}} = \text{model parameter}$$

The model parameter is related to the relative preference of Fe^{2+} and Mg^{2+} for the M1 and M2 sites.

If no data on site distribution, set $\Delta G^{\text{Exch}} = 0$.

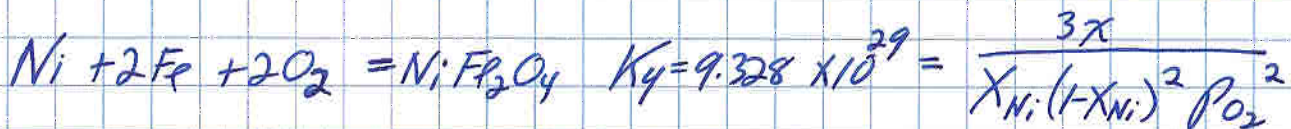
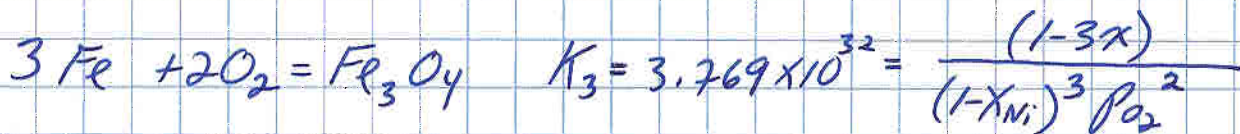
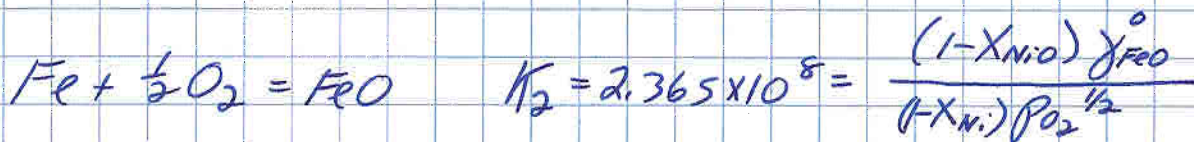
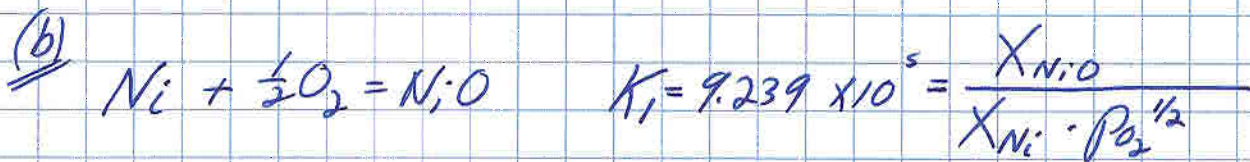
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where: $x = X_{\text{Ni:Fe}_2\text{O}_4}$ in the $\text{Fe}_3\text{O}_4 - \text{Ni}_3\text{O}_4$ system

$$a_{\text{Fe}_3\text{O}_4} = \frac{X_{\text{Fe}^{2+}(\text{B})} X_{\text{Fe}^{3+}(\text{B})}}{(X_{\text{Fe}^{2+}(\text{B})}) (X_{\text{Fe}^{3+}(\text{B})})_{\text{when } x=0}} = \frac{(\frac{1-3x}{2})(\frac{1}{2})}{(\frac{1}{2})(\frac{1}{2})} = (1-3x)$$

$$a_{\text{Ni:Fe}_2\text{O}_4} = \frac{X_{\text{Fe}^{3+}(\text{B})} X_{\text{Ni}^{2+}(\text{B})}}{(X_{\text{Fe}^{3+}(\text{B})} X_{\text{Ni}^{2+}(\text{B})})_{x=\frac{1}{3}}} = \frac{(\frac{3x}{2})(\frac{1}{2})}{(\frac{1}{2})(\frac{1}{2})} = 3x$$



4 equations. 4 unknowns

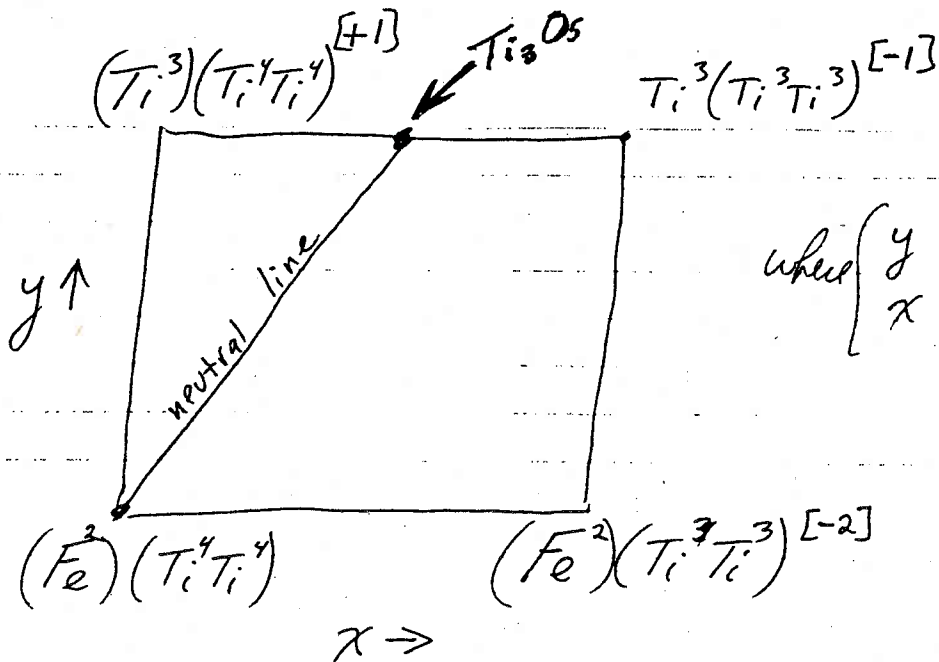
$$X_{\text{NiO}} = 0.815$$

$$p_{\text{O}_2} = 7.78 \times 10^{-13}$$

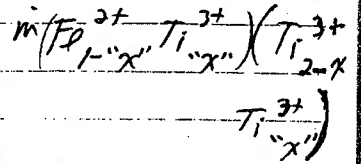
$$x = 0.21$$

$$X_{\text{Ni}} = 1.00$$

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(5)



where $\begin{cases} y = ("x") \\ x = (\frac{"x"}{2}) \end{cases}$



$$x = \frac{M_{\text{Ti}^{3+}_B}}{M_{\text{Ti}^{3+}_B} + M_{\text{Ti}^{4+}_B}}$$

$$y = \frac{M_{\text{Ti}^{3+}_A}}{M_{\text{Fe}^{2+}_A} + M_{\text{Ti}^{3+}_A}}$$

$$g = \left\{ (1-x)(1-y) g_{(\text{Fe}^{2+}\text{Ti}^{4+})_2}^{\circ} + x(1-y) g_{(\text{Fe}^{2+}\text{Ti}^{3+})_2}^{\circ} + y(1-x) g_{\text{Ti}^{4+}(\text{Ti}^{4+})_2}^{\circ} + xy g_{\text{Ti}^{3+}(\text{Ti}^{3+})_2}^{\circ} \right\}$$

$$+ 2RT(x \ln x + (1-x) \ln(1-x)) + RT(y \ln y + (1-y) \ln y)$$

$$\left[\begin{aligned} g_{\text{Fe}^{2+}(\text{Ti}^{4+})_2}^{\circ} &= g_{\text{FeTi}_2\text{O}_5(\text{real})}^{\circ} \\ -g_{\text{Ti}_3\text{O}_5(\text{real})}^{\circ} &= \left(\frac{1}{2} g_{\text{Ti}^{4+}(\text{Ti}^{4+})_2}^{\circ} + \frac{1}{2} g_{\text{Ti}^{3+}(\text{Ti}^{3+})_2}^{\circ} \right) + 2RT \left(\frac{1}{2} \ln \frac{1}{2} + \frac{1}{2} \ln \frac{1}{2} \right) \\ &= (\dots) - 2RT \ln 2 \end{aligned} \right.$$

This leaves 2 g° 's to fix. Can choose one arbitrarily.

Then: Model parameter = $\Delta G^{\circ}_{\text{EXCHANGE}}$