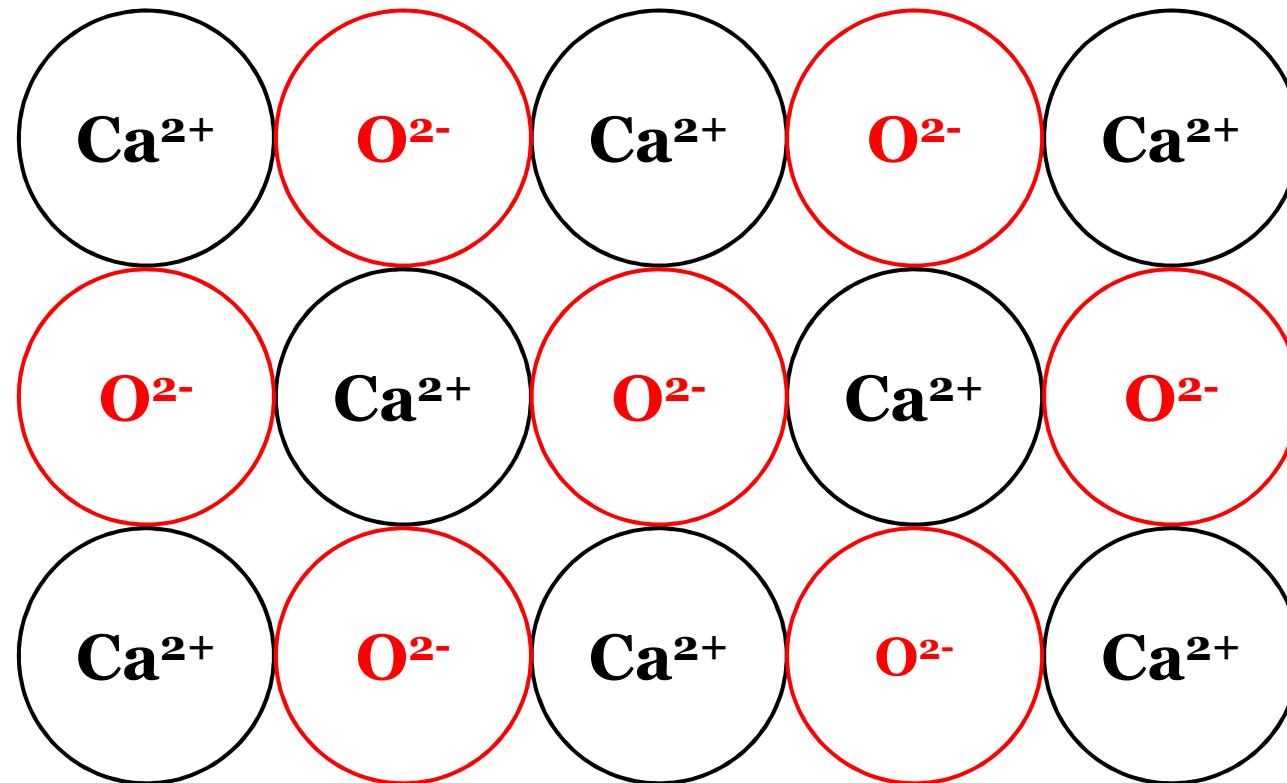


# Structure and Thermodynamics of Liquid Oxides

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May 18, 2010

# Ionic (“Basic”) Oxides



$\text{CaO}$ ,  $\text{MgO}$ ,  $\text{FeO}$ ,  $\text{MnO}$ , ...

$\text{Na}_2\text{O}$ ,  $\text{K}_2\text{O}$ , ...

# Acidic Oxides (network formers)

- Tetrahedral:



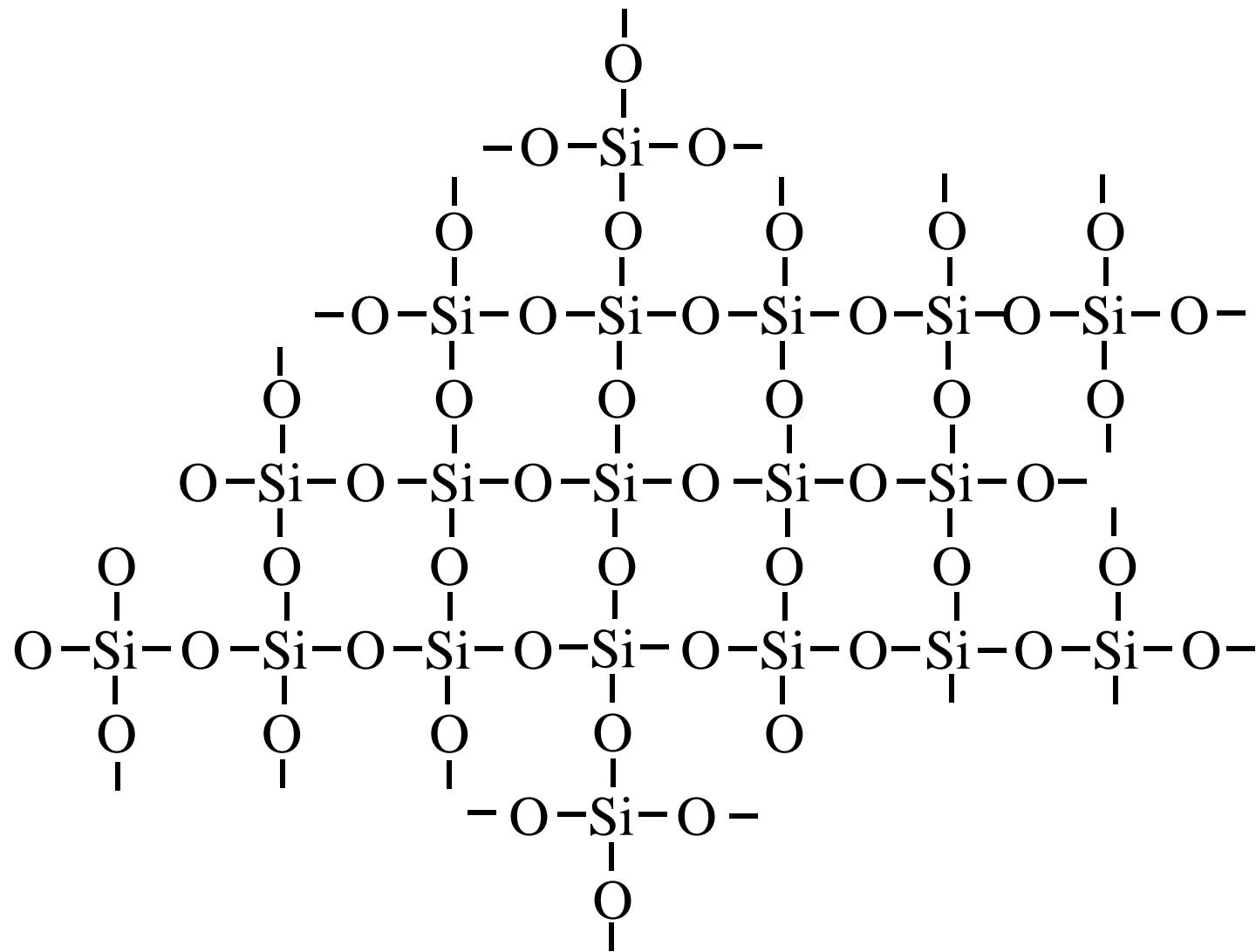
- Trigonal:



- Complex:



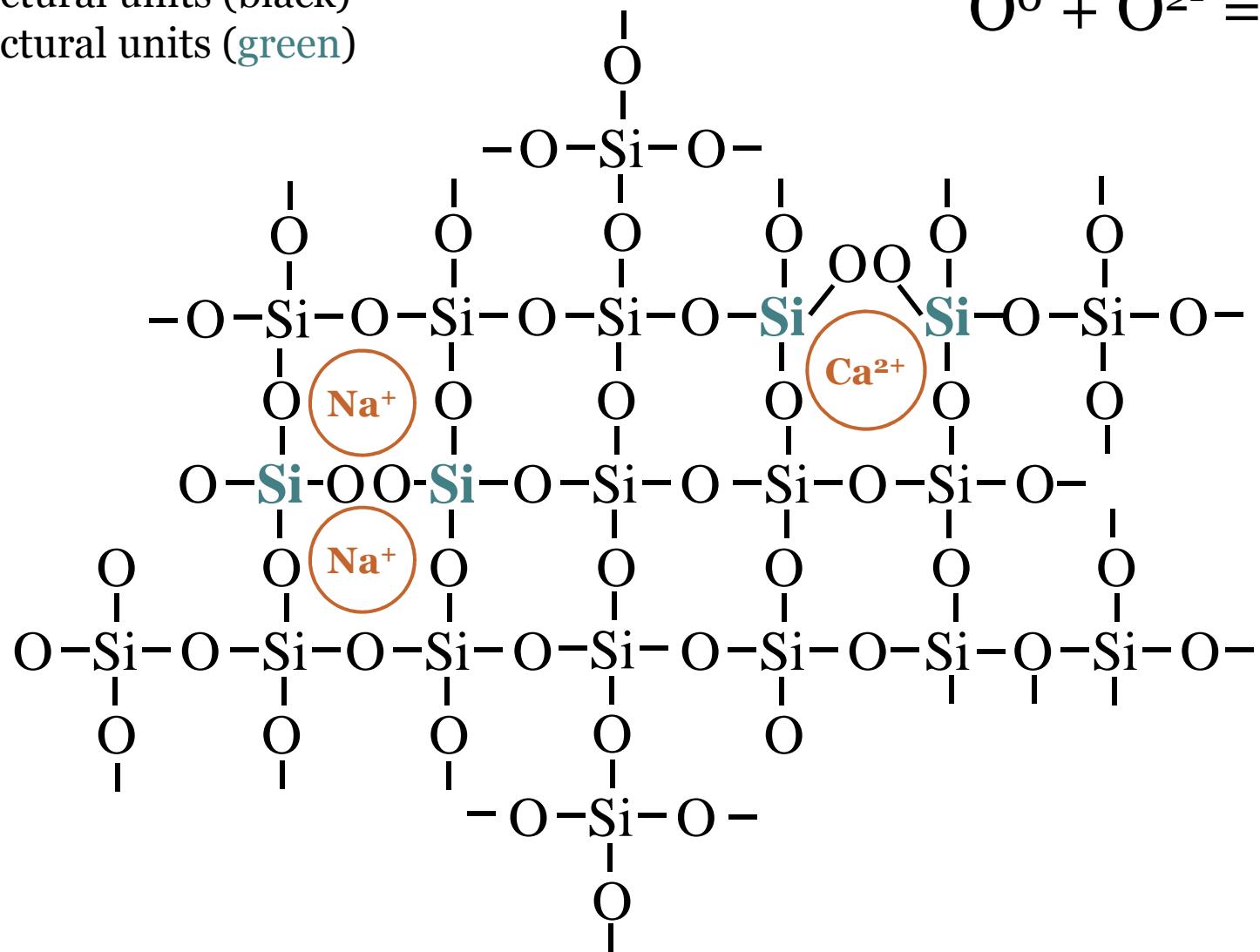
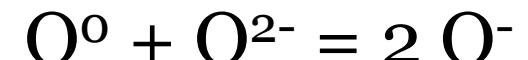
# Structure of $\text{SiO}_2$



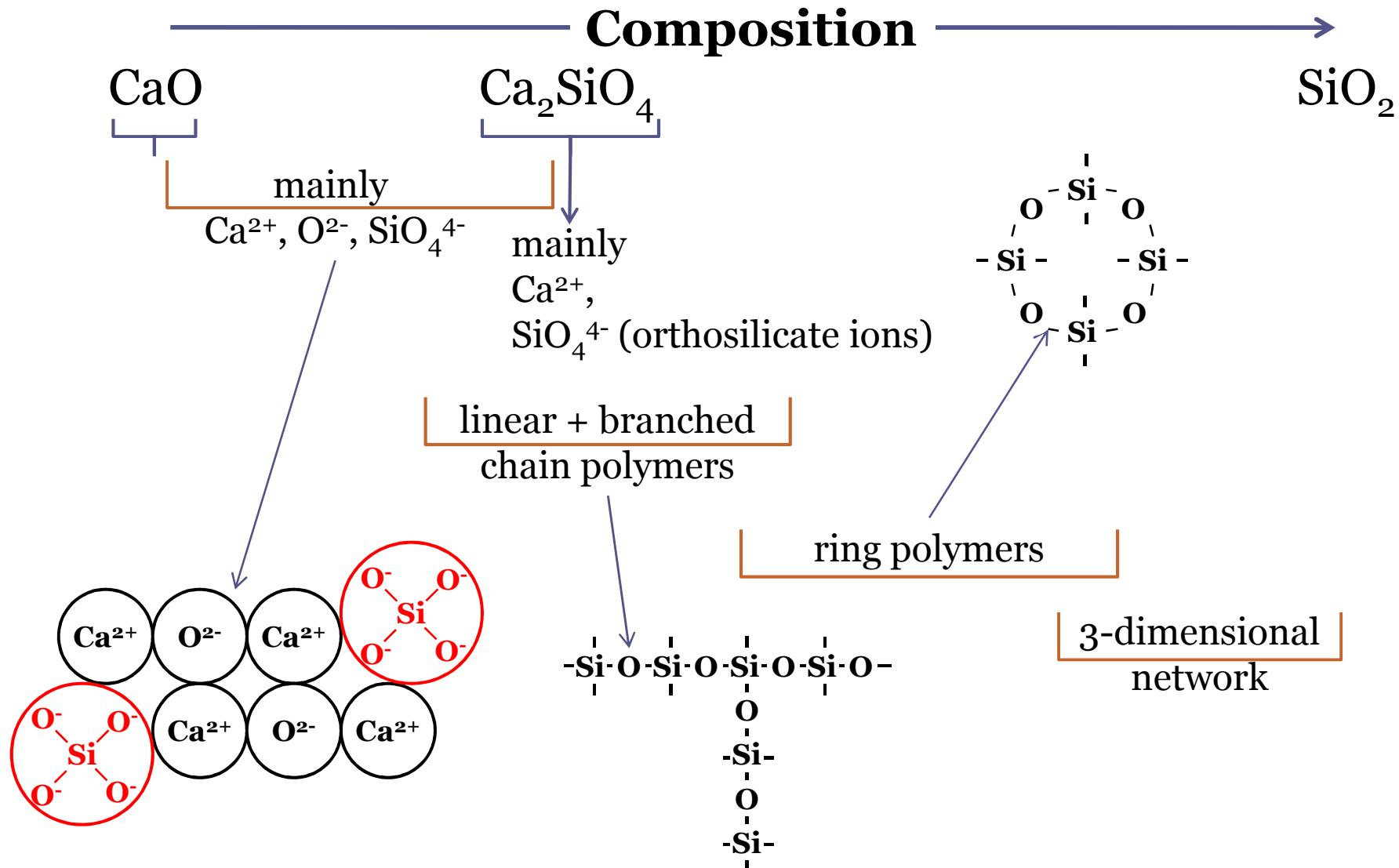
# Network Modification by Basic Oxides

Q<sup>4</sup> structural units (black)

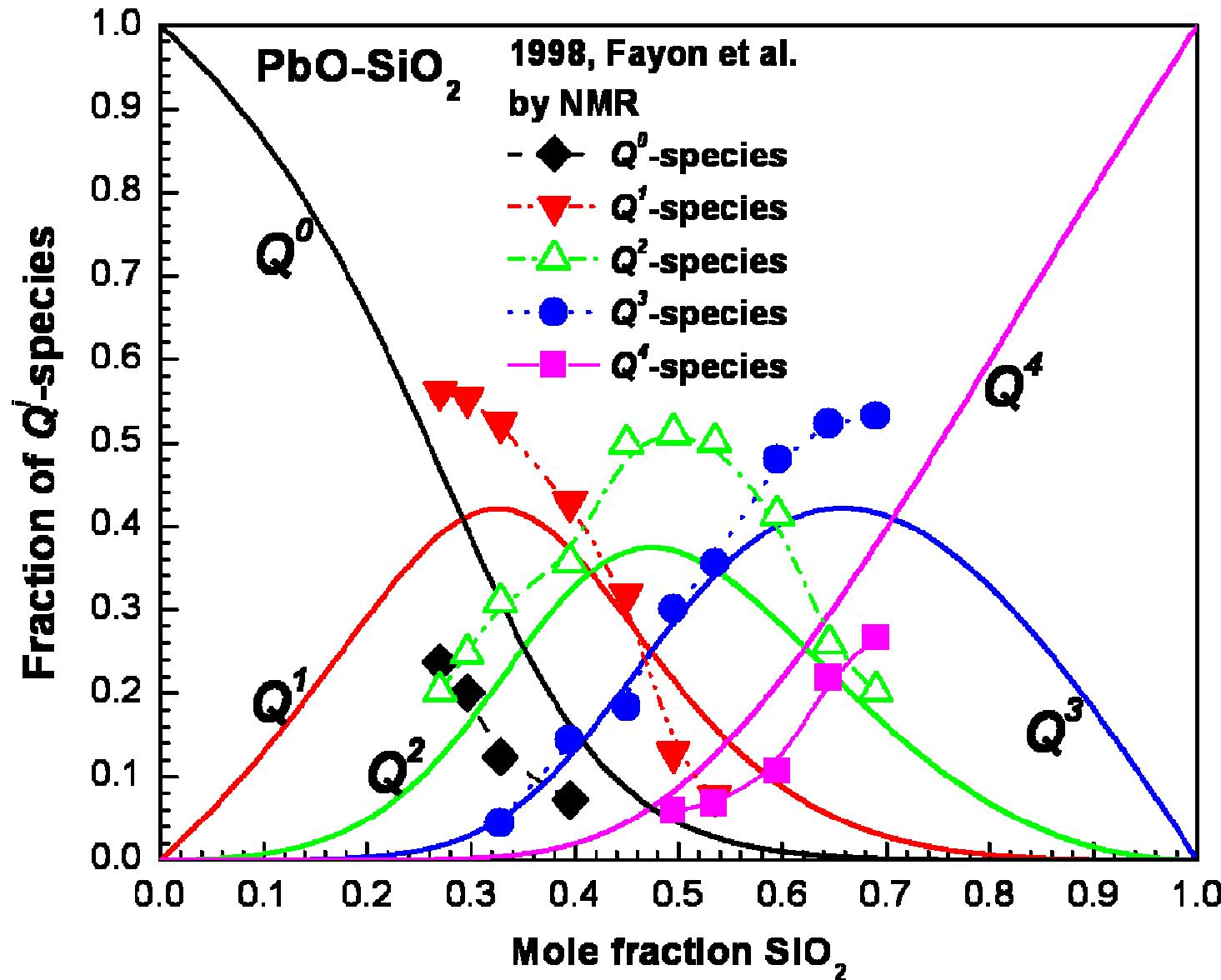
Q<sup>3</sup> structural units (green)



# Structure of CaO-SiO<sub>2</sub> Liquid Solutions

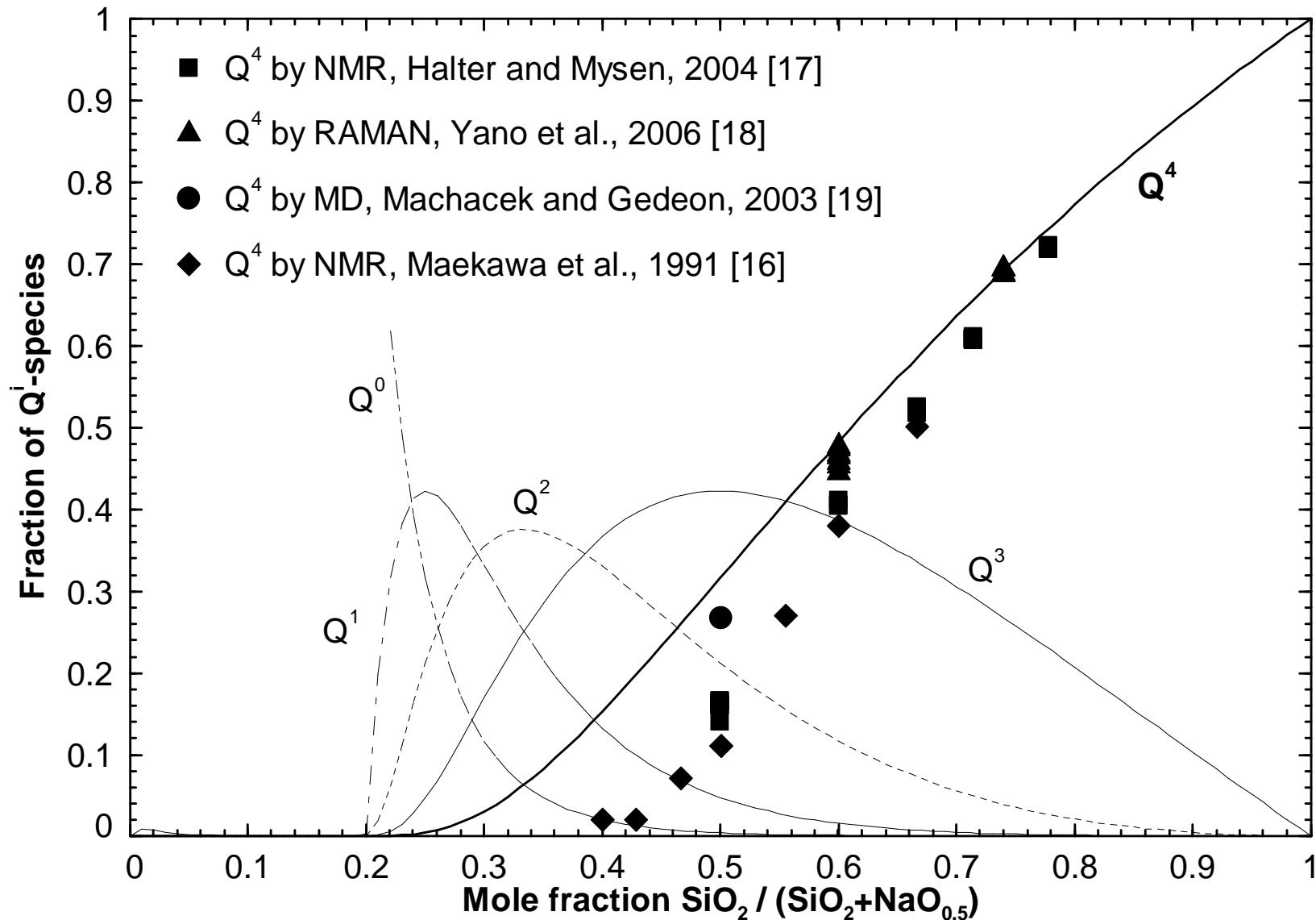


# Fractions of Q Species as Measured by NMR

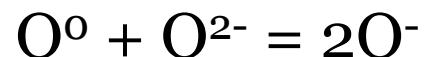
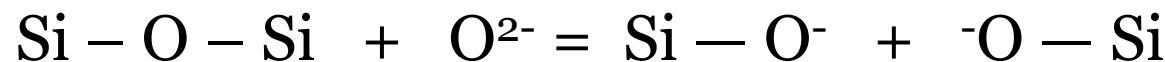


# The System $\text{NaO}_{0.5}\text{-SiO}_2$

## Measured Fractions of $\text{Q}^4$ Species

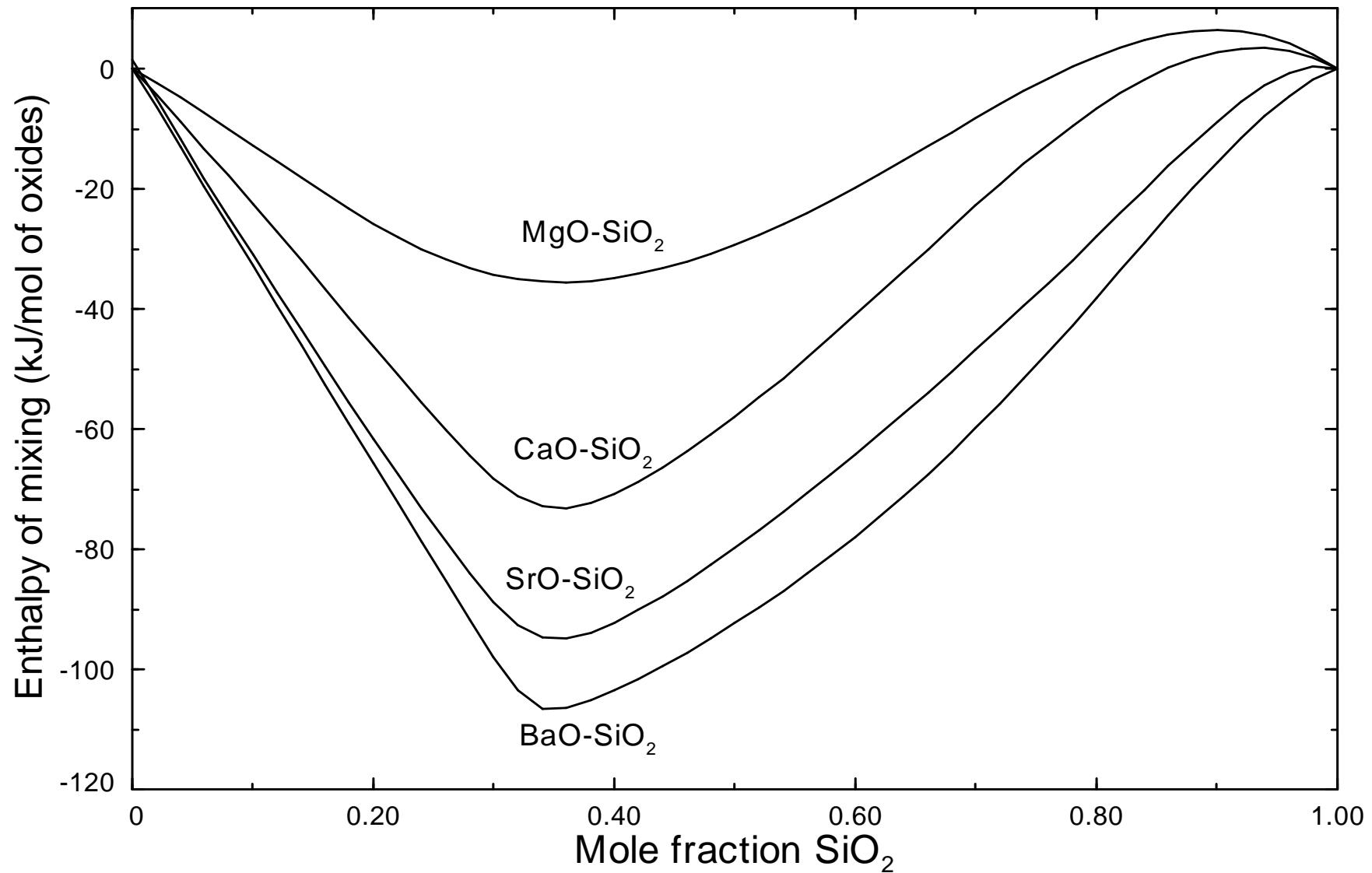


## Thermodynamic Properties as Functions of Composition

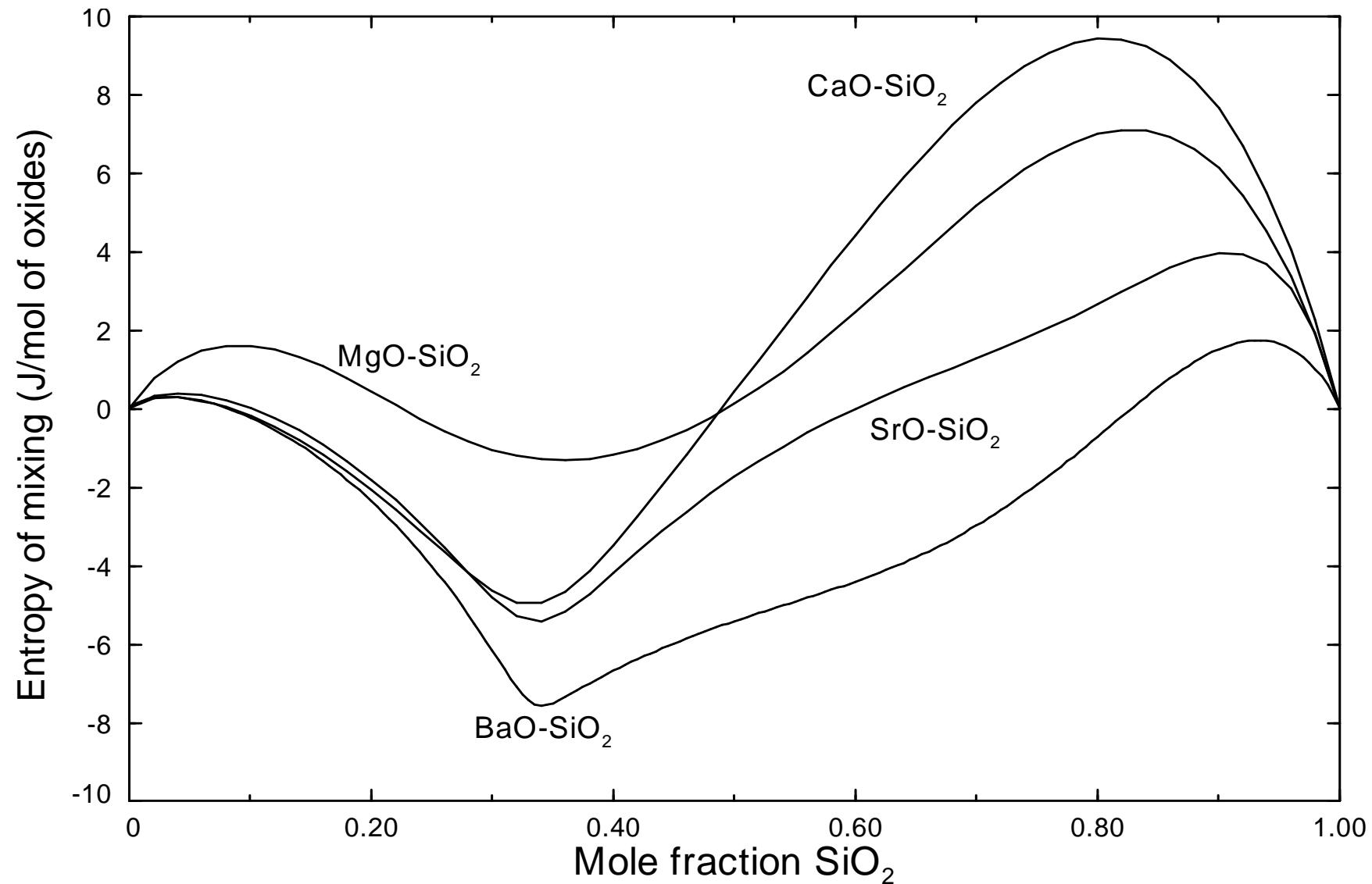


$\Delta H \ll 0$   
 $\Delta G \ll 0$

# Enthalpy of Mixing in Liquid Alkaline-earth Silicates

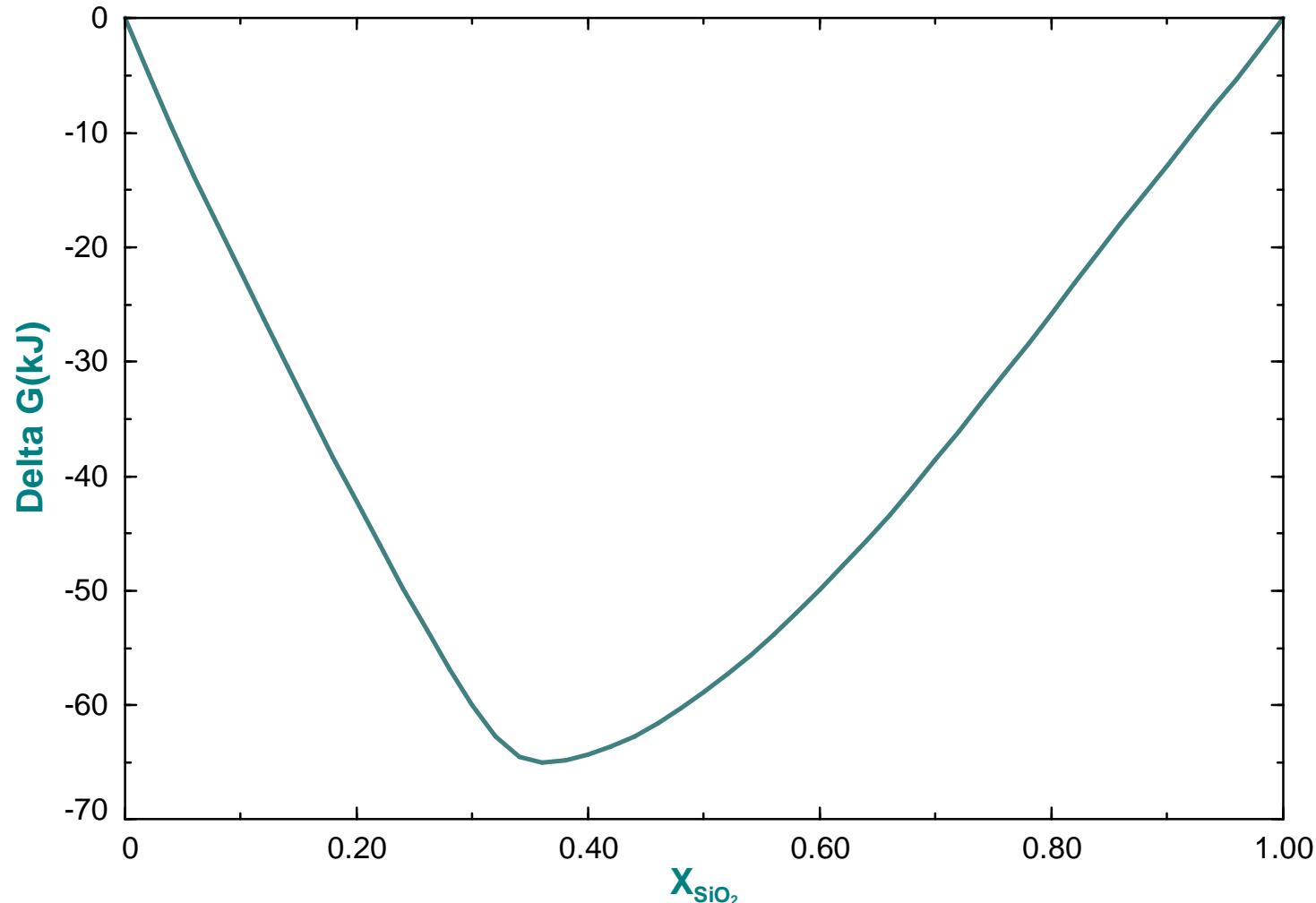


# Entropy of Mixing in Liquid Alkaline-earth Silicates



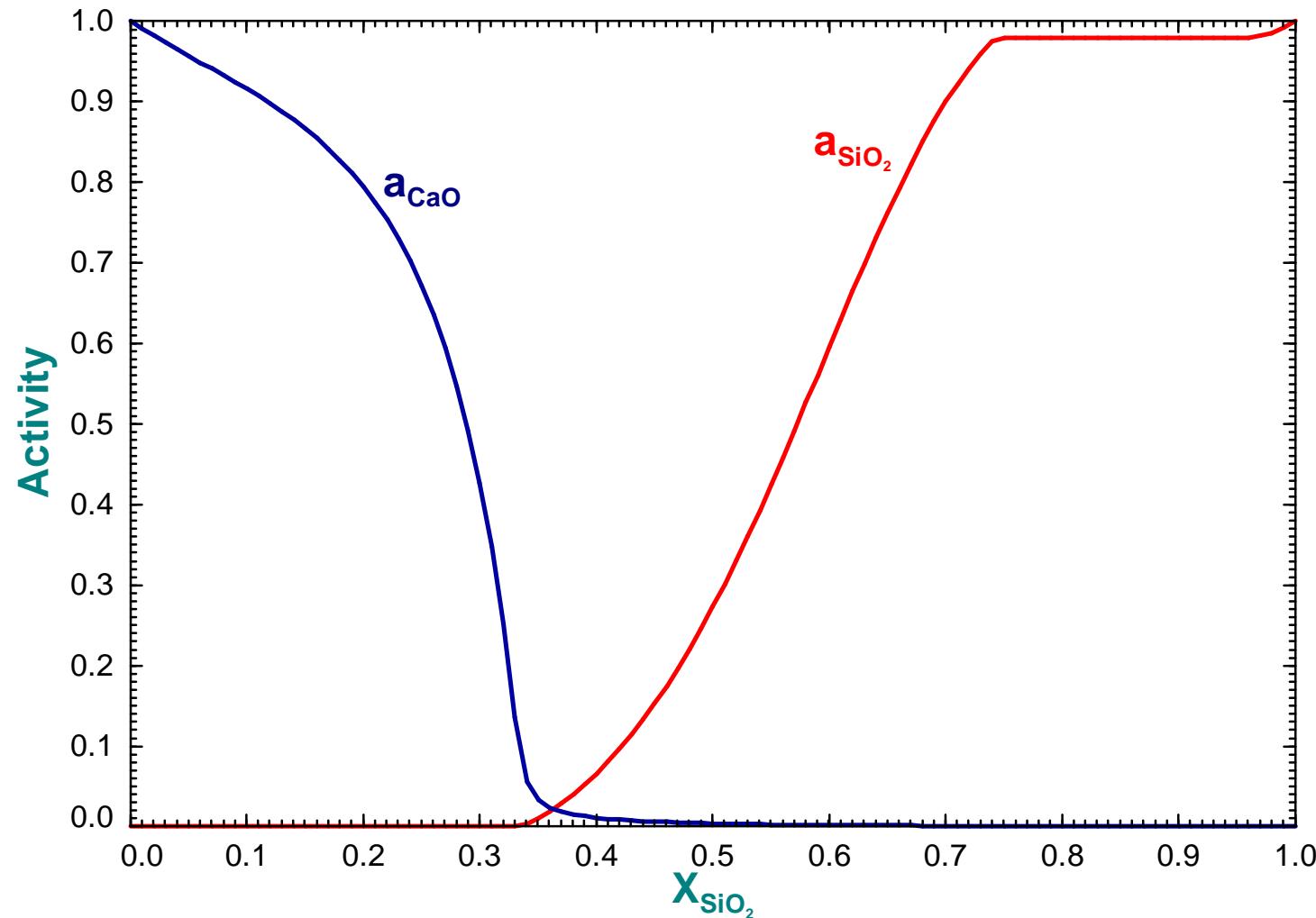
# CaO-SiO<sub>2</sub> System:

## $\Delta G$ vs $X_{\text{SiO}_2}$ at 1750°C

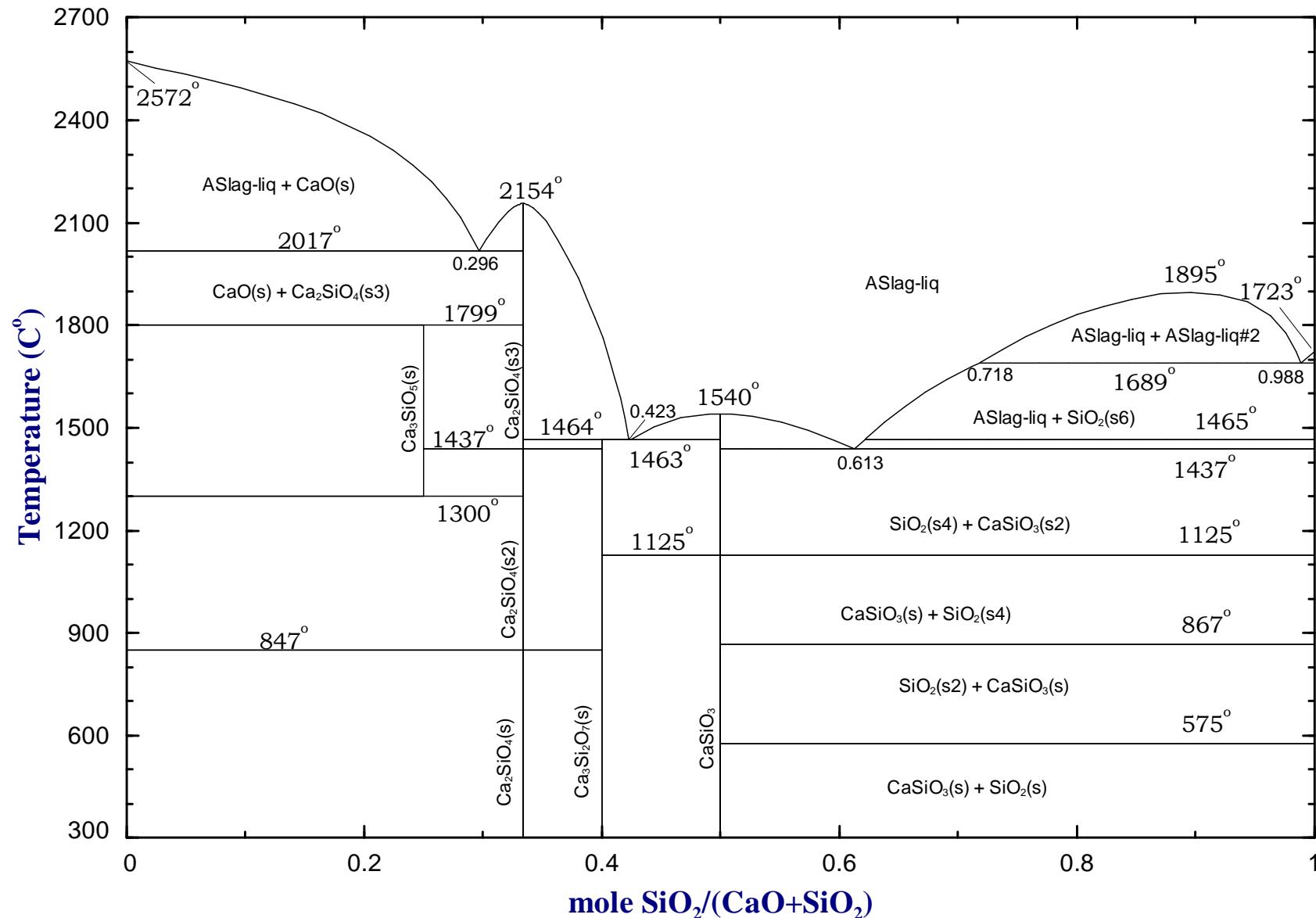


# CaO-SiO<sub>2</sub> System:

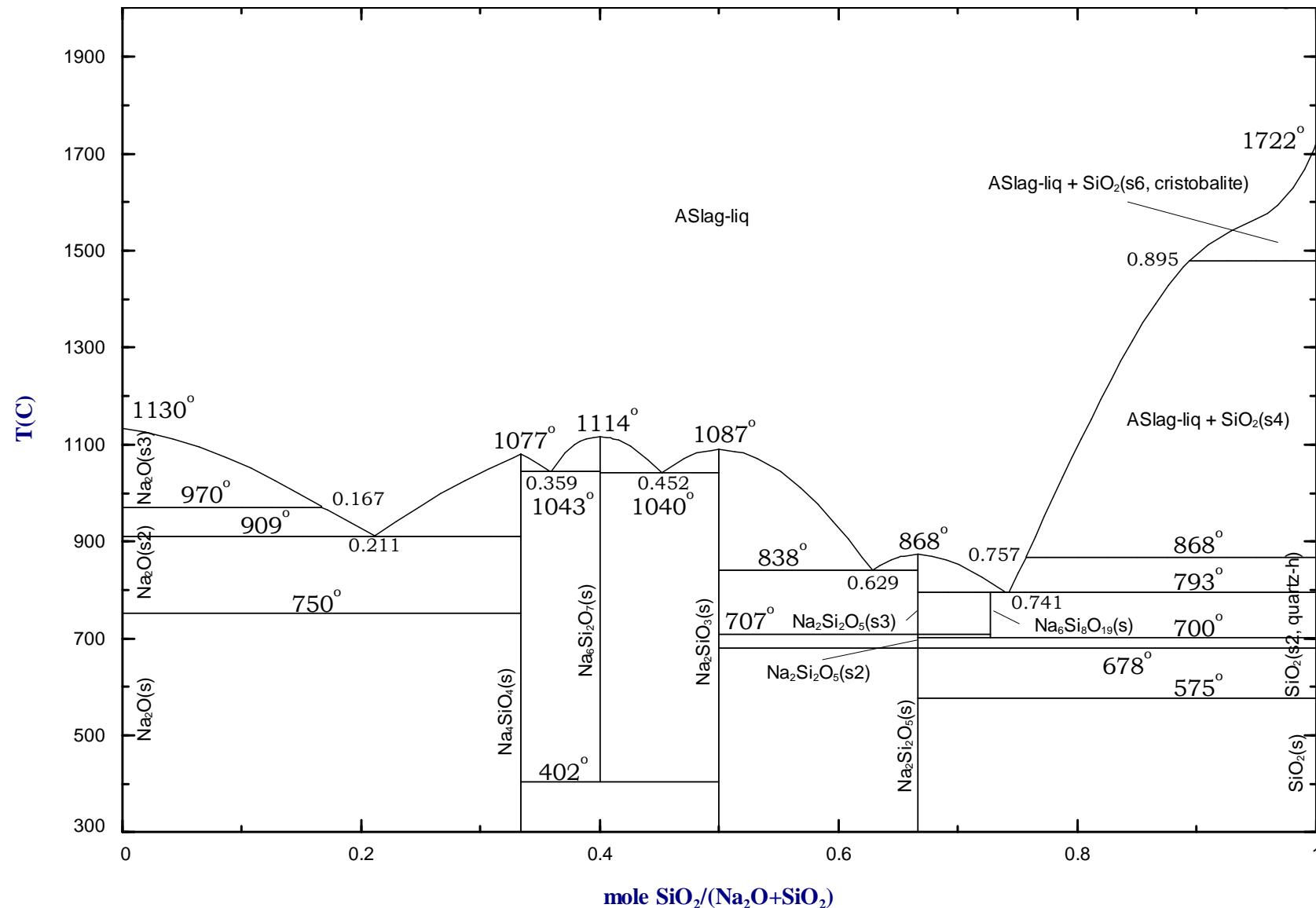
$a_{\text{SiO}_2}$  and  $a_{\text{CaO}}$  vs  $X_{\text{SiO}_2}$  at 1750 °C



# CaO - SiO<sub>2</sub> Phase Diagram

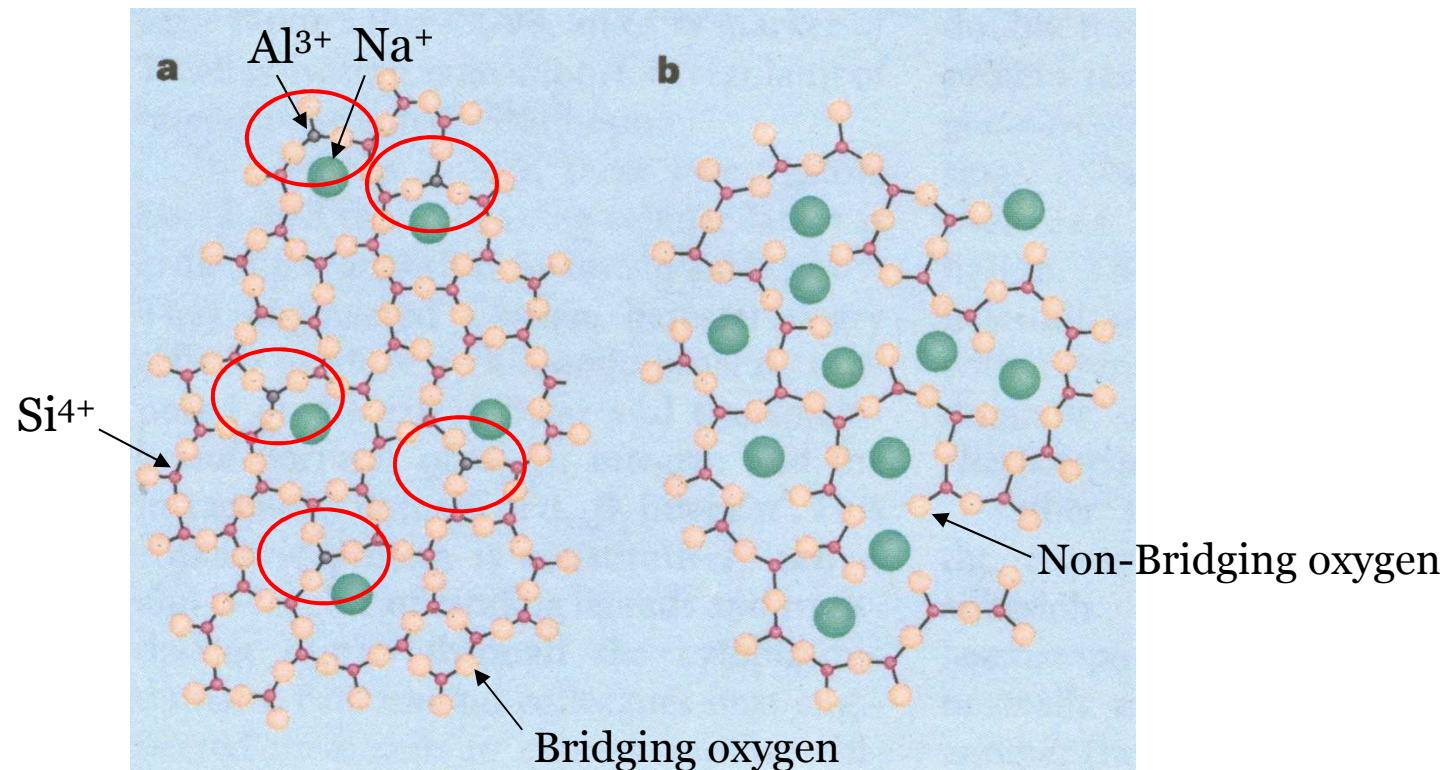


# $\text{Na}_2\text{O} - \text{SiO}_2$ Phase Diagram



# Systems with $\text{Al}_2\text{O}_3$ (amphoretic)

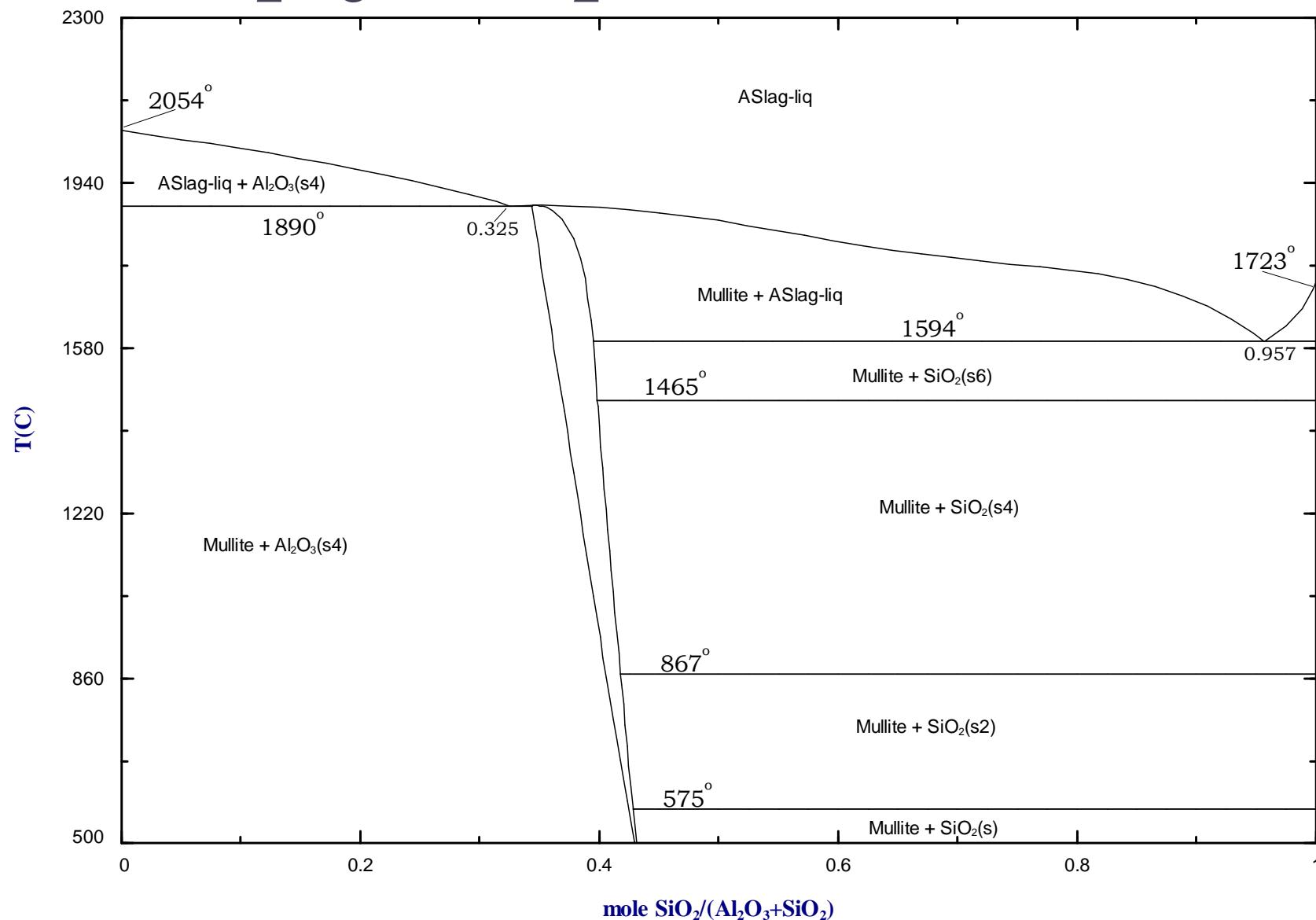
## The Charge Compensation effect



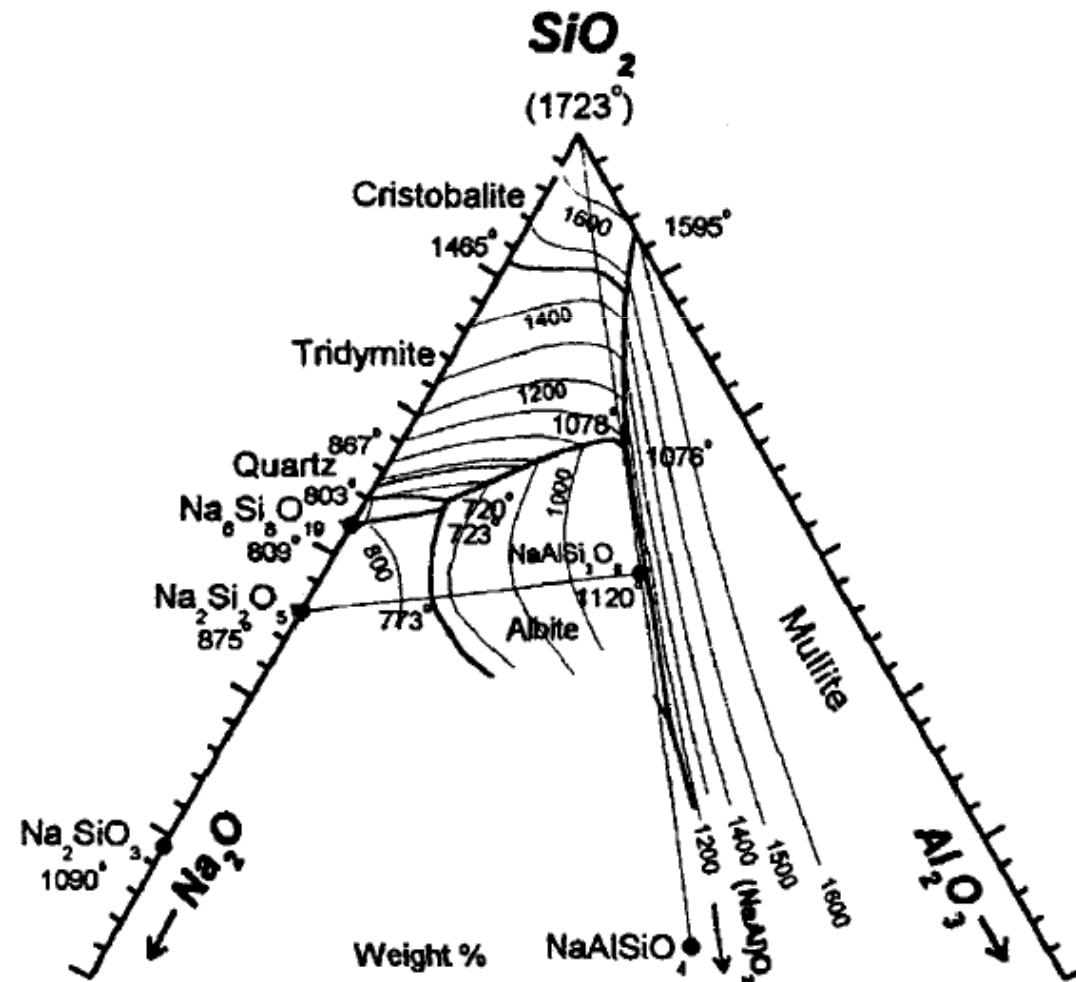
$\text{Al}^{3+}$  can replace  $\text{Si}^{4+}$   
 $\text{Na}^+$  or  $\text{K}^+$  compensates the charge

$2 \text{Al}^{3+}$  replace  $2 \text{Si}^{4+}$   
 $\text{Ca}^{2+}$  or  $\text{Mg}^{2+}$  compensates the charge

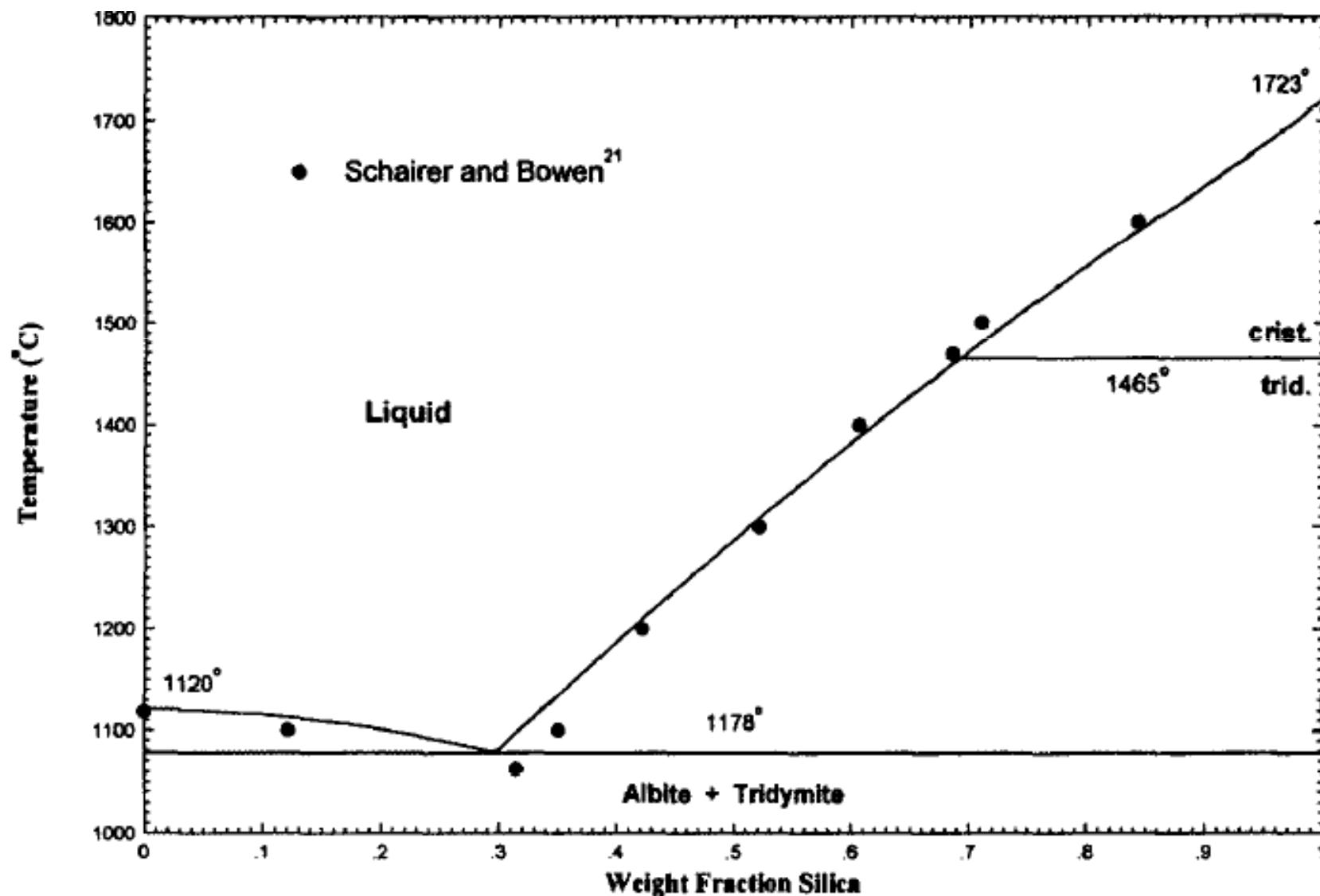
# $\text{Al}_2\text{O}_3 - \text{SiO}_2$ Phase Diagram



# $\text{Na}_2\text{O} - \text{SiO}_2 - \text{Al}_2\text{O}_3$ Phase Diagram (liquidus projection)



# Albite( $\text{NaAlSi}_3\text{O}_8$ ) - $\text{SiO}_2$



# CaO - SiO<sub>2</sub> - Al<sub>2</sub>O<sub>3</sub> Phase Diagram (liquidus projection)

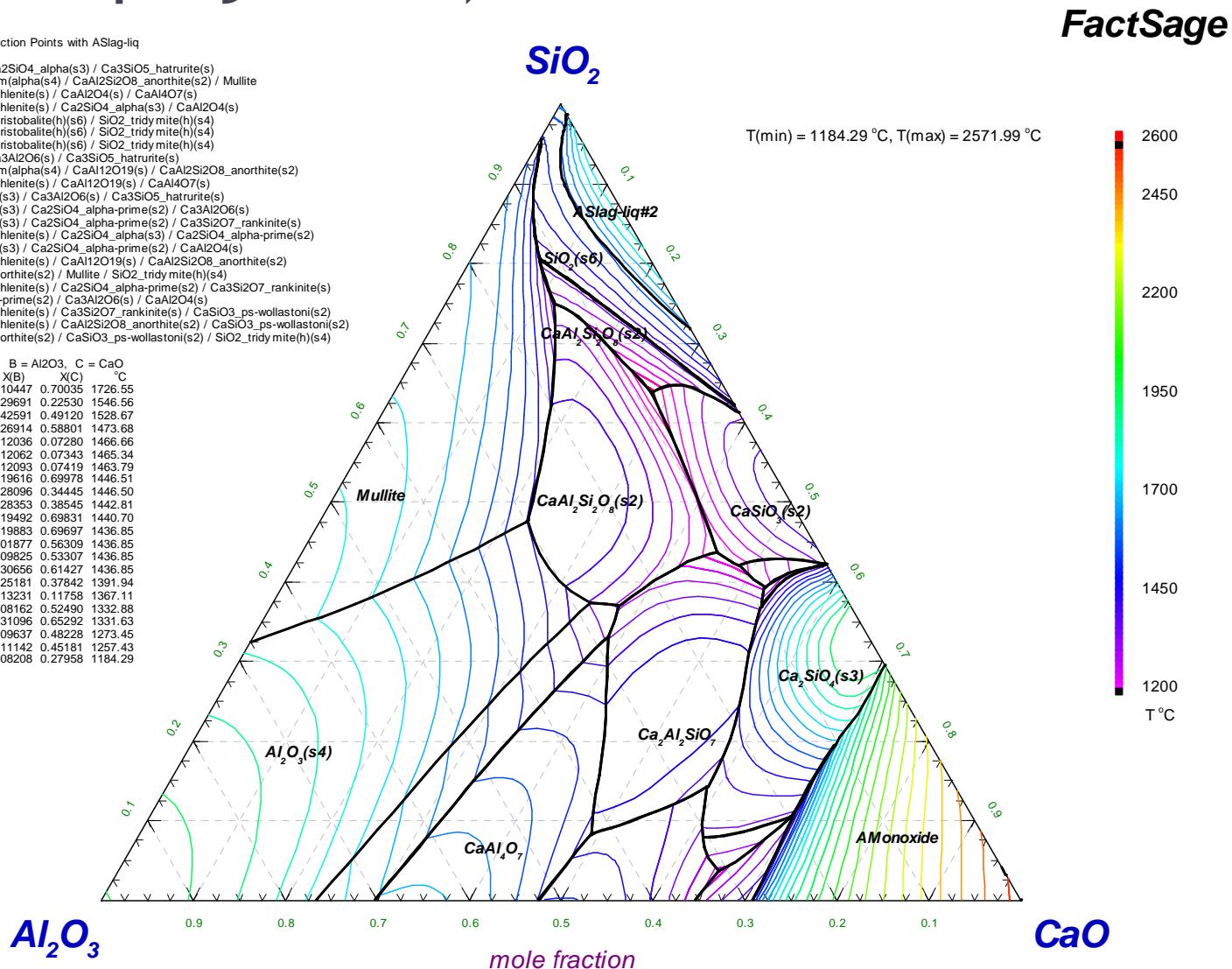
Four-Phase Intersection Points with ASlag-liq

```

1: AMonoxide / Ca2SiO4_alpha(s3) / Ca3SiO5_hatrurite(s)
2: Al2O3_corundum(alpha(s4) / CaAl2Si2O8_anorthite(s2) / Mullite
3: Ca2Al2SiO7_gehlenite(s) / CaAl2O4(s) / CaAl4O7(s)
4: Ca2Al2SiO7_gehlenite(s) / Ca2SiO4_alpha(s3) / CaAl2O4(s)
5: Mullite / SiO2_cristobalite(h)(s6) / SiO2_tridymite(h)(s4)
6: Mullite / SiO2_cristobalite(h)(s6) / SiO2_tridymite(h)(s4)
7: Mullite / SiO2_cristobalite(h)(s6) / SiO2_tridymite(h)(s4)
8: AMonoxide / Ca3Al2O6(s) / Ca3SiO5_hatrurite(s)
9: Al2O3_corundum(alpha(s4) / CaAl12O19(s) / CaAl2Si2O8_anorthite(s)
10: Ca2Al2SiO7_gehlenite(s) / CaAl12O19(s) / CaAl4O7(s)
11: Ca2SiO4_alpha(s3) / Ca3Al2O6(s) / Ca3SiO5_hatrurite(s)
12: Ca2SiO4_alpha(s3) / Ca2SiO4_alpha-prime(s2) / Ca3Al2O6(s)
13: Ca2SiO4_alpha(s3) / Ca2SiO4_alpha-prime(s2) / Ca3Si2O7_rankinite(s)
14: Ca2Al2SiO7_gehlenite(s) / Ca2SiO4_alpha(s3) / Ca2SiO4_alpha-prime(s2)
15: Ca2SiO4_alpha(s3) / Ca2SiO4_alpha-prime(s2) / CaAl2O4(s)
16: Ca2Al2SiO7_gehlenite(s) / Mullite / SiO2_tridymite(h)(s4)
17: Ca2Al2SiO7_gehlenite(s) / Ca2SiO4_alpha-prime(s2) / Ca3Si2O7_rankinite(s)
18: Ca2SiO4_alpha-prime(s2) / Ca3Al2O6(s) / CaAl2O4(s)
19: Ca2Al2SiO7_gehlenite(s) / Ca3Si2O7_rankinite(s) / CaSiO3_ps-wollaston(s2)
20: Ca2Al2SiO7_gehlenite(s) / CaAl2Si2O8_anorthite(s2) / CaSiO3_ps-wollaston(s2)
21: Ca2Al2SiO7_gehlenite(s) / CaAl2Si2O8_anorthite(s2) / CaSiO3_ps-wollaston(s2)
22: CaAl2Si2O8_anorthite(s2) / CaSiO3_ps-wollaston(s2) / SiO2_tridymite(h)(s4)

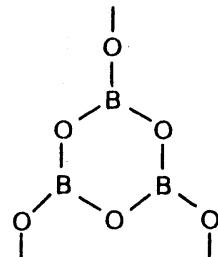
```

A = SiO<sub>2</sub>, B = Al<sub>2</sub>O<sub>3</sub>, C = CaO  
 $X(A)$     $X(B)$     $X(C)$    °C  
1: 0.19519 0.10447 0.70035 1726.55  
2: 0.47779 0.29691 0.22530 1546.56  
3: 0.08289 0.42591 0.49120 1528.67  
4: 0.14285 0.26914 0.58801 1473.68  
5: 0.80684 0.12036 0.07280 1466.66  
6: 0.80594 0.12062 0.07343 1465.34  
7: 0.80489 0.12093 0.07419 1463.79  
8: 0.10406 0.19616 0.69978 1446.51  
9: 0.37459 0.28096 0.34445 1446.50  
10: 0.33101 0.28353 0.38545 1442.81  
11: 0.10677 0.19492 0.69831 1440.70  
12: 0.10422 0.19888 0.69697 1436.85  
13: 0.41814 0.01877 0.56309 1436.85  
14: 0.36661 0.09825 0.53307 1436.85  
15: 0.07917 0.30651 0.61427 1436.85  
16: 0.36977 0.25181 0.37842 1391.94  
17: 0.75011 0.13231 0.11758 1367.11  
18: 0.39348 0.08162 0.52490 1332.88  
19: 0.03612 0.31098 0.65292 1331.63  
20: 0.42135 0.09637 0.48228 1273.45  
21: 0.43677 0.11142 0.45181 1257.43  
22: 0.63835 0.08208 0.27958 1184.29

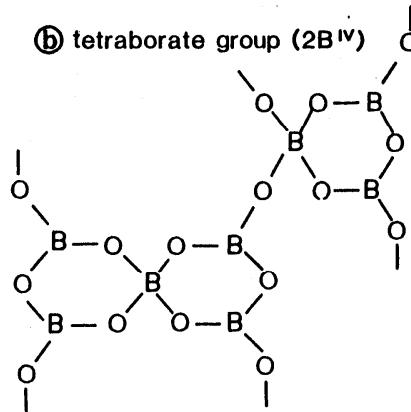


# Species in Borate Melts

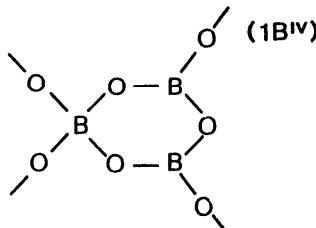
(a) boroxol group ( $B_2O_3$ )



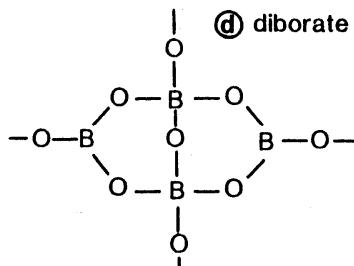
(b) tetraborate group ( $2B^{IV}$ )



(c) six-membered borate ring  
( $1B^{IV}$ )



(d) diborate group ( $2B^{IV}$ )



(e) ring type metaborate group

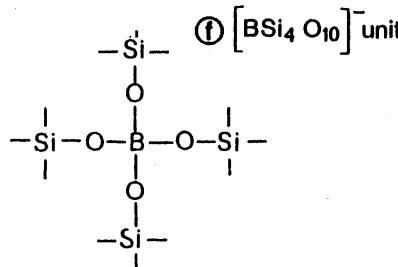
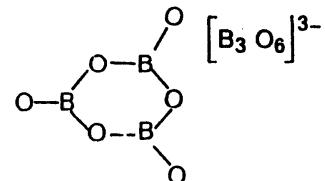
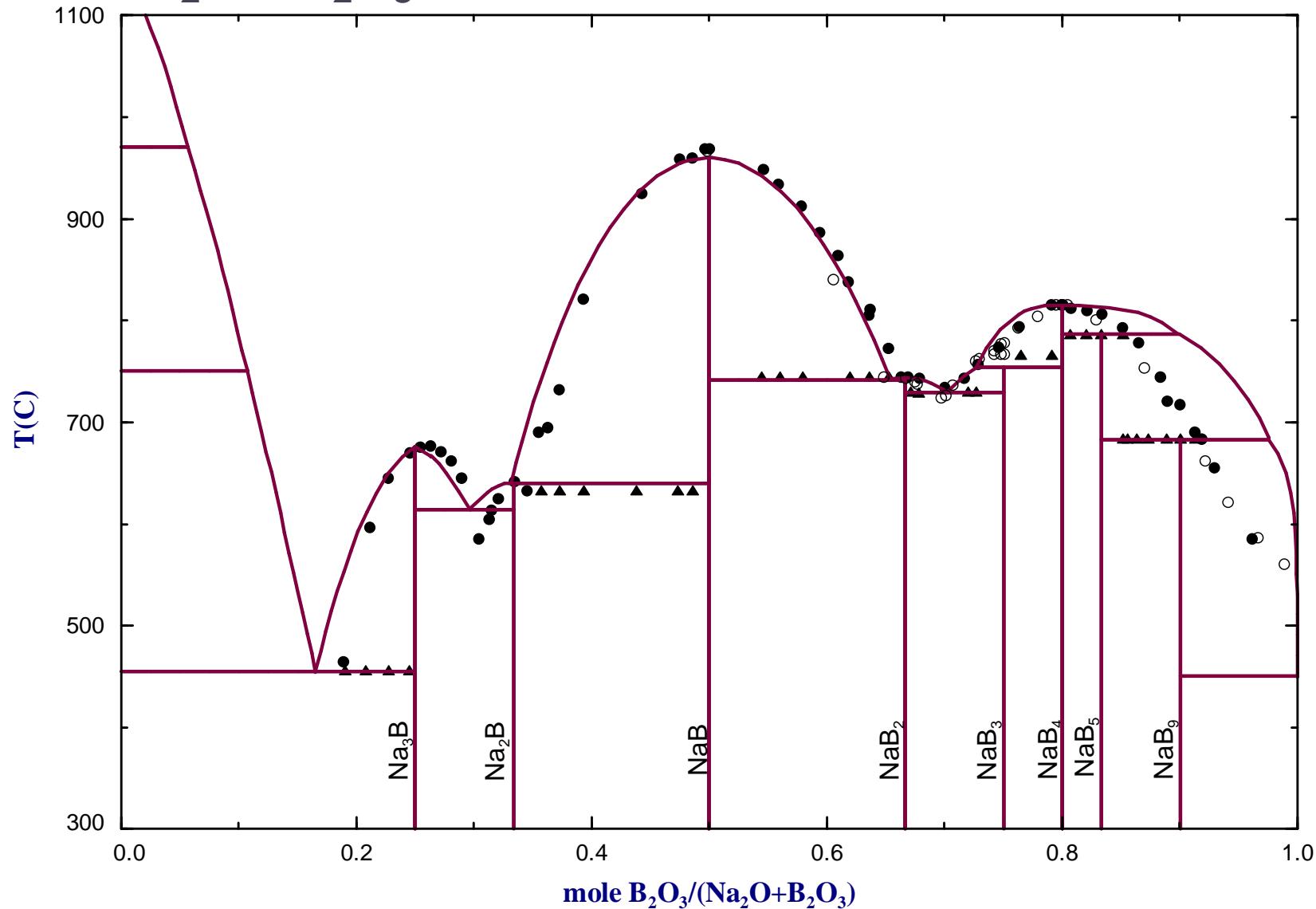
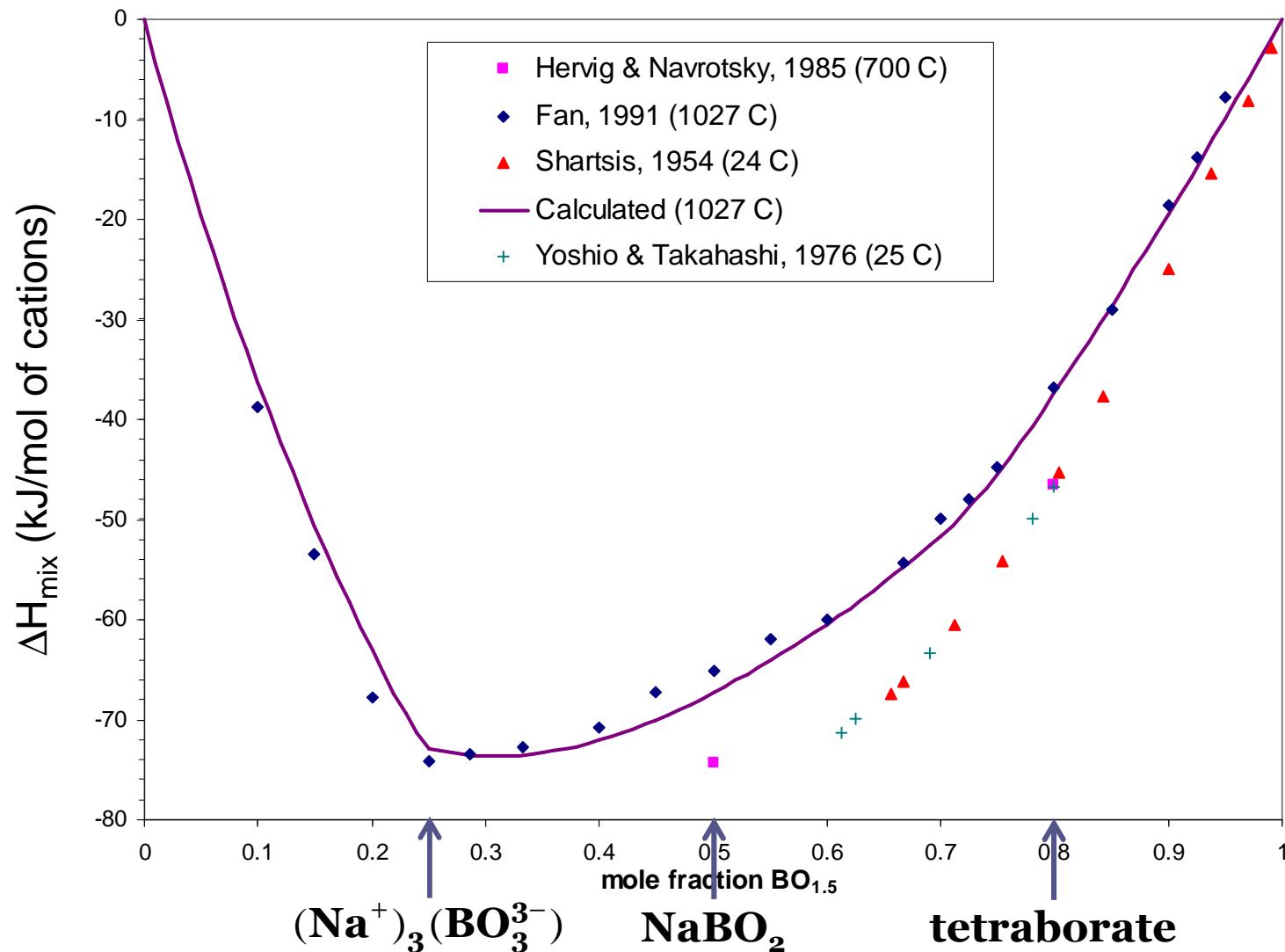


Figure 2. Species proposed by various authors for the structural role of boron in melts. (Used by permission of the editor of *Bulletin de Minéralogie*, from Pichavant, 1983a, Fig. 7, p. 208.)

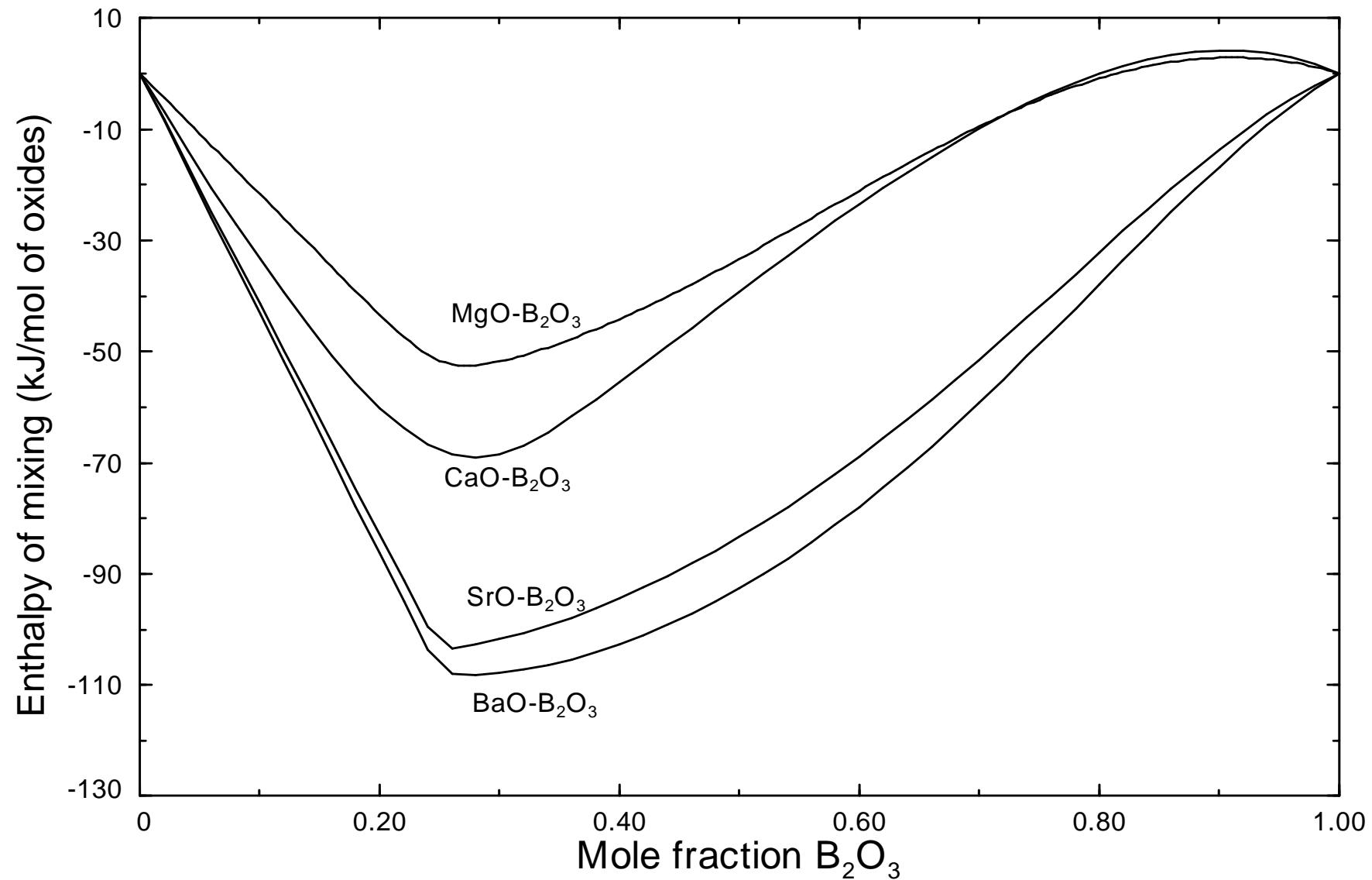
# $\text{Na}_2\text{O} - \text{B}_2\text{O}_3$ System: The $\text{Na}_2\text{O} - \text{B}_2\text{O}_3$ Phase Diagram



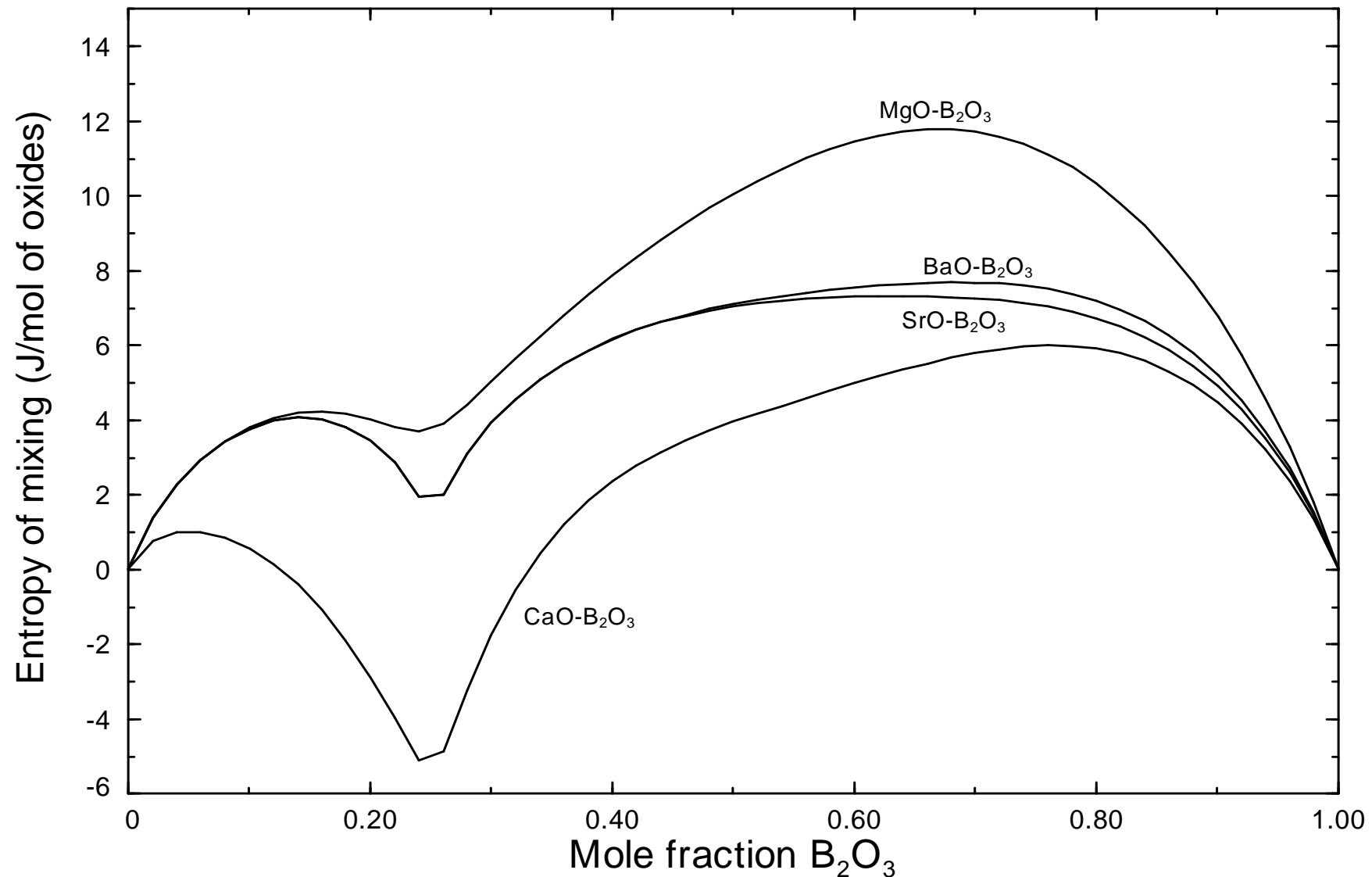
# Na<sub>2</sub>O - B<sub>2</sub>O<sub>3</sub> System: Enthalpies of Mixing in the Na<sub>0.5</sub>O - BO<sub>1.5</sub> System



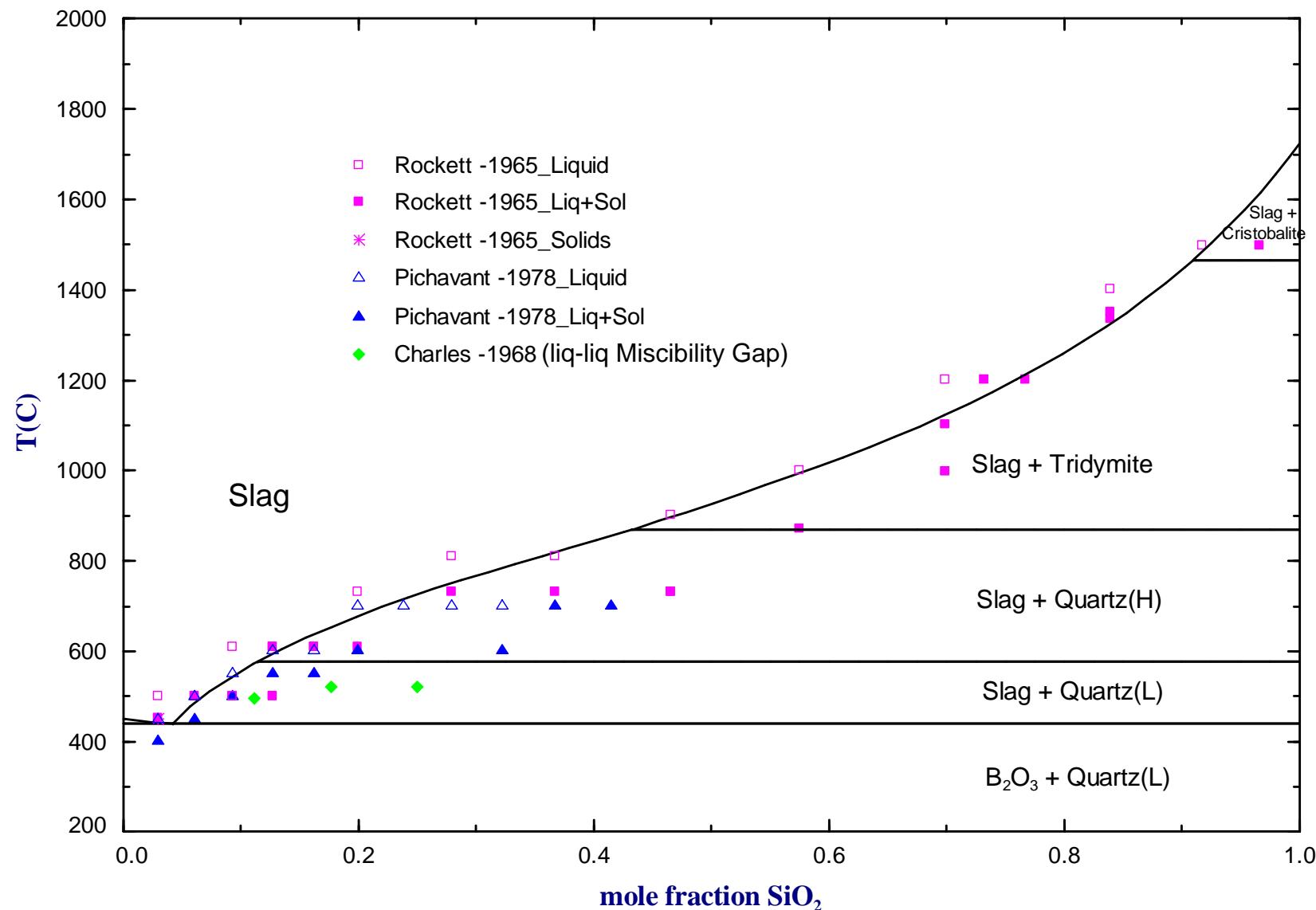
## Enthalpy of Mixing in Liquid Alkaline-earth Borates



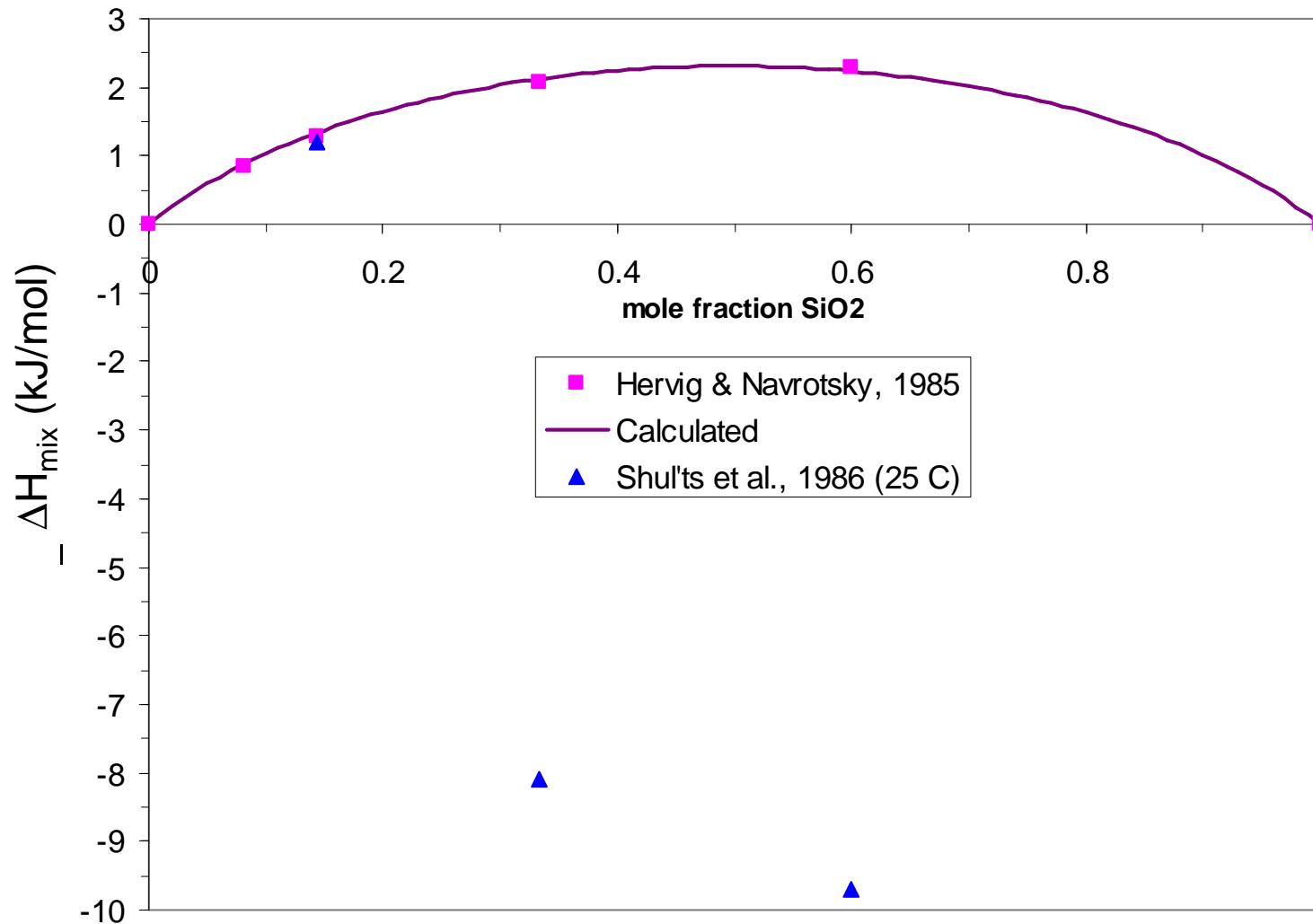
## Entropy of Mixing in Liquid Alkaline-earth Borates



# $B_2O_3 - SiO_2$ System: The $BO_{1.5} - SiO_2$ Phase Diagram

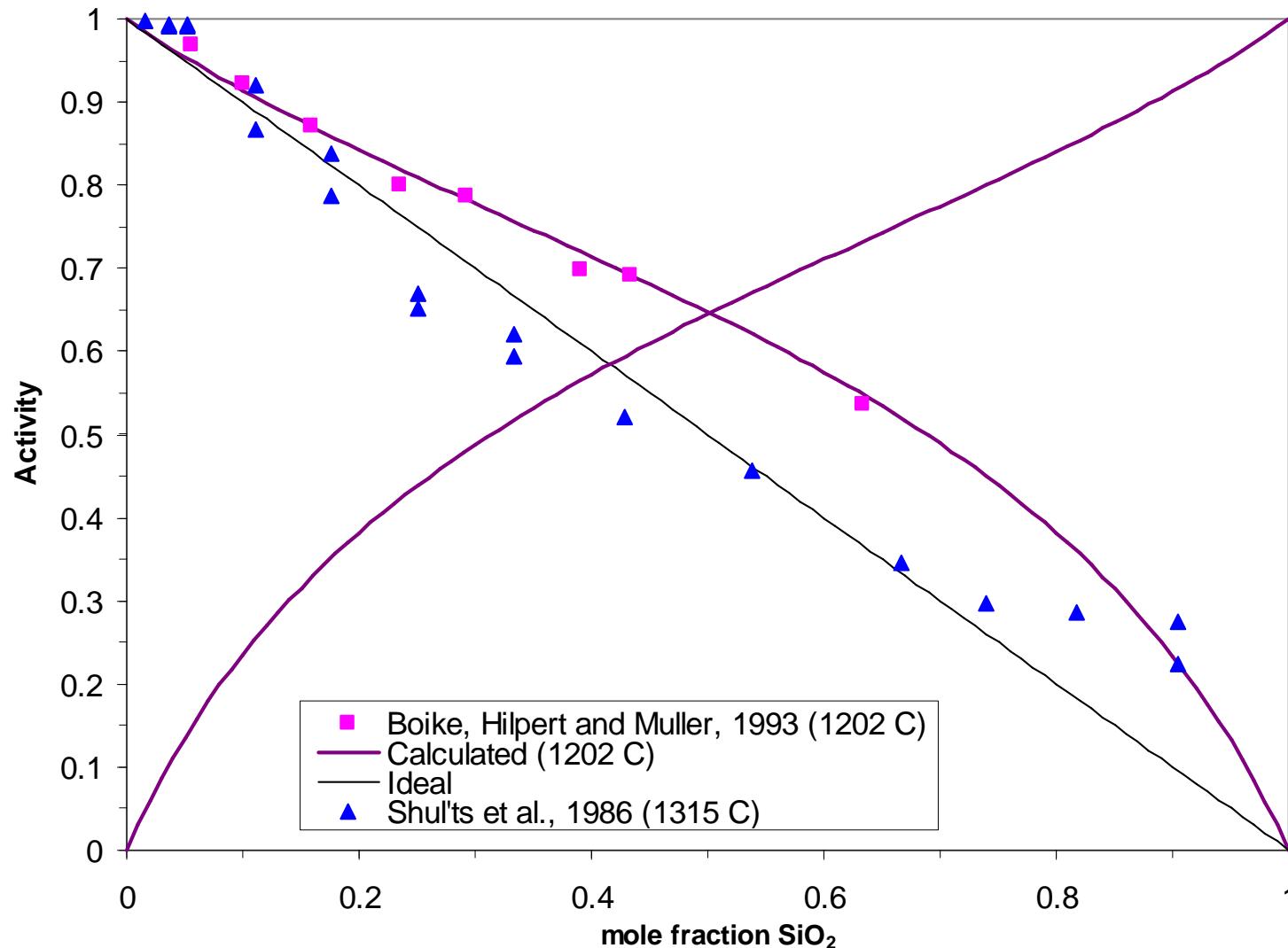


# $B_2O_3 - SiO_2$ System: Enthalpy of Mixing in the $BO_{1.5} - SiO_2$ System at 700 °C

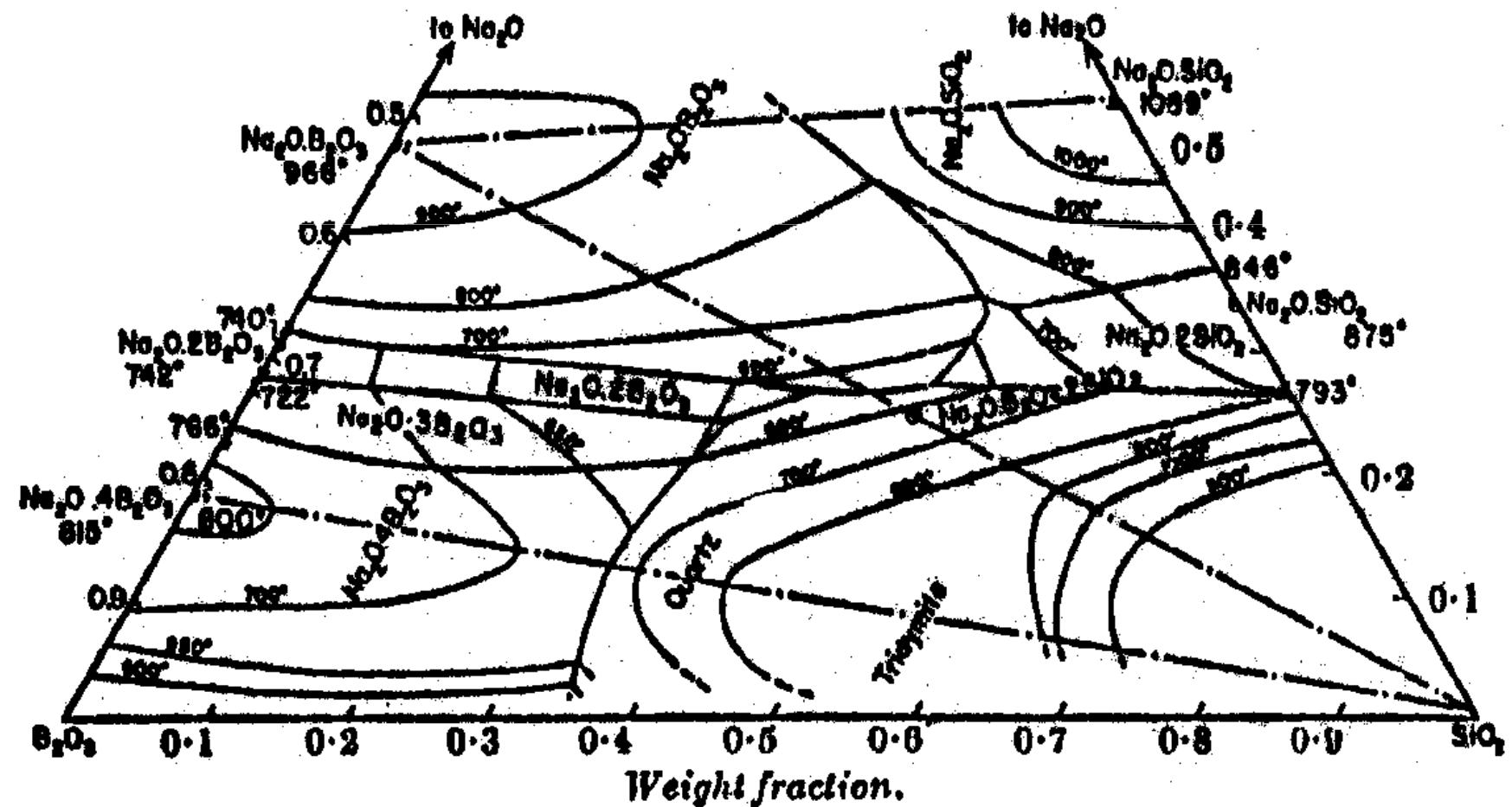


# $B_2O_3 - SiO_2$ System:

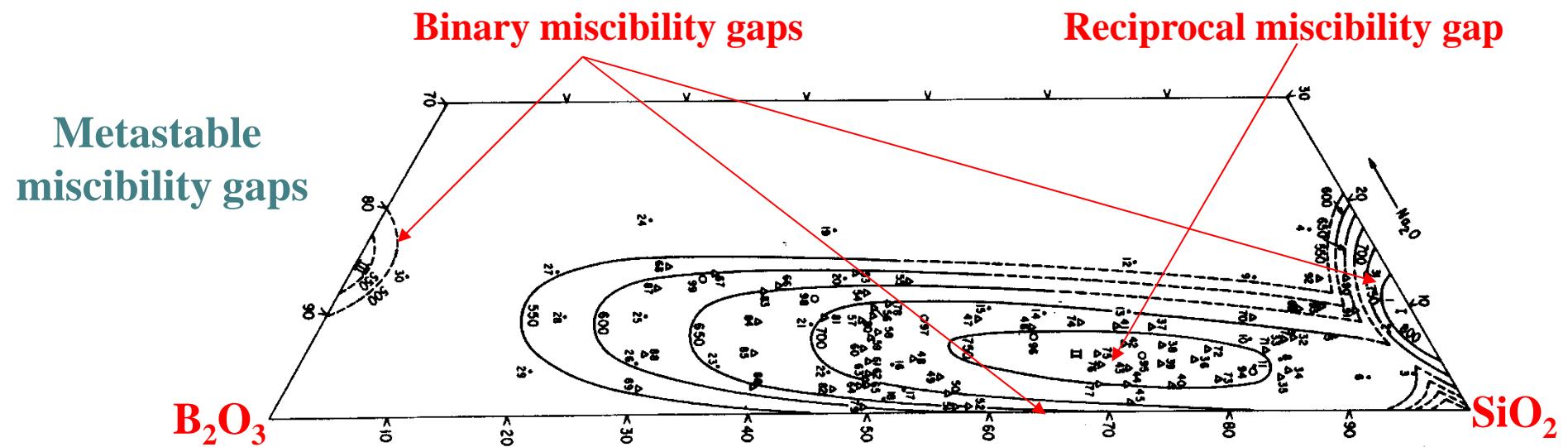
## Activity of $BO_{1.5}$ in the $BO_{1.5} - SiO_2$ Melts by Mass-spectroscopy



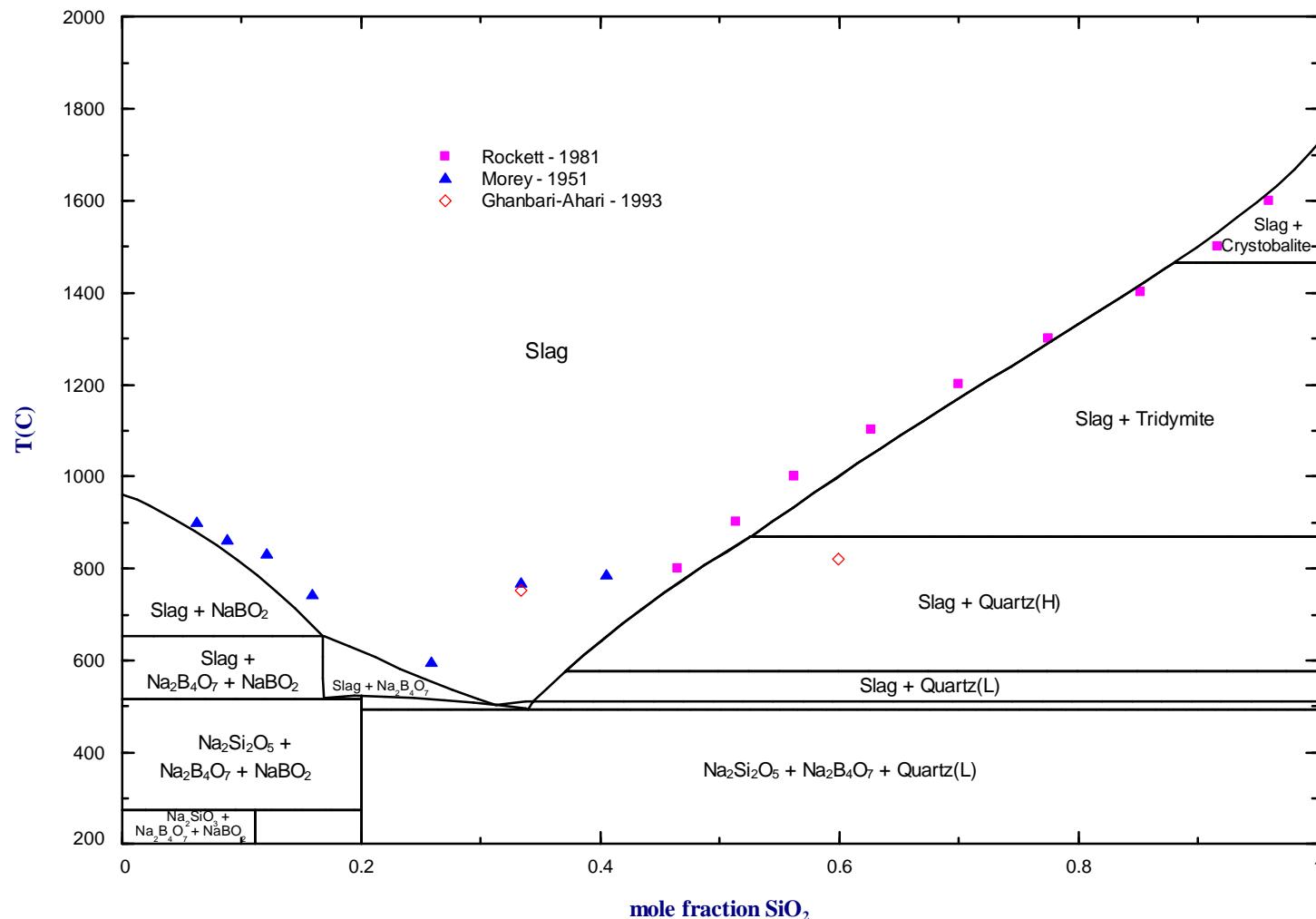
# $\text{SiO}_2\text{-B}_2\text{O}_3\text{-Na}_2\text{O}$ Liquidus Projection



# $\text{SiO}_2\text{-B}_2\text{O}_3\text{-Na}_2\text{O}$ Subsolidus Miscibility Gap

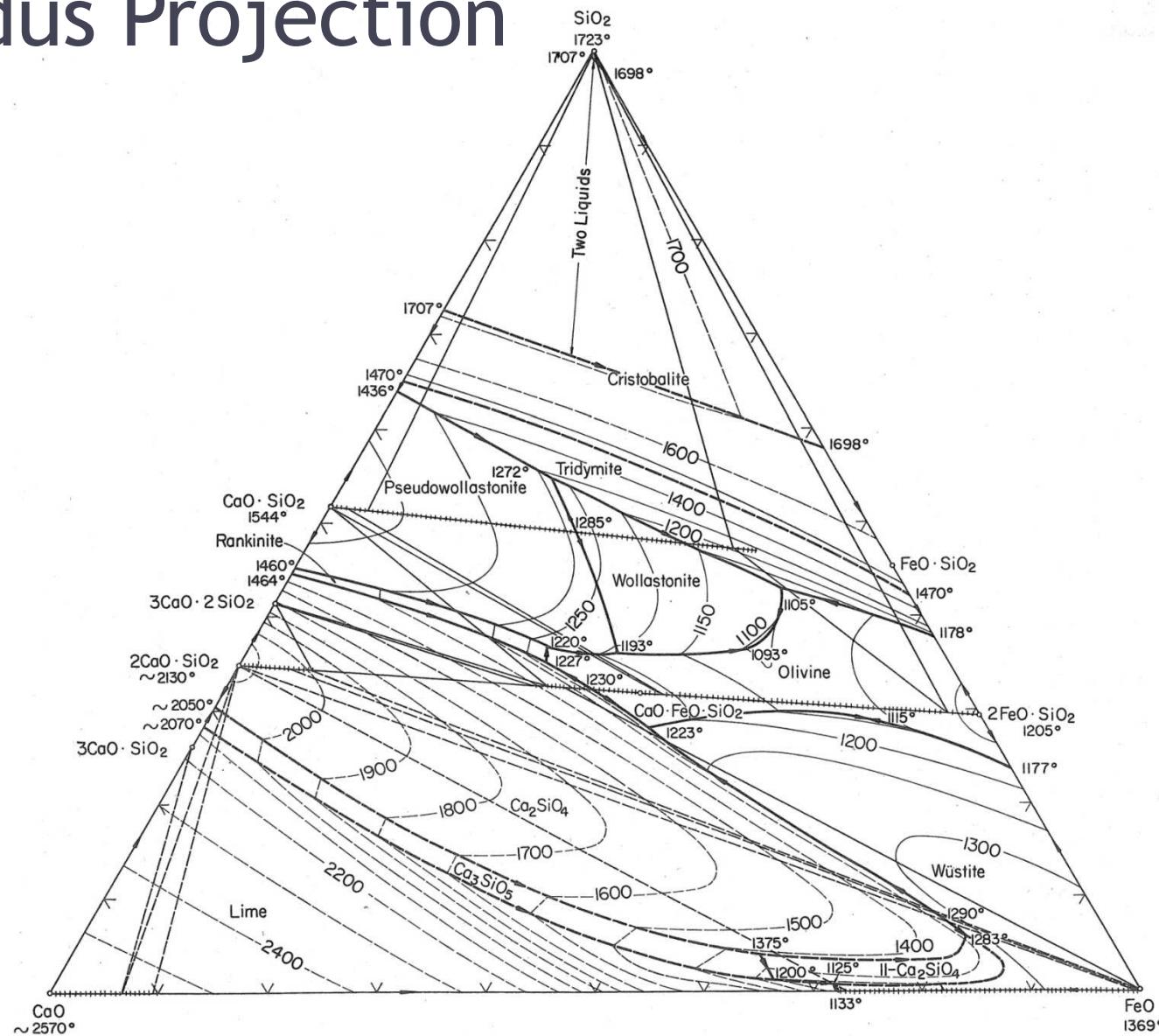


# $\text{Na}_2\text{O}$ - $\text{B}_2\text{O}_3$ - $\text{SiO}_2$ System: Liquidus along the $(\text{NaBO}_2)/2$ - $\text{SiO}_2$ section (close to an ideal liquid solution)

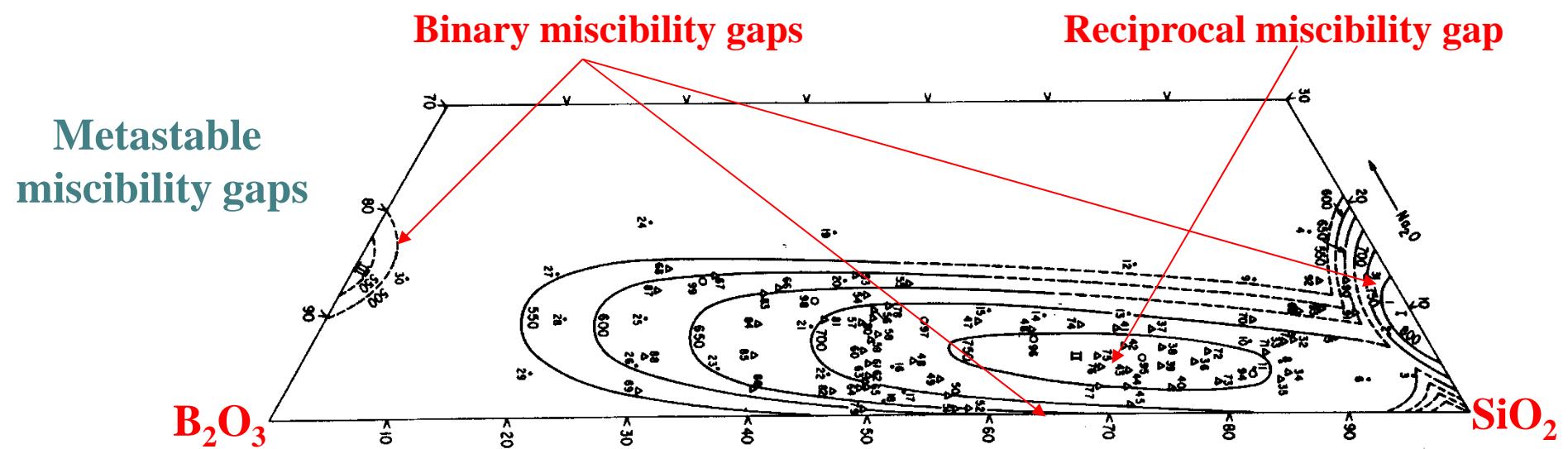


# $\text{SiO}_2\text{-CaO-FeO}$

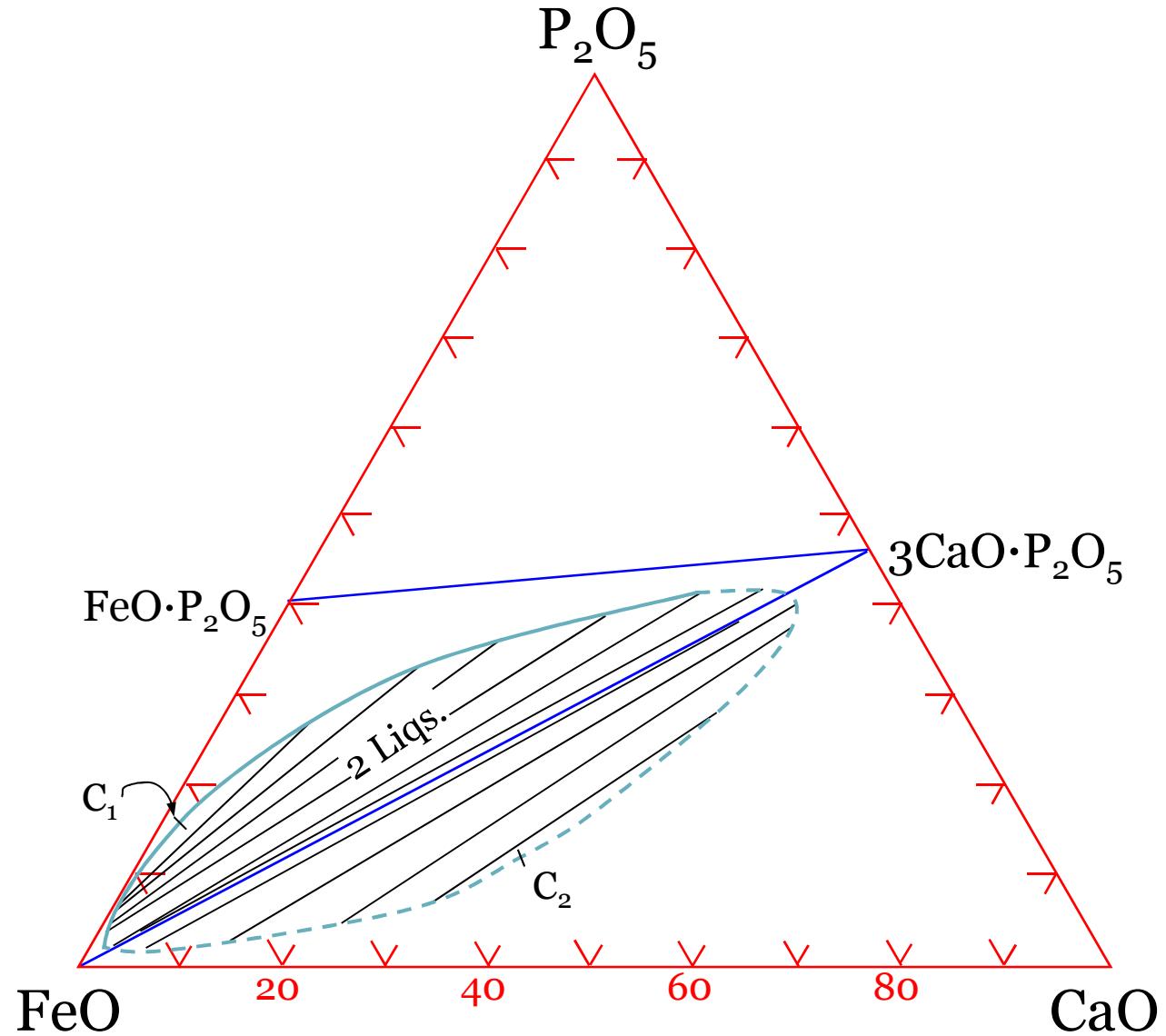
## Liquidus Projection



# $\text{SiO}_2\text{-B}_2\text{O}_3\text{-Na}_2\text{O}$ Subsolidus Miscibility Gap



# CaO-FeO-P<sub>2</sub>O<sub>5</sub> System



# Thermodynamic Modeling of Solutions

The simplest example:

A "regular" solution in which the molecules of each component are randomly distributed on a quasilattice:

$$\begin{aligned} g(\text{molar}) &= (x_1 g_1^0 + x_2 g_2^0 + x_3 g_3^0 + \dots) \\ &+ RT(x_1 \ln x_1 + x_2 \ln x_2 + x_3 \ln x_3) \\ &+ \alpha_{12} x_1 x_2 + \alpha_{23} x_2 x_3 + \alpha_{31} x_3 x_1 + \dots + \alpha_{123} x_1 x_2 x_3 + \dots \end{aligned}$$

where:  $x_i$  = mole fraction of component  $i$

$g_i^0$  = Gibbs function of pure component  $i$

$\alpha_{ij}$  = empirical binary parameter of the model

$\alpha_{123}$  = empirical ternary parameter of the model

$\alpha_{ij}$  represents the energy of forming  $i-j$  nearest neighbour bonds upon mixing.

$\alpha_{ij}$  may be expanded as an empirical power series:

$$\alpha_{ij} = \sum q_{ij}^k (x_i - x_j)^k$$

The empirical parameters  $q_{ij}^k$  are found by fitting experimental data.

- For molten oxides a more sophisticated model is required.
- We use the Modified Quasichemical Model (MQM).



- Consider a random distribution of second-nearest-neighbor cation pairs.
- Model parameters are the Gibbs energies of the pair-exchange reactions such as:

$$[Ca\text{-}Ca]_{\text{pair}} + [Si\text{-}Si]_{\text{pair}} = 2 [Ca\text{-}Si]_{\text{pair}} \quad \Delta g_{CaSi} < 0$$

$$G = \left( n_{SiO_2} G_{SiO_2}^0 + n_{CaO} G_{CaO}^0 + \dots \right)$$

$$-T \Delta S^{\text{config}} + \sum_{n>m} n_{mn} (\Delta g_{mn}/2)$$

**where :**  $n_i$ ,  $G_i^0$  = number of moles and Gibbs energy of component i in solution

$n_{mn}$  = number of moles of [m-n] pairs at equilibrium

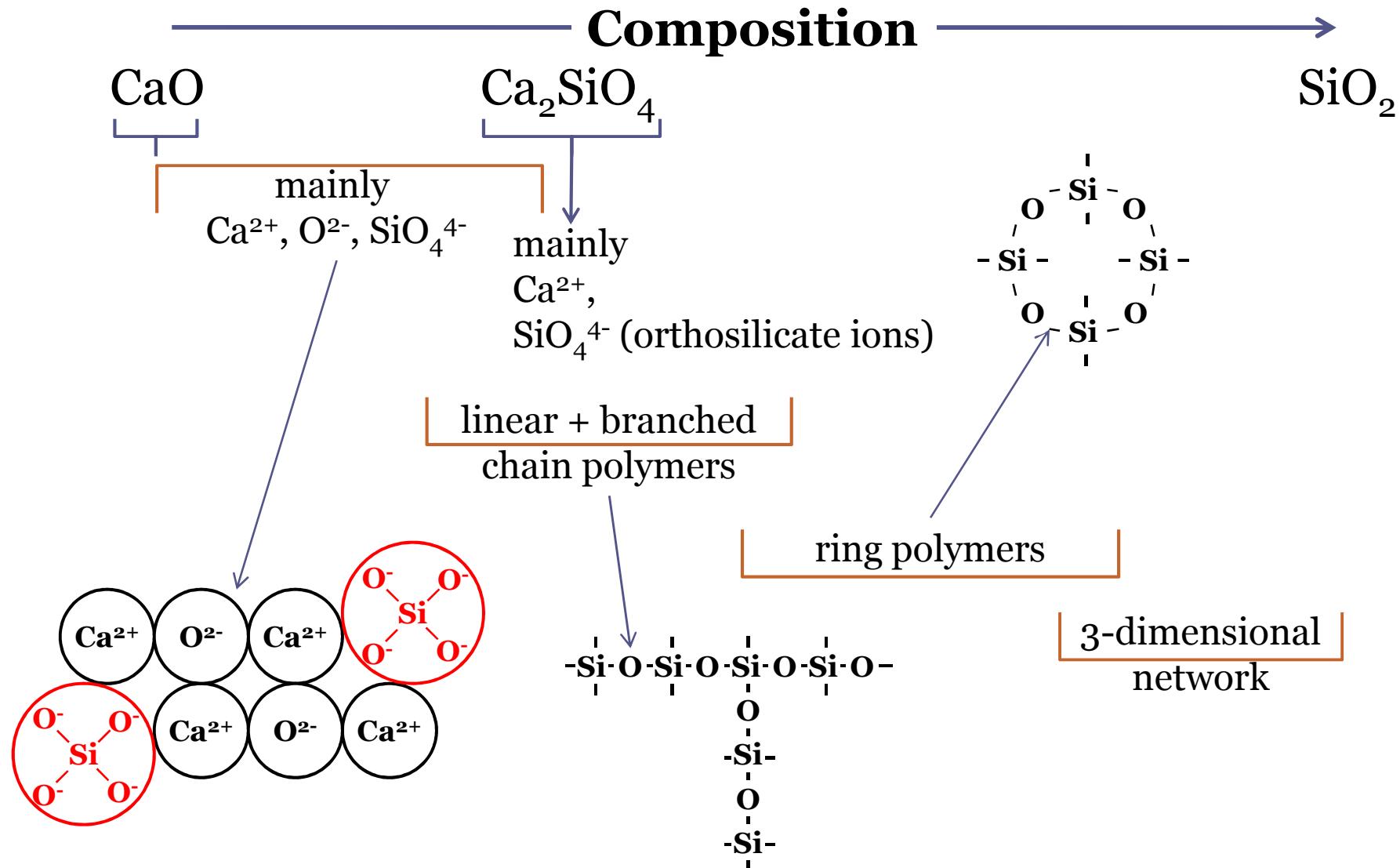
$\Delta S^{\text{config}}$  = (Ising) entropy for random distribution of pairs = function of  $n_i$  and  $n_{mn}$

$\Delta g_{mn}$  = empirical binary model parameters  
(which are functions of composition and temperature)

(The equilibrium values of  $n_{mn}$  are obtained by setting  $\partial G / \partial n_{mn} = 0$  at constant  $n_i$ )

Binary model parameters are optimized by fitting experimental data.

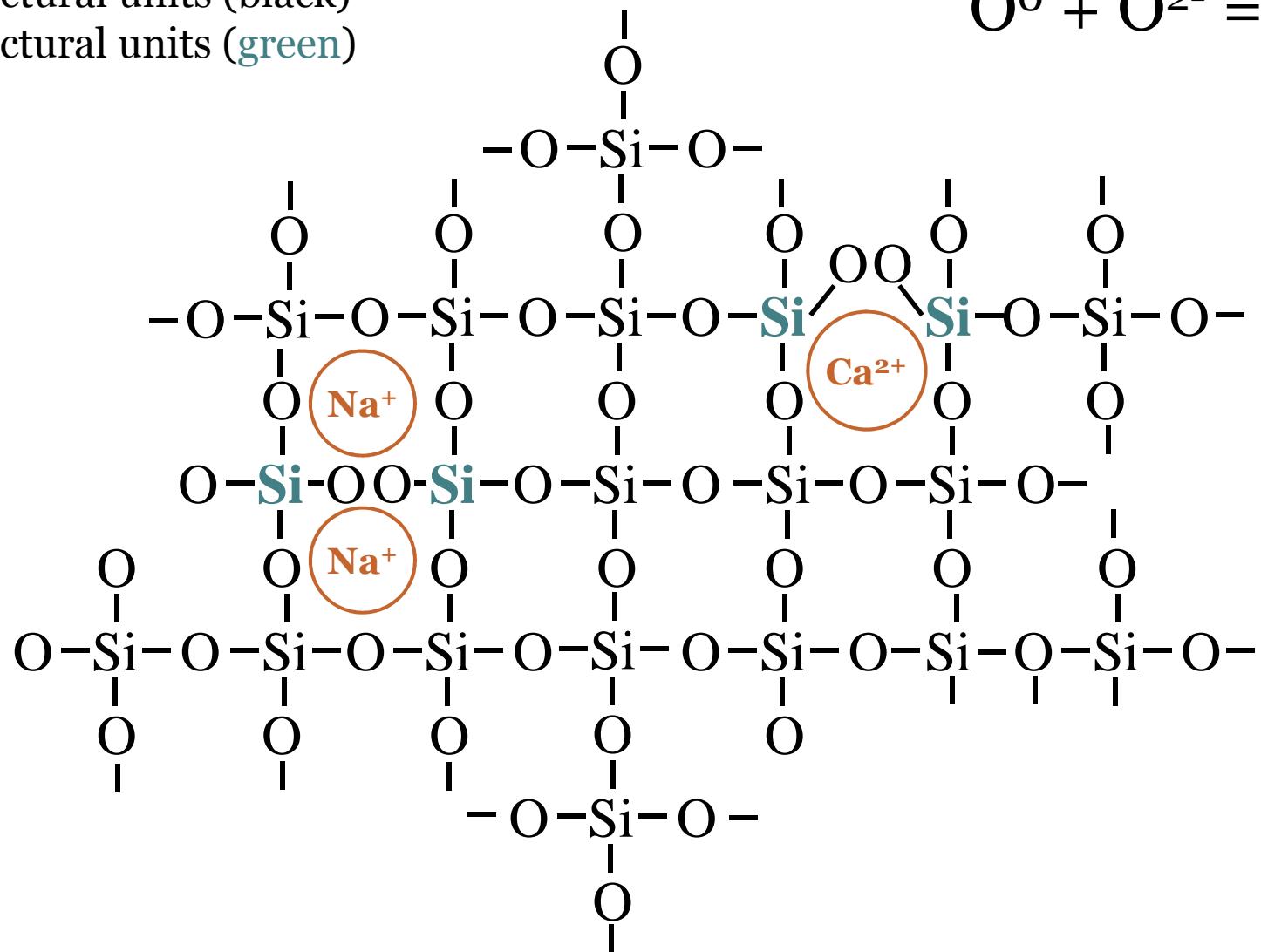
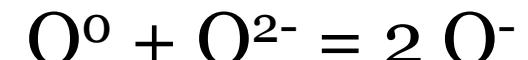
# Structure of CaO-SiO<sub>2</sub> Liquid Solutions



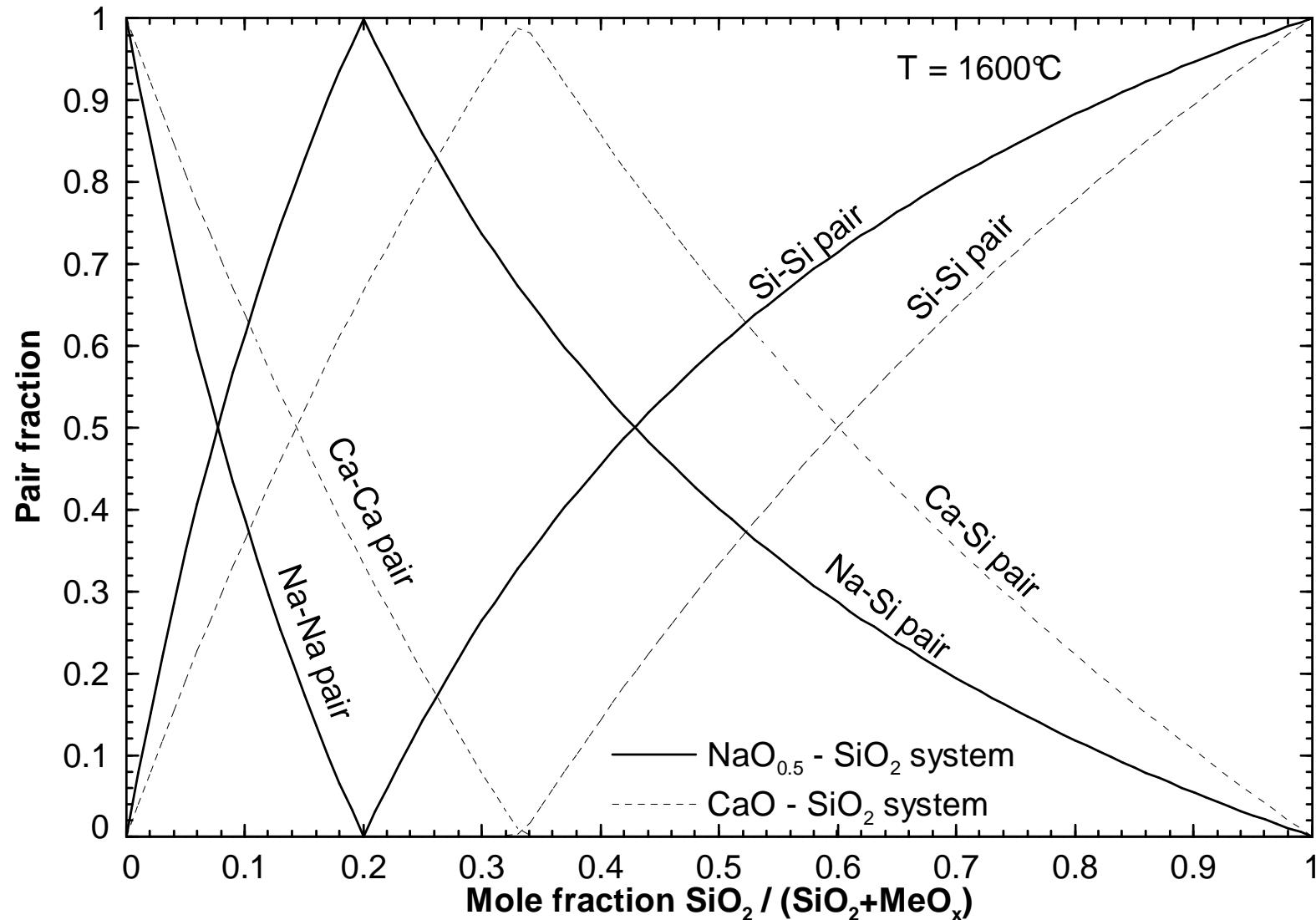
# Network Modification by Basic Oxides

Q<sup>4</sup> structural units (black)

Q<sup>3</sup> structural units (green)



# Pair Fractions in the Systems $\text{CaO}-\text{SiO}_2$ and $\text{NaO}_{0.5}-\text{SiO}_2$



# Thermodynamic Database Development

Modeling and Phase Diagram Calculation in Oxide Systems

**Several thermodynamic software/database packages** with applications in materials science have been developed over the last 30 years.

- These packages all contain large **critically evaluated** databases for thousands of compounds and hundreds of solution phases, as well as user interfaces of varying degrees of user-friendliness.
  - **HSC Chemistry**
  - **MTS-NPL**
  - **Thermo-Calc**
  - **Thermodata**
  - **FactSage**

- **Thermochemical databases** contain parameters giving the **Gibbs energy**, **G**, of all compounds as functions of T (and P) and of all solutions as functions of T, (P) and composition. This is a complete description because all the other thermodynamic properties ( $H$ ,  $C_p$ ,  $\mu$ , etc.) can be calculated by taking the appropriate derivatives of the G functions.
- **For a given set of constraints** (such as temperature, total pressure, total mass of each element) the **software** calculates the equilibrium conditions by **minimizing the total Gibbs energy** of the system. This is mathematically equivalent to solving all the equilibrium constant equations simultaneously.
- Data are automatically extracted as required from the databases.

# How a thermodynamic database is developed by evaluation/optimisation

There are many kinds of chemical thermodynamic data for compounds and solutions:

- **Calorimetric data:**
  - Heat capacity
  - Solution calorimetry
  - Enthalpy of mixing
  - ...
- **Vapour pressures**
- **Phase equilibria:**
  - Solid/liquid/gas
  - Phase diagrams (T-P-Composition)
- **Chemical potentials or activities**
  - From electrochemical cells
  - From phase equilibria (vapour pressures, isopiestic, ...)
  - ...
- **...(and so on)**

These diverse kinds of data are not independent of each other, but are related through the **GIBBS FUNCTIONS** of the phases.

For each phase (compound or solution):

$$G = G(T, P, \text{Composition})$$

**Then:**  $H(\text{enthalpy or "heat"}) = \left[ \frac{\partial \left( \frac{G}{T} \right)}{\partial \left( \frac{1}{T} \right)} \right]_{P, \text{Composition}}$

$$C_p(\text{heat capacity}) = \left( \frac{dH}{dT} \right)_P$$

$$S(\text{entropy}) = - \left( \frac{\partial G}{\partial T} \right)_{P, \text{composition}}$$

$$\mu_i = \frac{(\text{chemical potential of component } i \text{ of a solution})}{=} \left( \frac{\partial G}{\partial n_i} \right)_{T, P, n_j} \quad (\text{where } n_i = \text{moles of } i)$$

**When phases are in equilibrium:**

$$\begin{aligned} \mu_i(\text{in phase } \alpha) &= \mu_i(\text{in phase } \beta) \text{ for all components } i \\ &= \mu_i(\text{in phase } \gamma) \\ &= \dots \end{aligned}$$

**... (and so on)**

- Therefore, in developing a database for a multicomponent chemical system, one assesses and evaluates ALL the data SIMULTANEOUSLY in order to obtain an optimal Gibbs function,  $G(T, P, \text{Composition})$ , for each phase.
- The resultant database is then thermodynamically self-consistent.
- The optimized Gibbs functions are stored in the database (as sets of parameters). All thermodynamic properties and phase equilibria can then be calculated from these functions.

- Step 1): **Develop a mathematical model for each solution phase based upon the structure of the solution.**

**The simplest example:**

a “regular” solution in which the atoms or molecules of each component are randomly distributed.

$$\begin{aligned}G(\text{molar}) = & \left( X_1 G_1^\circ + X_2 G_2^\circ + X_3 G_3^\circ + \dots \right) \\& + RT \left( X_1 \ln X_1 + X_2 \ln X_2 + \dots \right) \\& + \alpha_{12} X_1 X_2 + \alpha_{23} X_2 X_3 + \alpha_{31} X_3 X_1 + \dots\end{aligned}$$

Where:  $X_i$  = mole fraction of component  $i$   
 $G_i^\circ$  = Gibbs function of pure component  $i$   
 $\alpha_{ij}$  = empirical parameters of the model

- **Step 2):**

**Obtain the parameters of the models by simultaneous critical evaluation/optimization of all available data of all kinds (thermodynamic data, phase equilibria data, structural data) (generally for 2- and 3-component systems.)**

- **Step 3):**

**Store parameters and use models to estimate properties of N-component phases using optimized 2- and 3-component parameters.**

- **Step 4):**

**Calculate complex phase equilibria by minimization of the Gibbs energy of the total system.**

$$G(\text{total system}) = n_{\alpha}G^{\alpha} + n_{\beta}G^{\beta} + n_{\gamma}G^{\gamma} + \dots$$

*Where:  $n_{\alpha}, n_{\beta}, n_{\gamma}, \dots$  = numbers of moles of phases  $\alpha, \beta, \gamma, \dots$  at equilibrium*

*$G^{\alpha}, G^{\beta}, G^{\gamma}, \dots$  = molar Gibbs function of each phase*

# The FACT OXIDE DATABASE

## Components

- **Major:**
  - (completely evaluated and modeled at all compositions and temperatures)  
 $\text{Al}_2\text{O}_3 - \text{CaO} - \text{FeO} - \text{Fe}_2\text{O}_3 - \text{MgO} - \text{SiO}_2 -$
- **Secondary:**
  - (extensively evaluated, particularly with the major components, and particularly over composition ranges of practical importance)  
 $\text{B}_2\text{O}_3 - \text{CrO} - \text{Cr}_2\text{O}_3 - \text{MnO} - \text{Na}_2\text{O} - \text{NiO} - \text{PbO} -$   
 $\text{Ti}_2\text{O}_3 - \text{TiO}_2 - \text{ZnO} - \text{ZrO}_2 -$
- **Minor:**
  - (evaluated for some combinations with other components)  
 $\text{As}_2\text{O}_3 - \text{Cu}_2\text{O} - \text{K}_2\text{O} - \text{SnO}$

# The FACT OXIDE DATABASE

## Liquid Solution

- Modeled for all oxide components

**Also: Non-oxide components (in dilute solution)**

S, SO<sub>4</sub>, PO<sub>4</sub>, CO<sub>3</sub>, H<sub>2</sub>O, OH, F, Cl, Br, I

**> 150 Solid Stoichiometric Compounds**

# The FACT Oxide Database

## Major Oxide Solid Solutions

- **Spinel:** (Al, Co<sup>2+</sup>, Co<sup>3+</sup>, Cr<sup>2+</sup>, Cr<sup>3+</sup>, Fe<sup>2+</sup>, Fe<sup>3+</sup>, Mg, Ni<sup>2+</sup>, Zn)  
[Al, Co<sup>2+</sup>, Co<sup>3+</sup>, Cr<sup>3+</sup>, Fe<sup>2+</sup>, Fe<sup>3+</sup>, Mg, Ni<sup>2+</sup>, Zn, □]<sub>2</sub>O<sub>4</sub>
- **Pyroxenes:** (Ca, Fe<sup>2+</sup>, Mg)<sup>M<sub>2</sub></sup>(Fe<sup>2+</sup>, Fe<sup>3+</sup>, Mg, Al)<sup>M<sub>1</sub></sup>(Fe<sup>3+</sup>, Al, Si)<sup>B</sup>Si<sup>A</sup>O<sub>6</sub>
- **Olivine:** (Ca, Fe<sup>2+</sup>, Mg, Mn, Ni, Co, Zn)[Ca, Fe<sup>2+</sup>, Mg, Mn, Ni, Co, Zn]SiO<sub>4</sub>
- **Melilite:** (Ca)<sub>2</sub>[Mg, Fe<sup>2+</sup>, Fe<sup>3+</sup>, Al, Zn]{Fe<sup>3+</sup>, Al, Si}<sub>2</sub>O<sub>7</sub>
- **Monoxide:** CaO - MgO - MnO - CoO - NiO - FeO  
(+ Fe<sub>2</sub>O<sub>3</sub> - Al<sub>2</sub>O<sub>3</sub> - ZnO - Cr<sub>2</sub>O<sub>3</sub>)
- **α-Ca<sub>2</sub>SiO<sub>4</sub>:** α-Ca<sub>2</sub>SiO<sub>4</sub> (+ Fe<sub>2</sub>SiO<sub>4</sub>, Mg<sub>2</sub>SiO<sub>4</sub>, Mn<sub>2</sub>SiO<sub>4</sub>)
- **α'-Ca<sub>2</sub>SiO<sub>4</sub>:** α'-Ca<sub>2</sub>SiO<sub>4</sub> (+ Fe<sub>2</sub>SiO<sub>4</sub>, Mg<sub>2</sub>SiO<sub>4</sub>, Mn<sub>2</sub>SiO<sub>4</sub>, Pb<sub>2</sub>SiO<sub>4</sub>, Zn<sub>2</sub>SiO<sub>4</sub>)
- **Wollastonite:** CaSiO<sub>3</sub> (+ FeSiO<sub>3</sub>, MgSiO<sub>3</sub>, MnSiO<sub>3</sub>)
- **Corundum:** Al<sub>2</sub>O<sub>3</sub> - Cr<sub>2</sub>O<sub>3</sub> - Fe<sub>2</sub>O<sub>3</sub>
- **Ilmenite:** (Fe<sup>2+</sup>, Mg, Mn, Ti<sup>3+</sup>) (Ti<sup>4+</sup>, Ti<sup>3+</sup>)O<sub>3</sub>
- **Pseudobrookite:** (Fe<sup>2+</sup>, Mg, Mn, Ti<sup>3+</sup>) (Ti<sup>4+</sup>, Ti<sup>3+</sup>)<sub>2</sub>O<sub>5</sub>
- **26 other solid solutions**

# Sublattice Model - Compound Energy Formalism

- **Used for solid solutions**

- Example:

Spinel Solution ( $A^{2+}, A^{3+}, B^{2+}, C^{3+}, \dots$ ) $[A^{2+}, A^{3+}, B^{2+}, C^{3+}, \dots]O_4$

$$G = \sum_i \sum_j Y'_i Y''_j G_{ij} - TS^{config} + G^E$$

where:  $Y'_i, Y''_j$  = site fractions on first and second sublattices

$$S^{config} = -R \left( \sum_i Y'_i \ln Y'_i + 2 \sum_j Y''_j \ln Y''_j \right) = \text{configurational entropy}$$

$$G^E = \sum_i \sum_j \sum_k Y'_i Y'_j Y''_k L_{ijk} + \sum_i \sum_j \sum_k Y''_k Y''_i Y'_j L_{k:ij}$$

(usually  $G^E = 0$  or contains only a very few small parameters  $L_{ijk}$ )

$G_{ij}$  = “end-member Gibbs energies” (one for each ion pair)

The  $G_{ij}$  are the main parameters of the formalism.

## (Sublattice Model - Compound Energy Formalism)

- End-member Gibbs energies  $G_{ij}$  are the **formalism parameters**.
- Some may be equal to Gibbs energies of real compounds,
- In other cases, certain linear combinations of the  $G_{ij}$  have physical significance, and these combinations are the **model parameters**.
  - Example:

$\text{Fe}_3\text{O}_4$  spinel:  $(\text{Fe}^{2+}, \text{Fe}^{3+}) [\text{Fe}^{2+}, \text{Fe}^{3+}]_2\text{O}_4$

- Four end-member Gibbs energies:

$$G_{\text{Fe}^{2+}\text{Fe}^{2+}}, G_{\text{Fe}^{2+}\text{Fe}^{3+}}, G_{\text{Fe}^{3+}\text{Fe}^{2+}}, G_{\text{Fe}^{3+}\text{Fe}^{3+}}$$

$G_{\text{Fe}^{2+}\text{Fe}^{3+}}$  = Gibbs energy of hypothetical normal  $\text{Fe}_3\text{O}_4$

$$\begin{aligned} I &= G_{\text{Fe}^{3+}\text{Fe}^{3+}} + G_{\text{Fe}^{3+}\text{Fe}^{2+}} - 2G_{\text{Fe}^{2+}\text{Fe}^{3+}} \\ &= \text{model parameter related to degree of inversion} \end{aligned}$$

$$\begin{aligned} \Delta &= G_{\text{Fe}^{2+}\text{Fe}^{2+}} + G_{\text{Fe}^{3+}\text{Fe}^{3+}} - G_{\text{Fe}^{3+}\text{Fe}^{2+}} - G_{\text{Fe}^{2+}\text{Fe}^{3+}} \\ &= \text{model parameter related to reciprocal exchange of} \\ &\quad \text{nearest-neighbor pairs} \end{aligned}$$

$(G_{\text{Fe}^{3+}\text{Fe}^{2+}}$  can be arbitrarily set equal to  $G_{\text{Fe}^{2+}\text{Fe}^{3+}}$ )

# Quasichemical Model for Short-Range Ordering

- **Used for the liquid solution**



- Consider a random distribution of second-nearest-neighbor cation pairs.
- Model parameters are the Gibbs energies of the pair-exchange reactions such as:

$$[\text{Ca}-\text{Ca}]_{\text{pair}} + [\text{Si}-\text{Si}]_{\text{pair}} = 2 [\text{Ca}-\text{Si}]_{\text{pair}} \quad \Delta g_{\text{CaSi}} < 0$$

$$G = \left( n_{\text{SiO}_2} G_{\text{SiO}_2}^0 + n_{\text{CaO}} G_{\text{CaO}}^0 + \dots \right)$$

$$-T \Delta S^{\text{config}} + \sum_{n>m} n_{mn} (\Delta g_{mn}/2)$$

**where :**  $n_i$ ,  $G_i^0$  = number of moles and Gibbs energy of component i in solution

$n_{mn}$  = number of moles of [m-n] pairs at equilibrium

$\Delta S^{\text{config}}$  = (Ising) entropy for random distribution of pairs = function of  $n_i$  and  $n_{mn}$

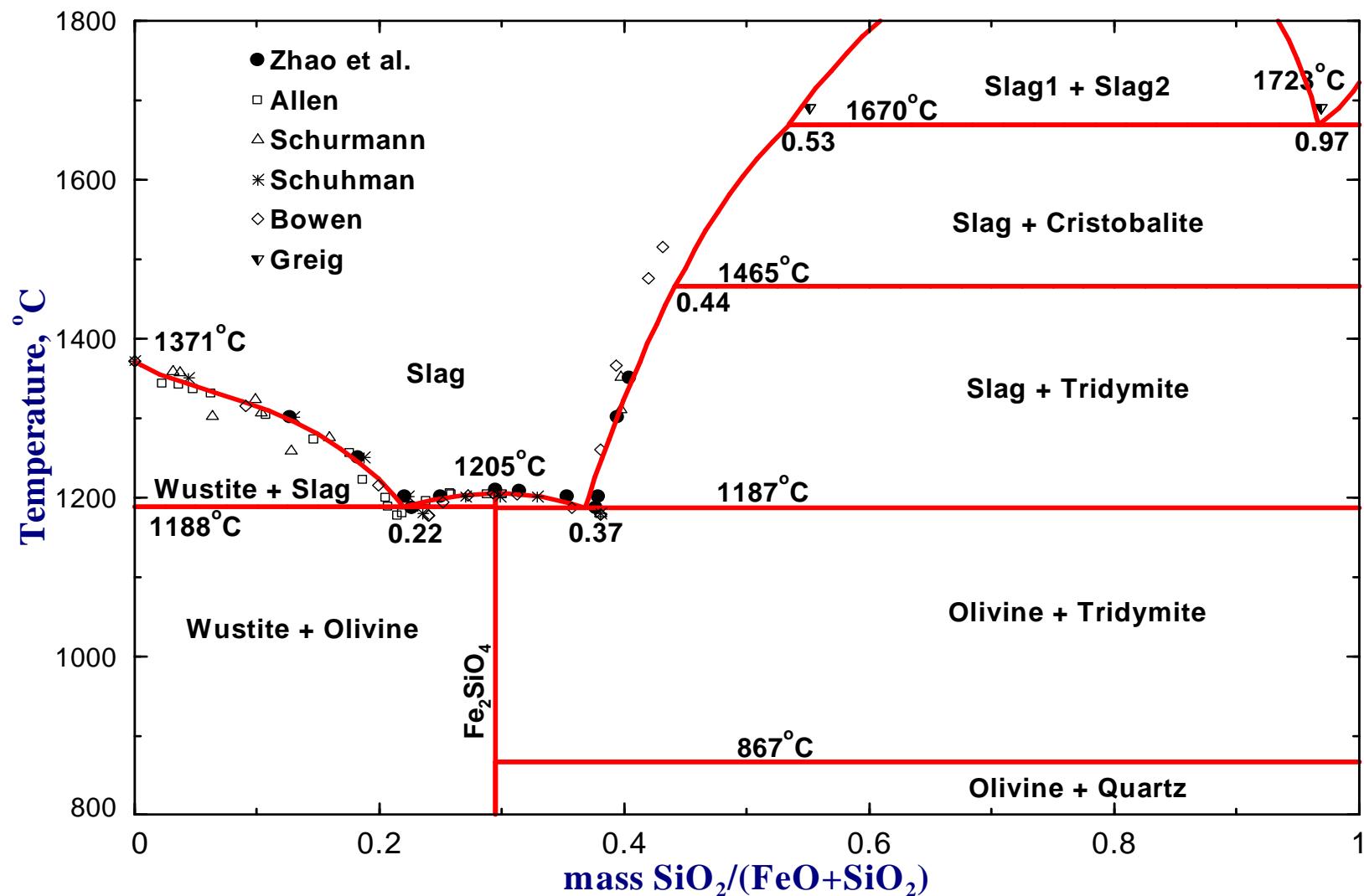
$\Delta g_{mn}$  = binary model parameters

(which may be functions of composition and T)

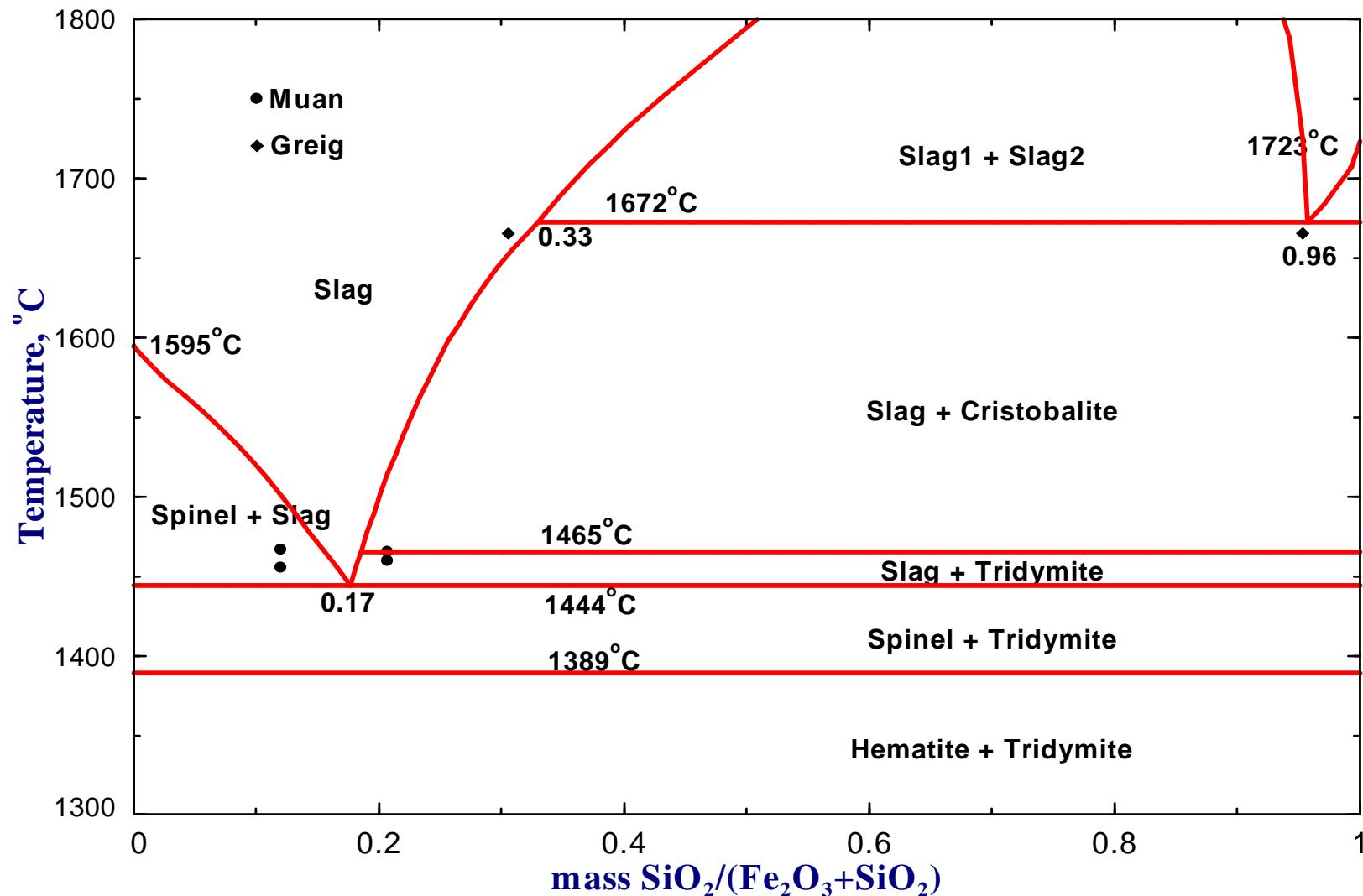
(The equilibrium values of  $n_{mn}$  are obtained by setting  $\partial G / \partial n_{mn} = 0$  at constant  $n_i$ )

Some of the data critically evaluated  
and used in the modeling of the  
 $\text{SiO}_2 - \text{Al}_2\text{O}_3 - \text{CaO} - \text{FeO} - \text{Fe}_2\text{O}_3$   
system, and comparison with  
calculations from the resultant  
optimized database.

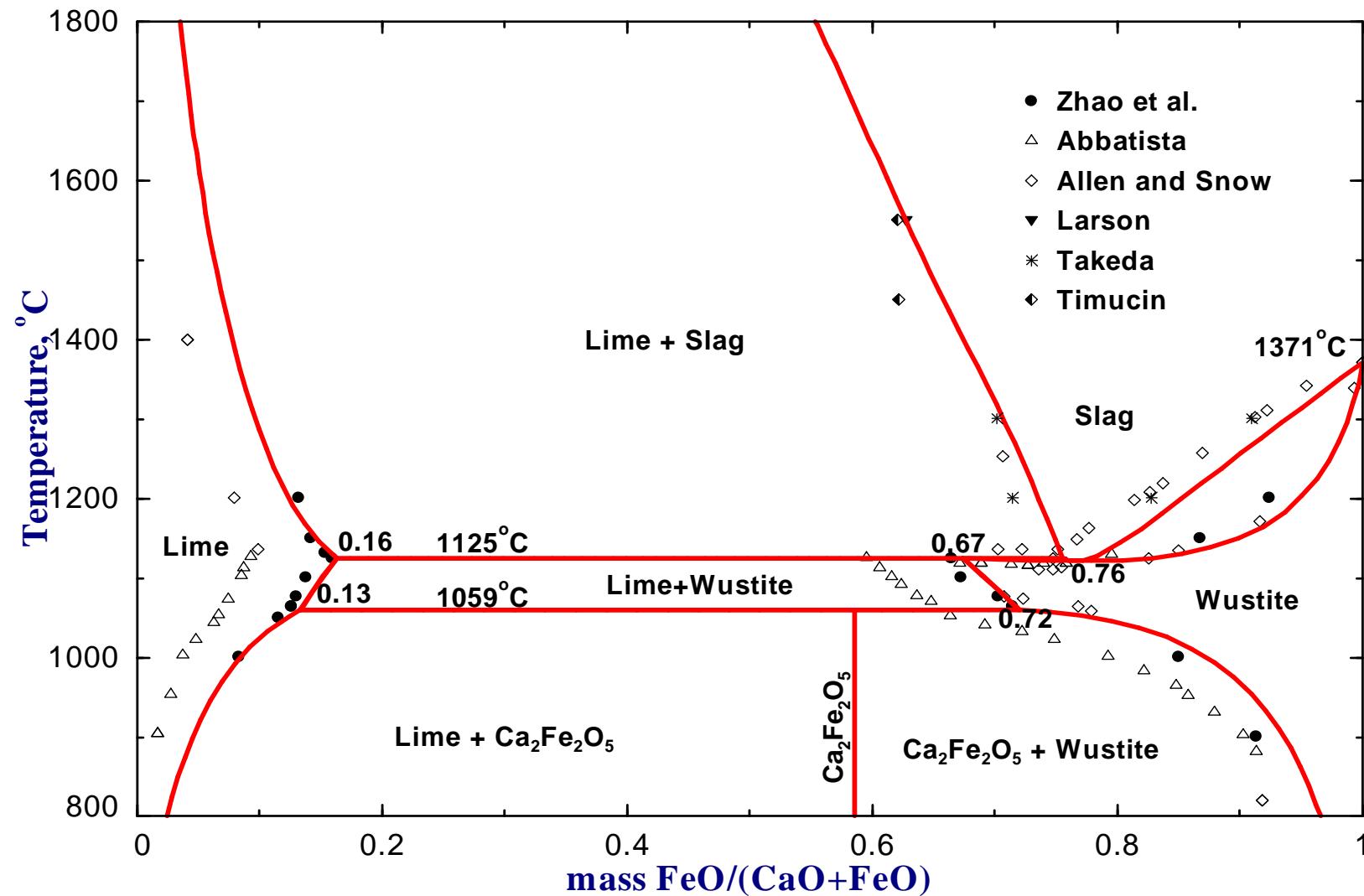
# Calculated Fe-Si-O phase diagram in equilibrium with iron



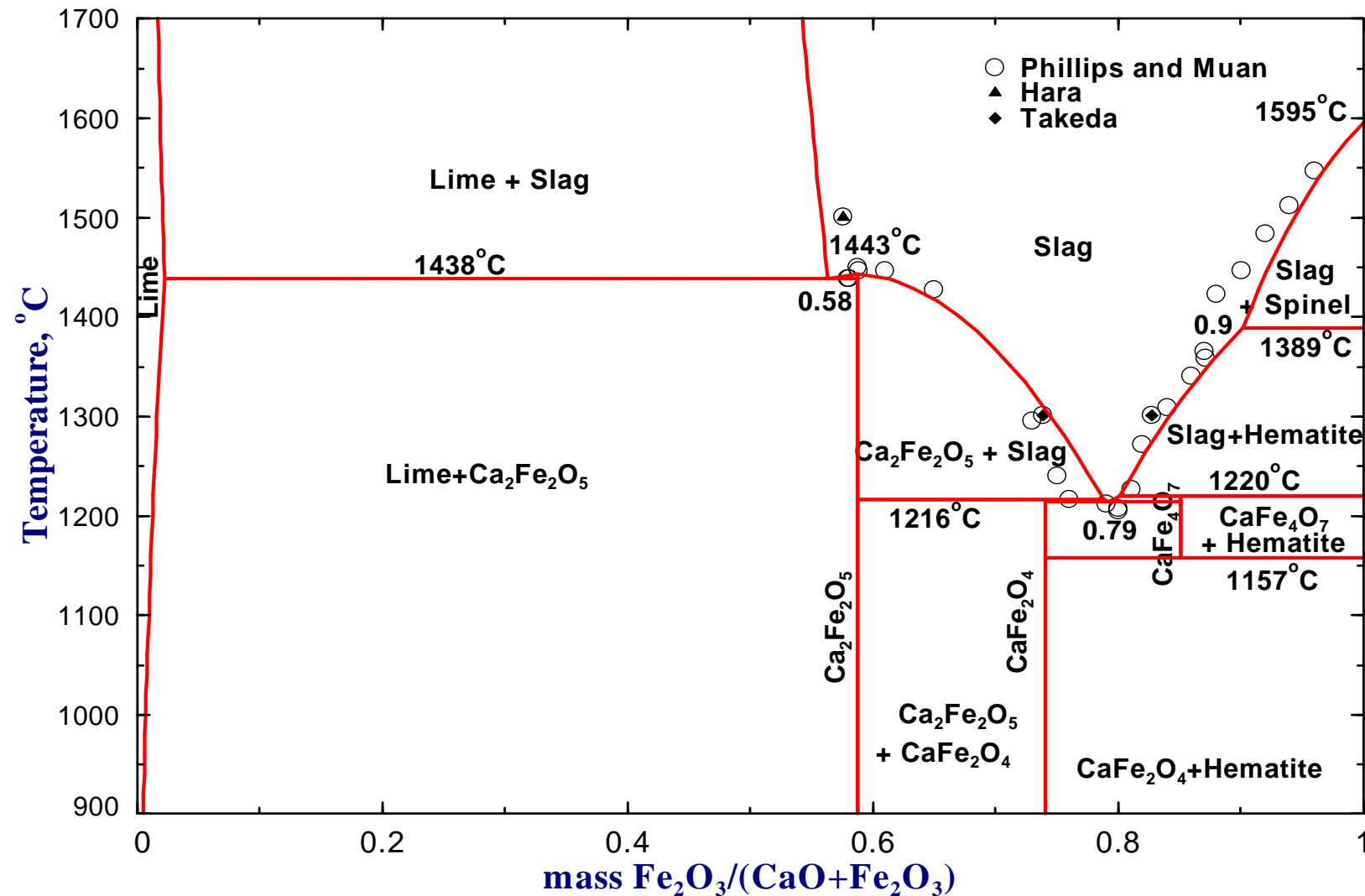
# Calculated Fe-Si-O phase diagram in equilibrium with air



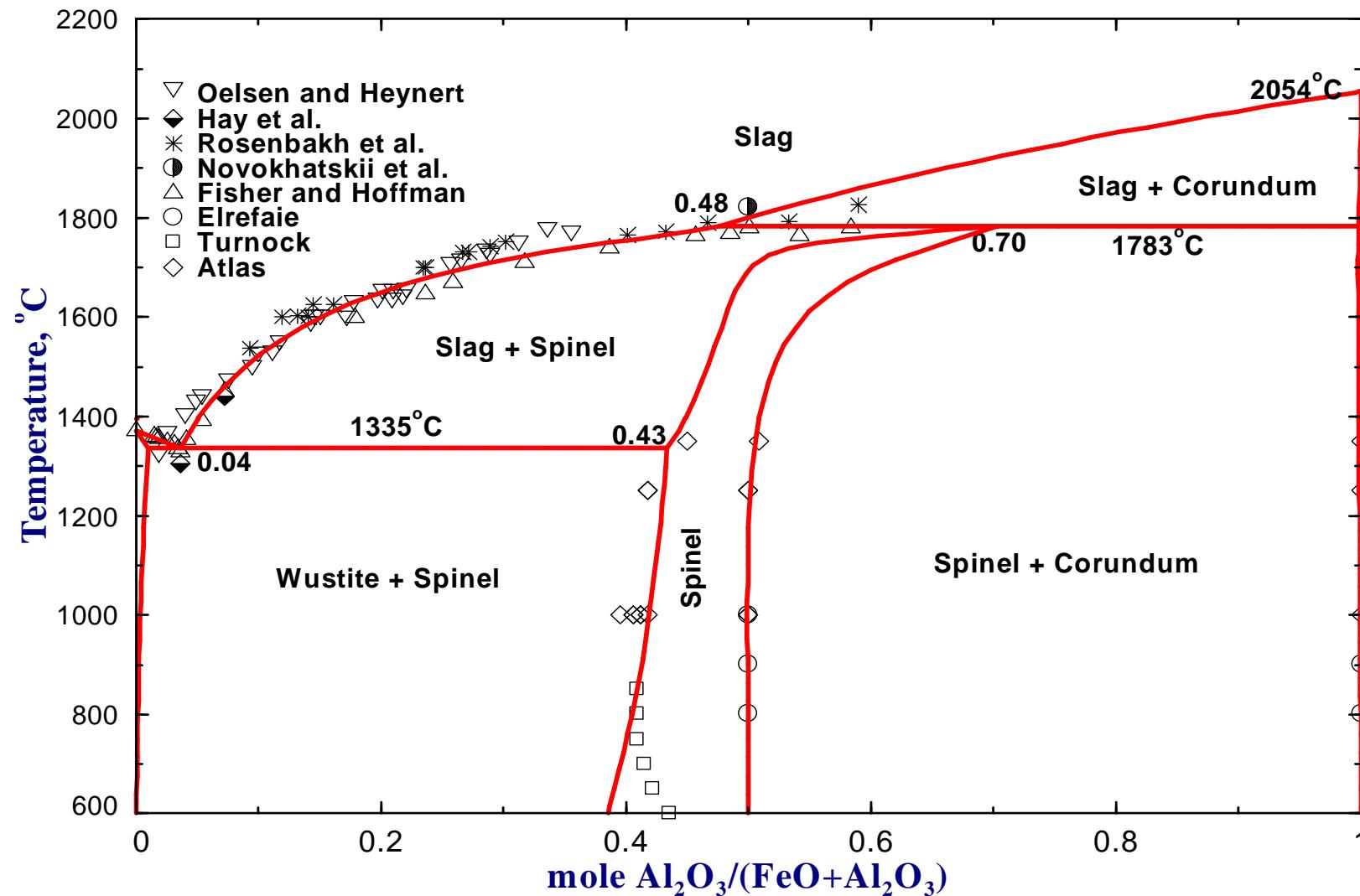
# Calculated Ca-Fe-O phase diagram in equilibrium with iron



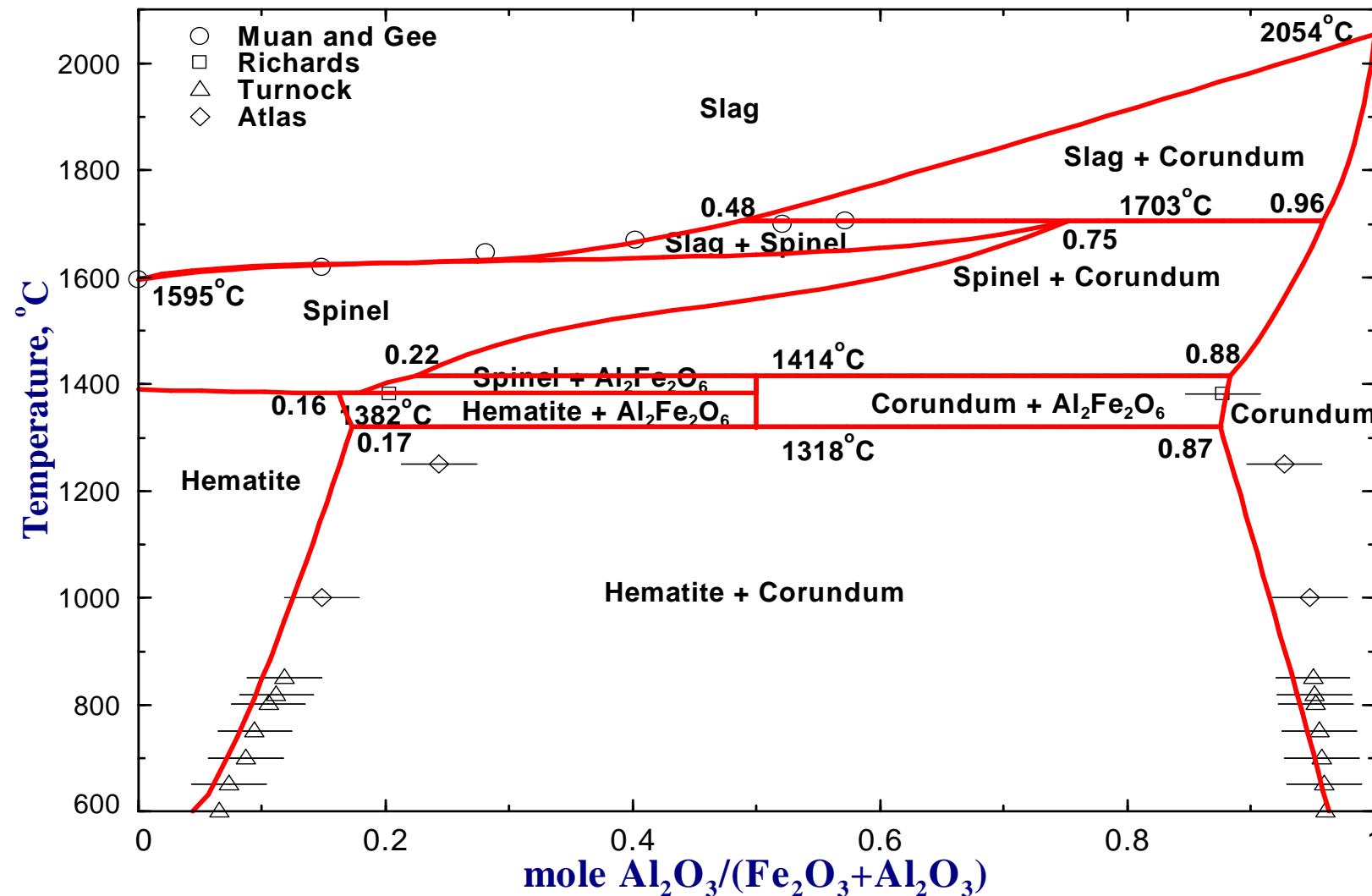
# Calculated Ca-Fe-O phase diagram in equilibrium with air



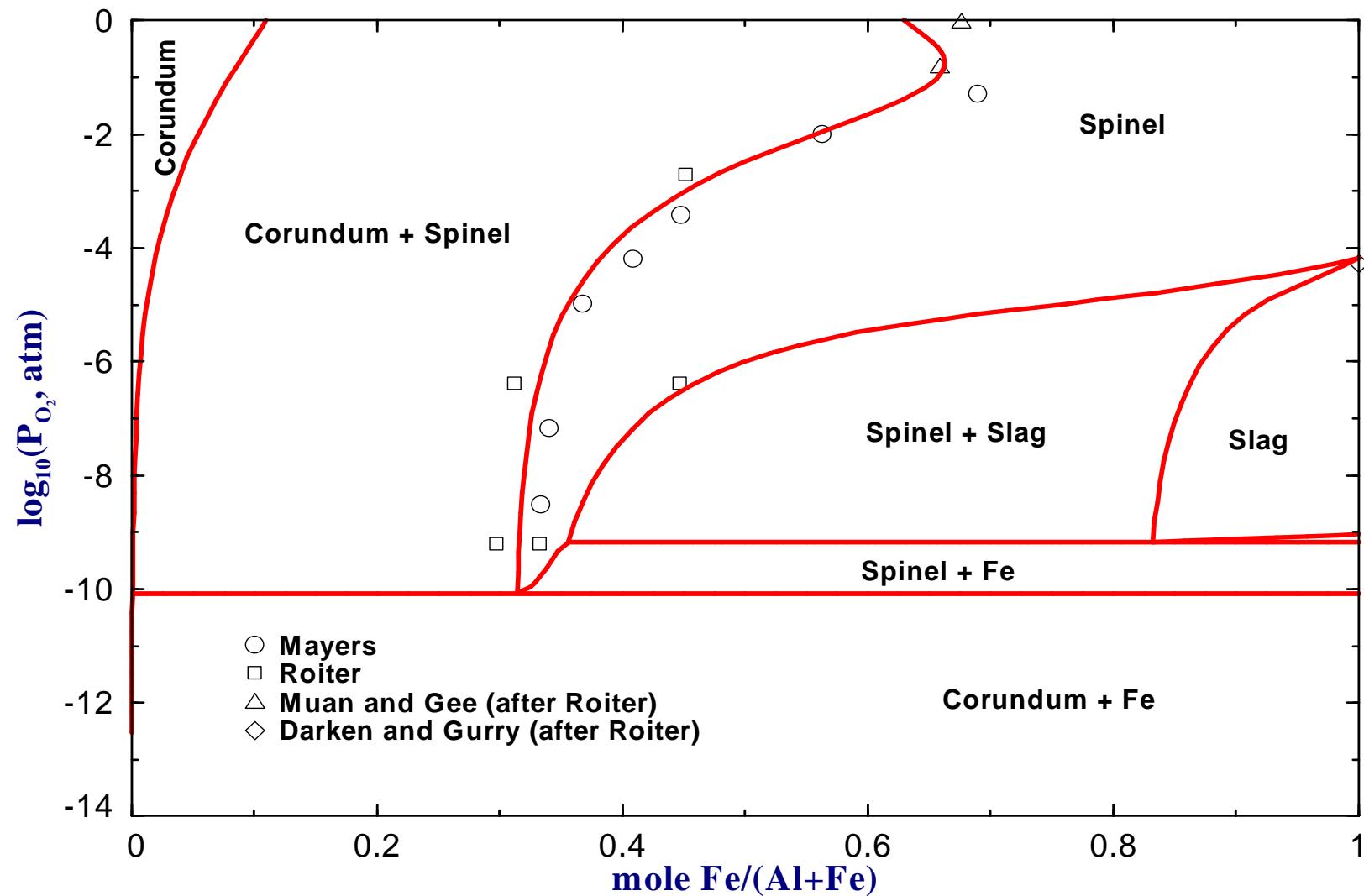
# Calculated FeO-Al<sub>2</sub>O<sub>3</sub> phase diagram in equilibrium with iron



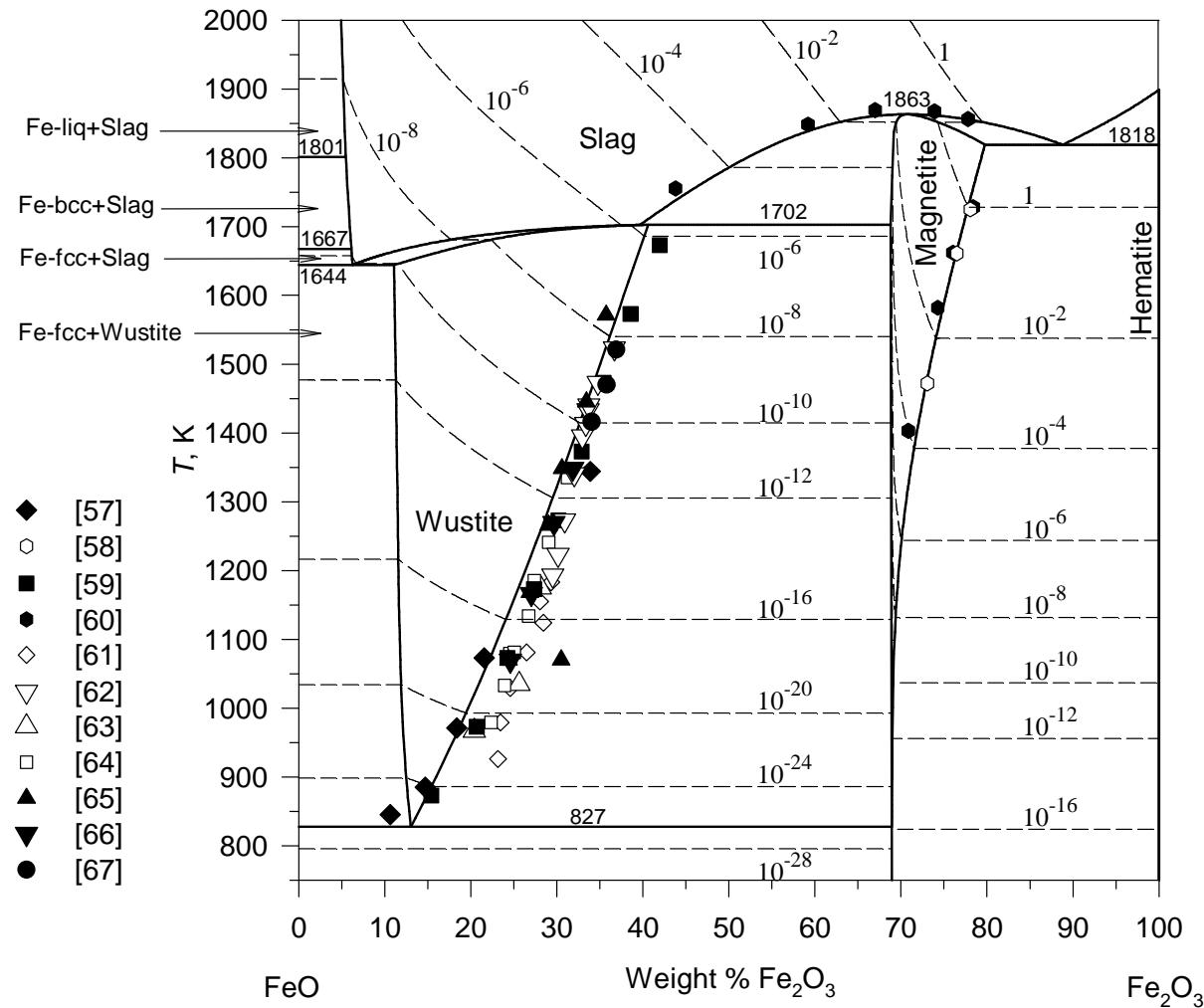
# Calculated Al-Fe-O phase diagram in equilibrium with air



# Calculated Al-Fe-O phase diagram at 1500°C

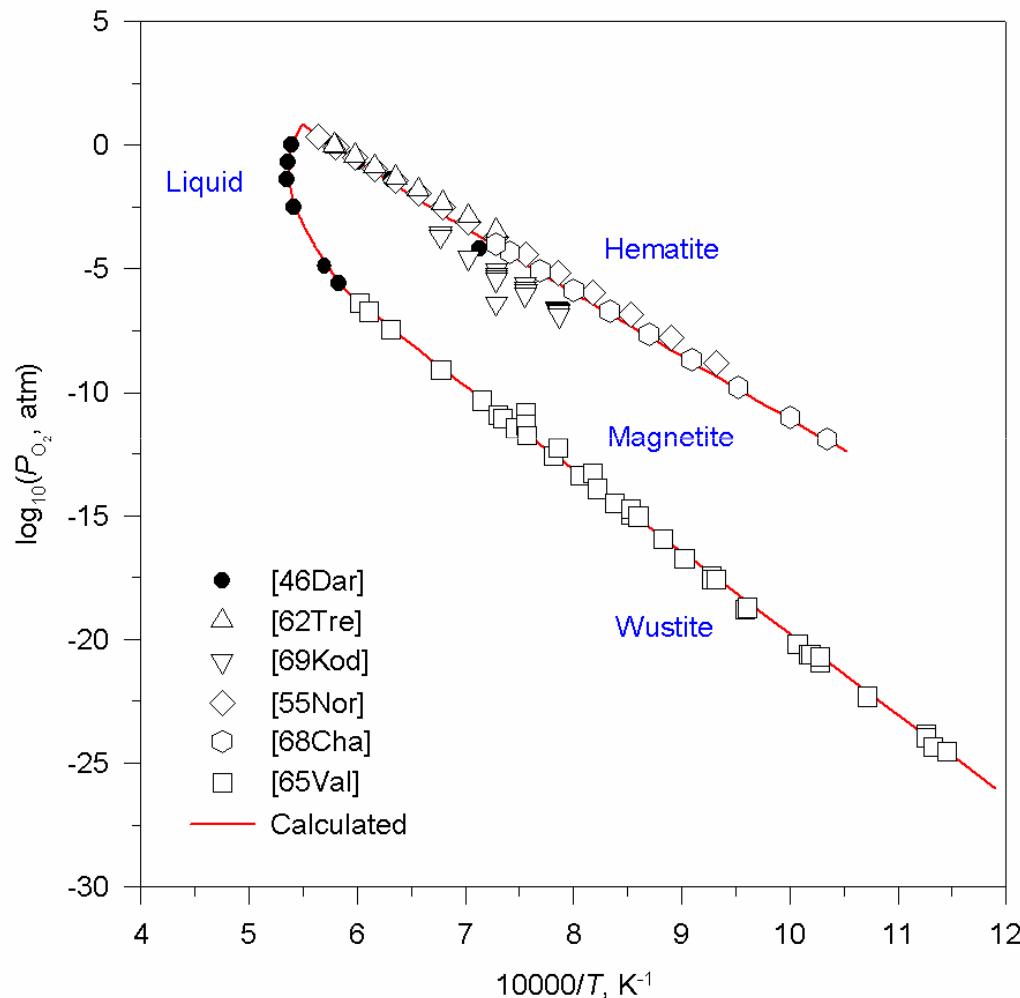


# FeO- $\text{Fe}_2\text{O}_3$ phase diagram

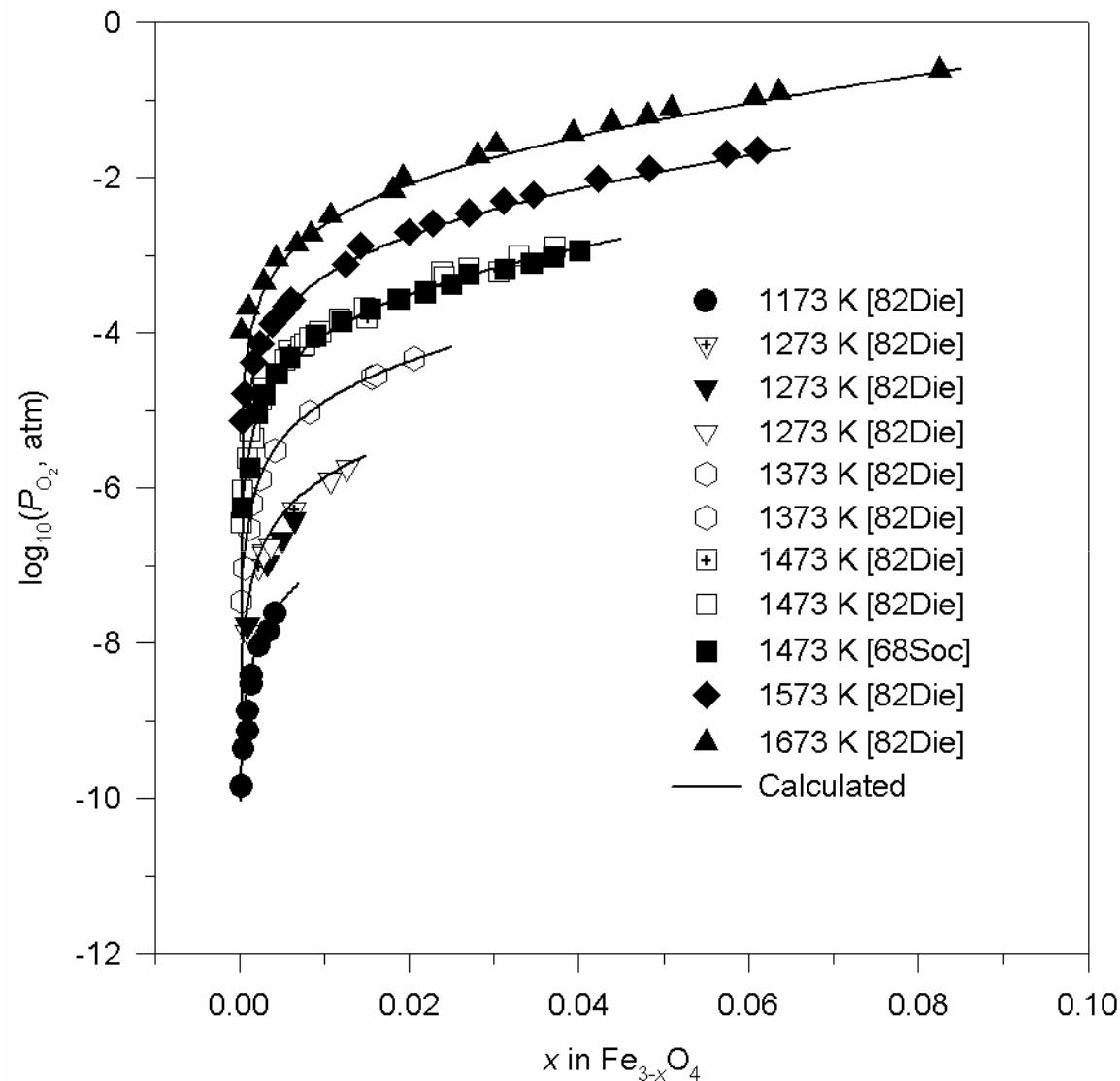


**Selected experimental points and calculated lines and invariant temperatures. Dashed lines are calculated oxygen isobars (bar).**

# Fe-O System



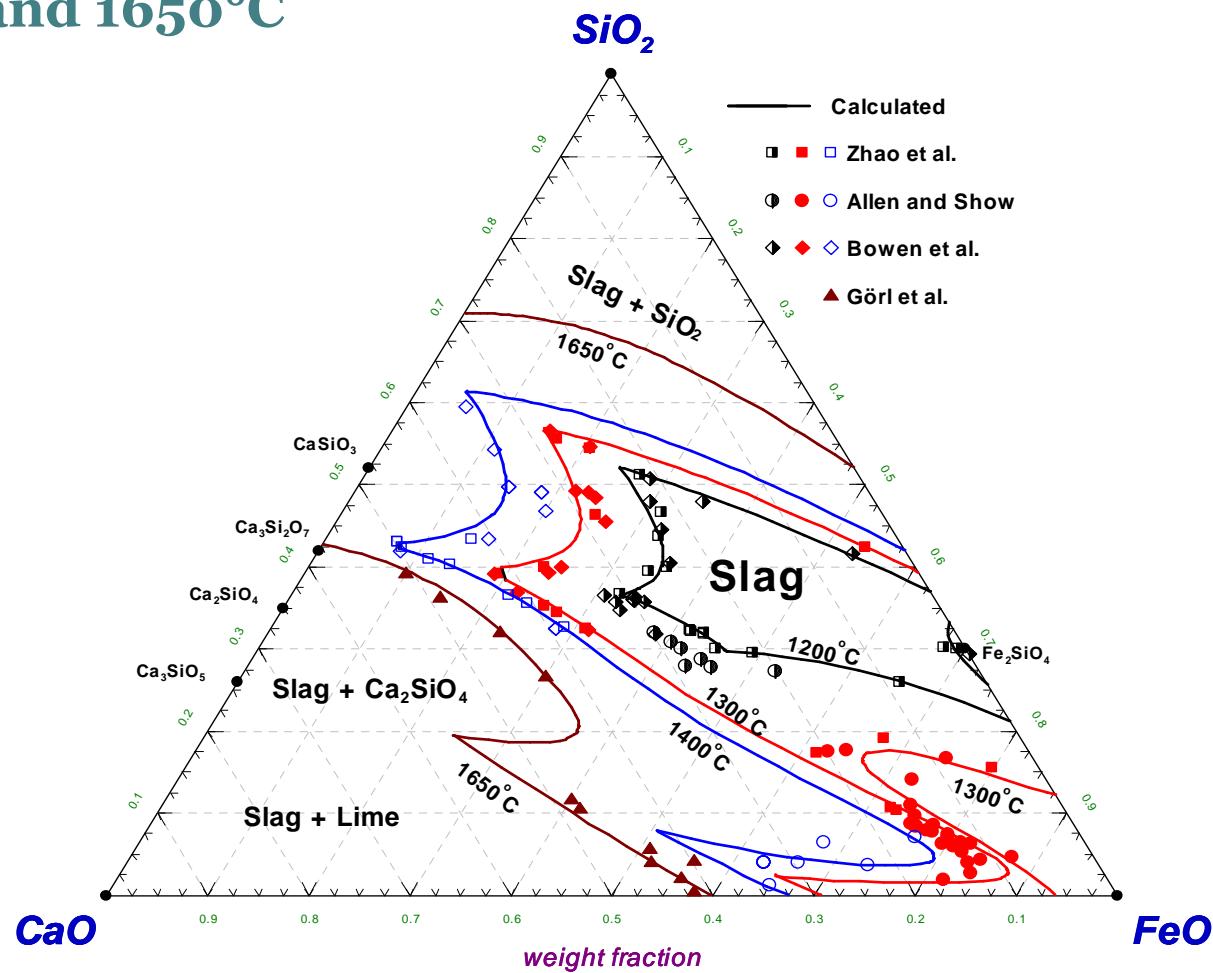
**Oxygen partial pressure for two-phase equilibria  
with magnetite in the Fe-O system.**



**Experimental and calculated oxygen partial pressure over single-phase magnetite as a function of composition.**

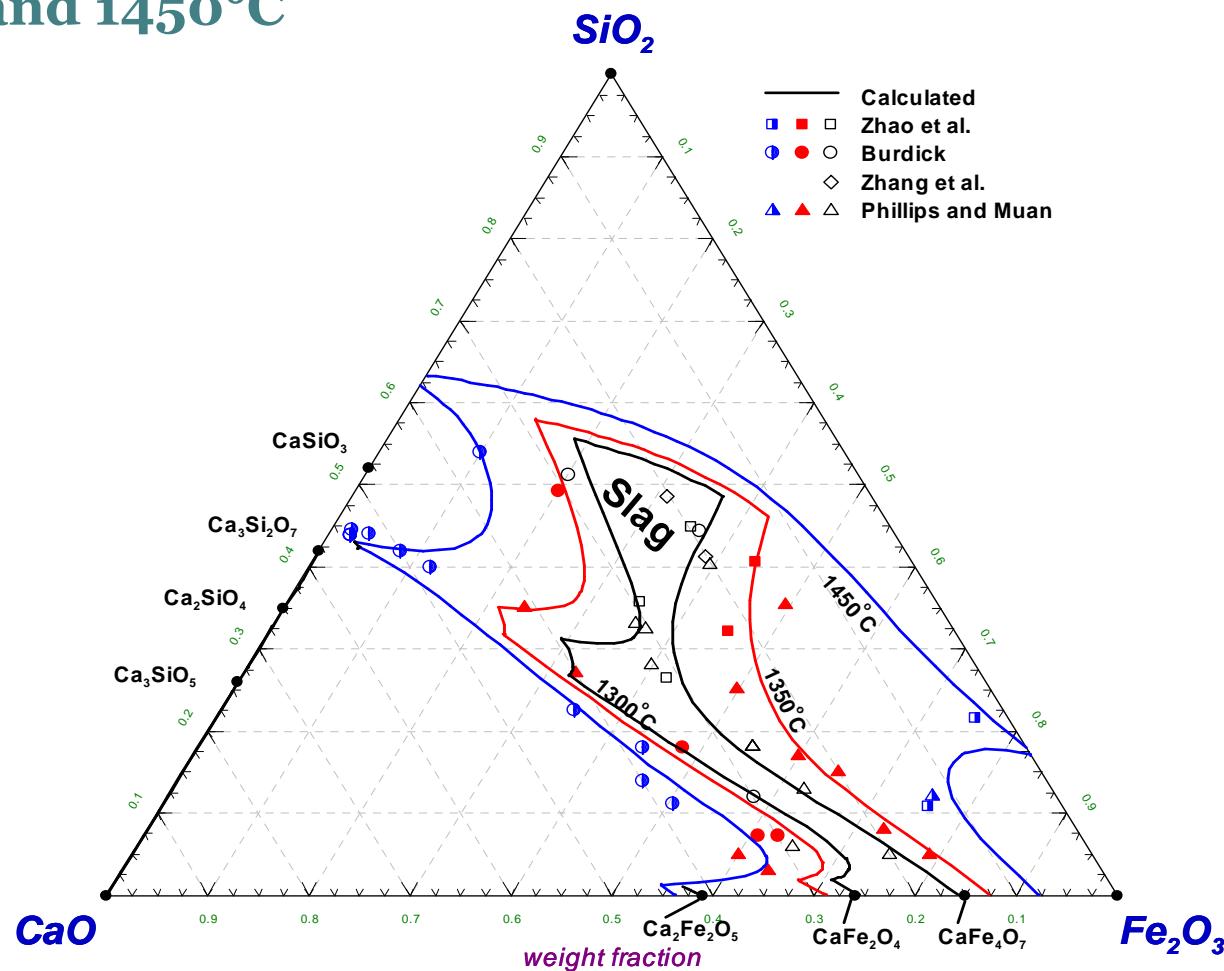
# Liquidus of the Ca-Fe-Si-O system in equilibrium with iron

Temperatures between  
**1200°C and 1650°C**



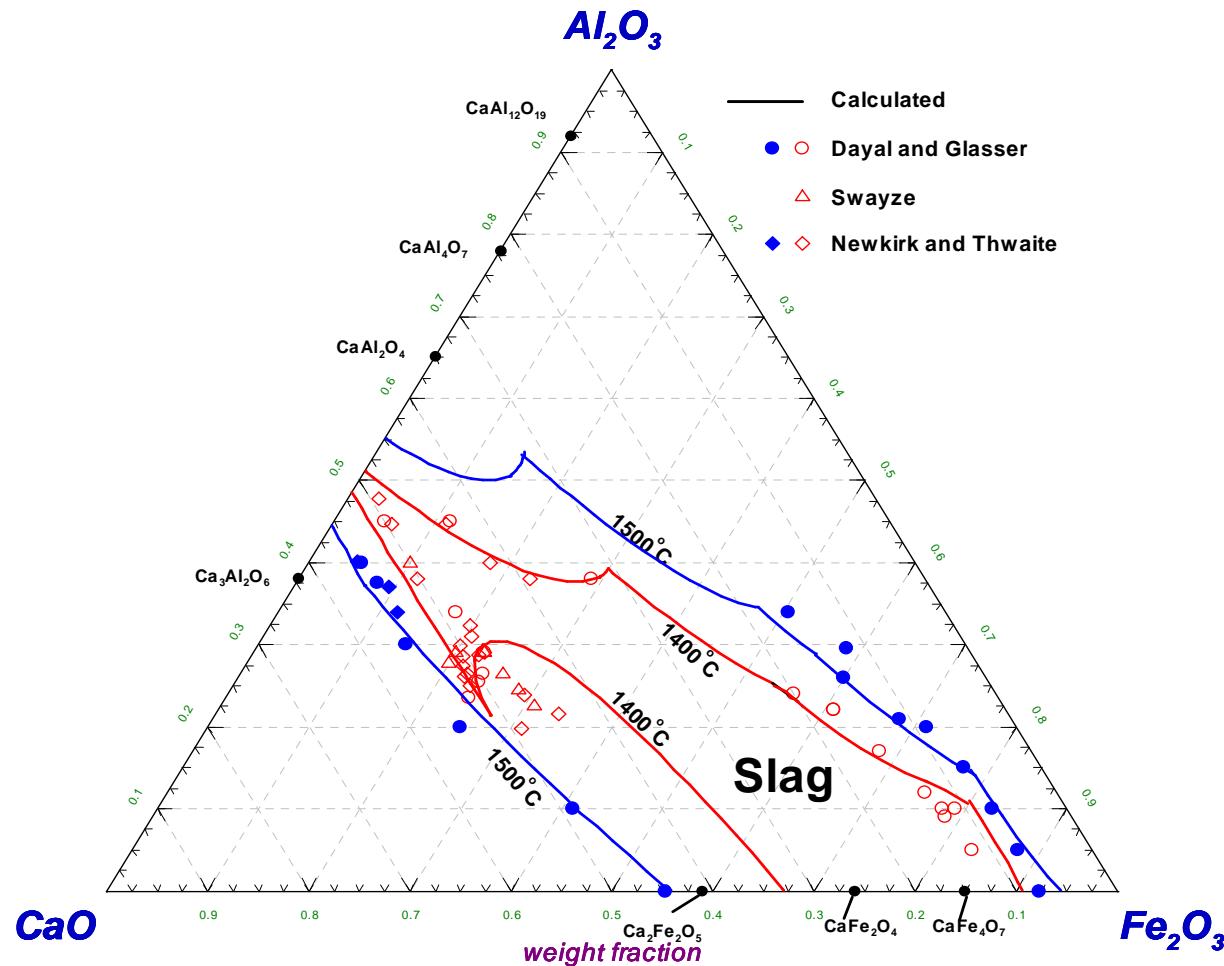
# Liquidus of the Ca-Fe-Si-O system in equilibrium with air

Temperatures between  
1300°C and 1450°C

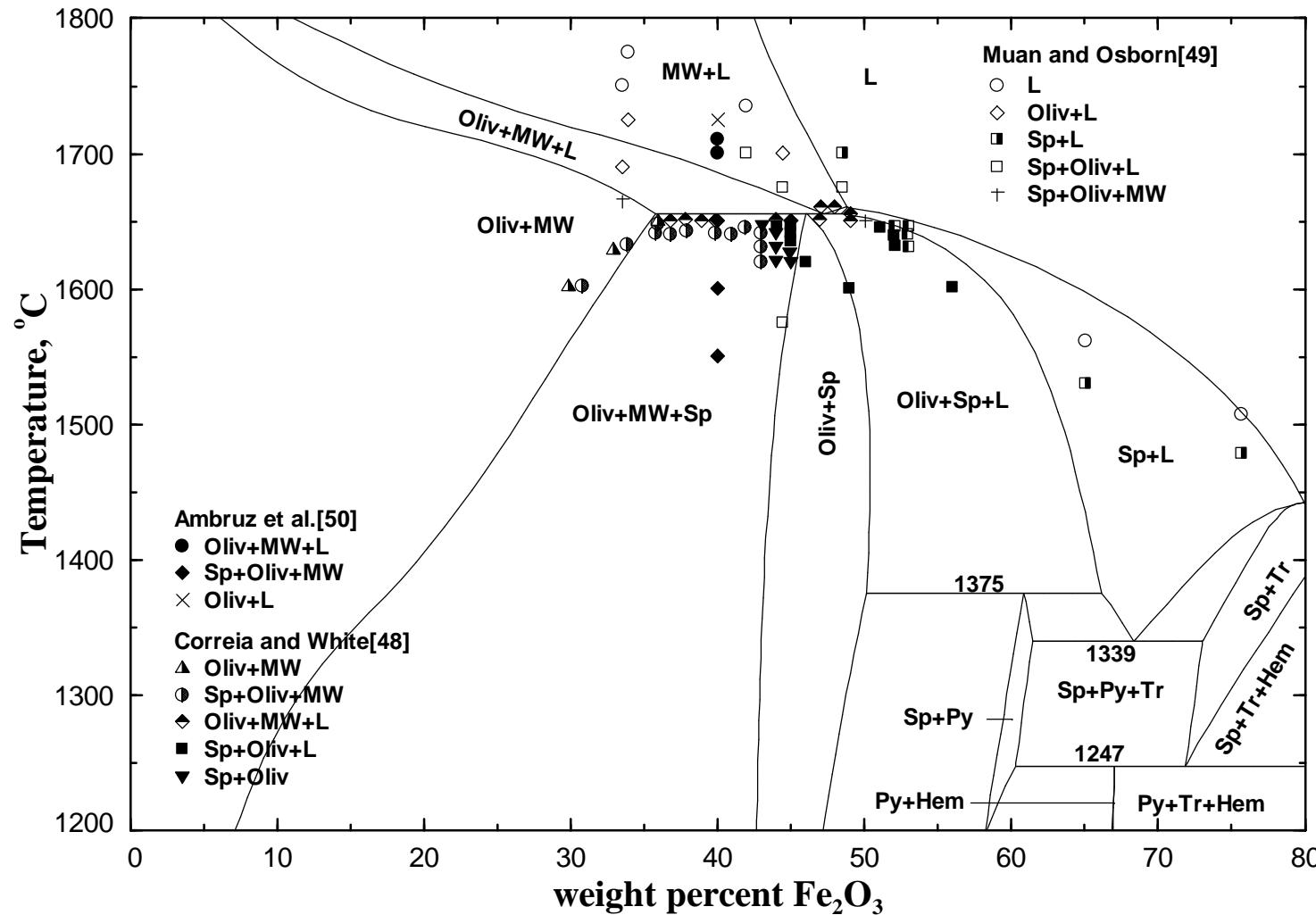


# Liquidus of the Al-Ca-Fe-O system in equilibrium with air

At 1400°C and 1500°C



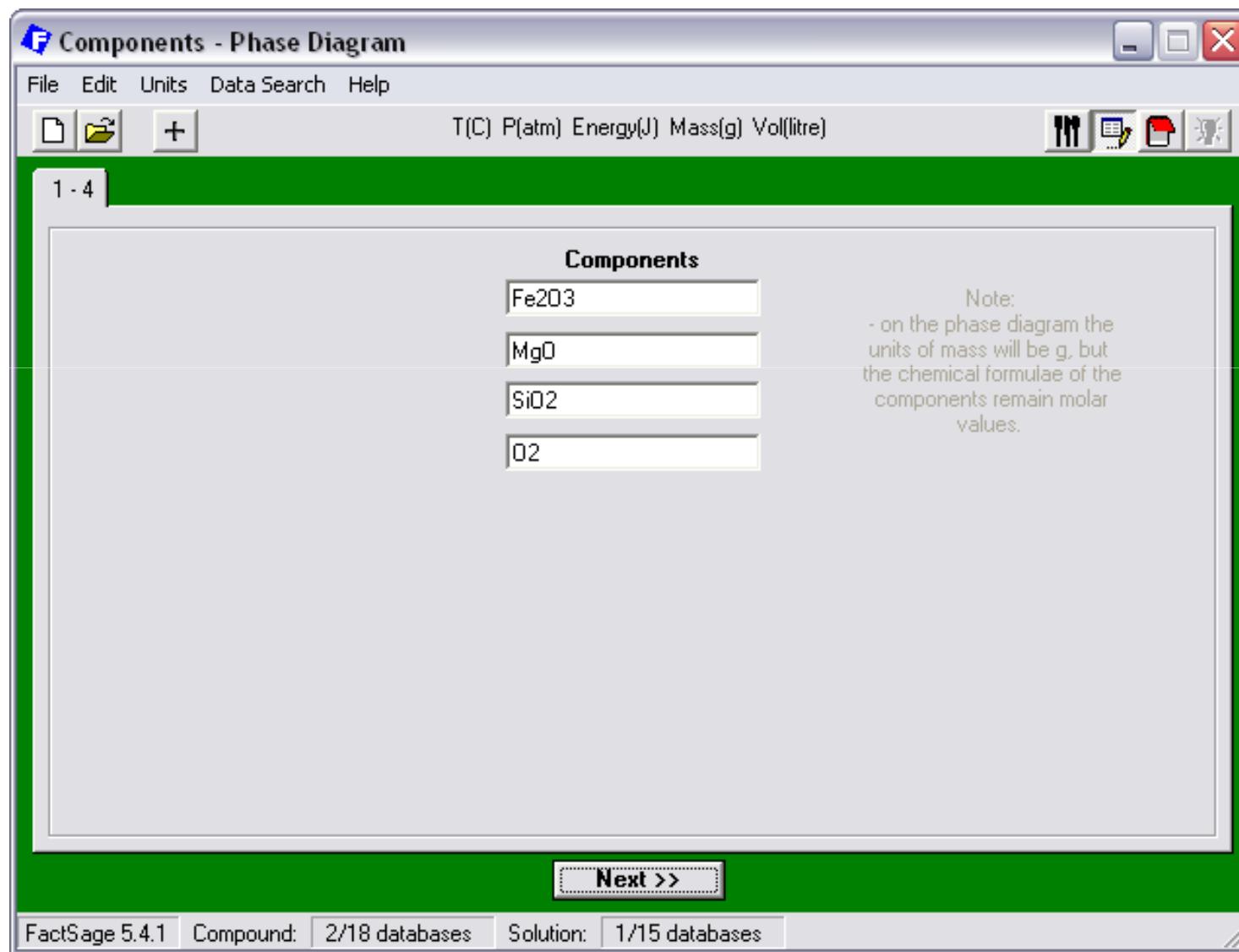
# Calculating Multicomponent Phase Diagram Sections using the Oxide Database



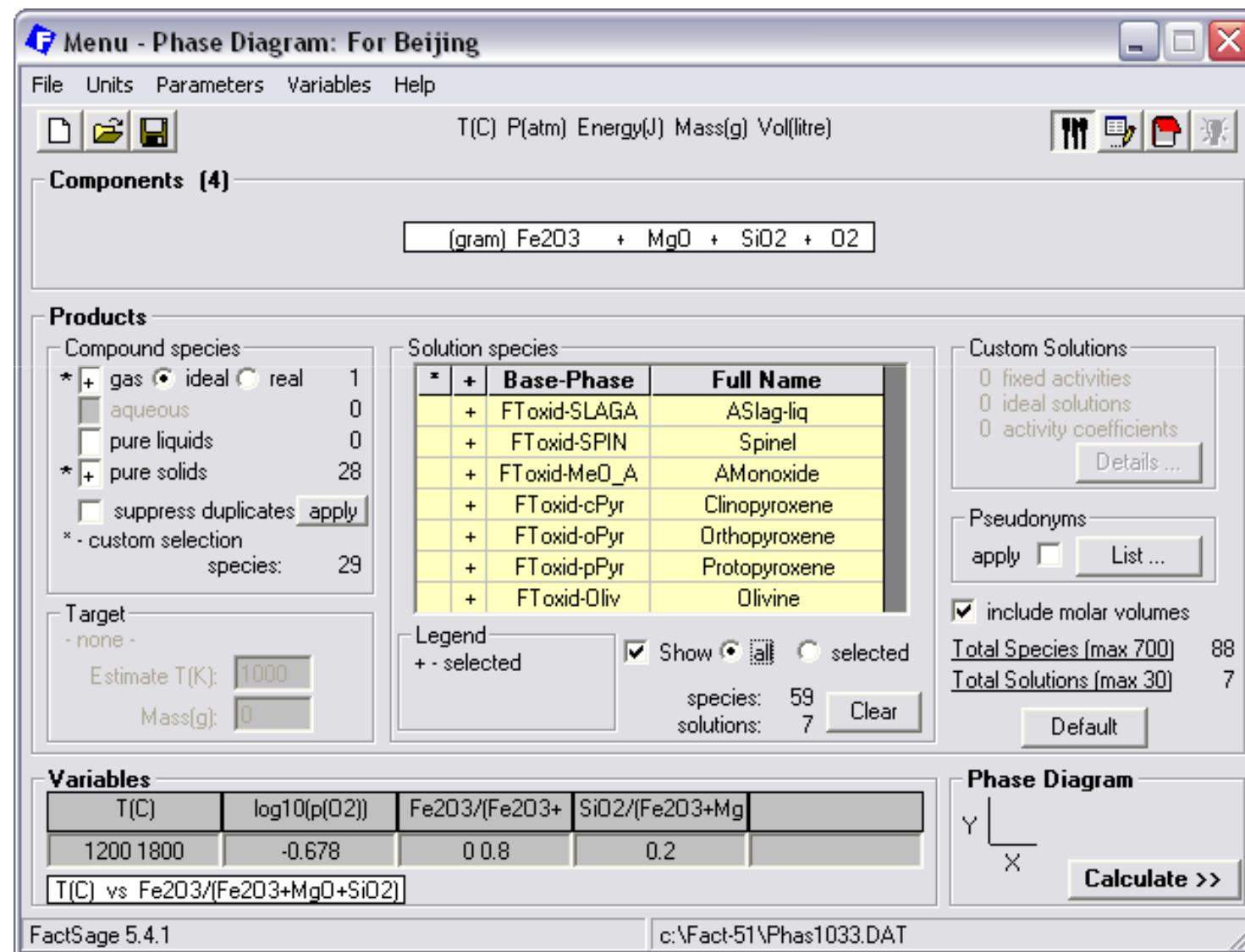
Calculated section of the  $\text{Fe}_2\text{O}_3$ - $\text{MgO}$ - $\text{SiO}_2$ - $\text{O}_2$  phase diagram in air at  $\text{SiO}_2/( \text{MgO} + \text{Fe}_2\text{O}_3 + \text{SiO}_2 ) = 20$  weight %

- Inputs to the FactSage module required to generate the preceding diagram
- (data retrieved automatically from database)

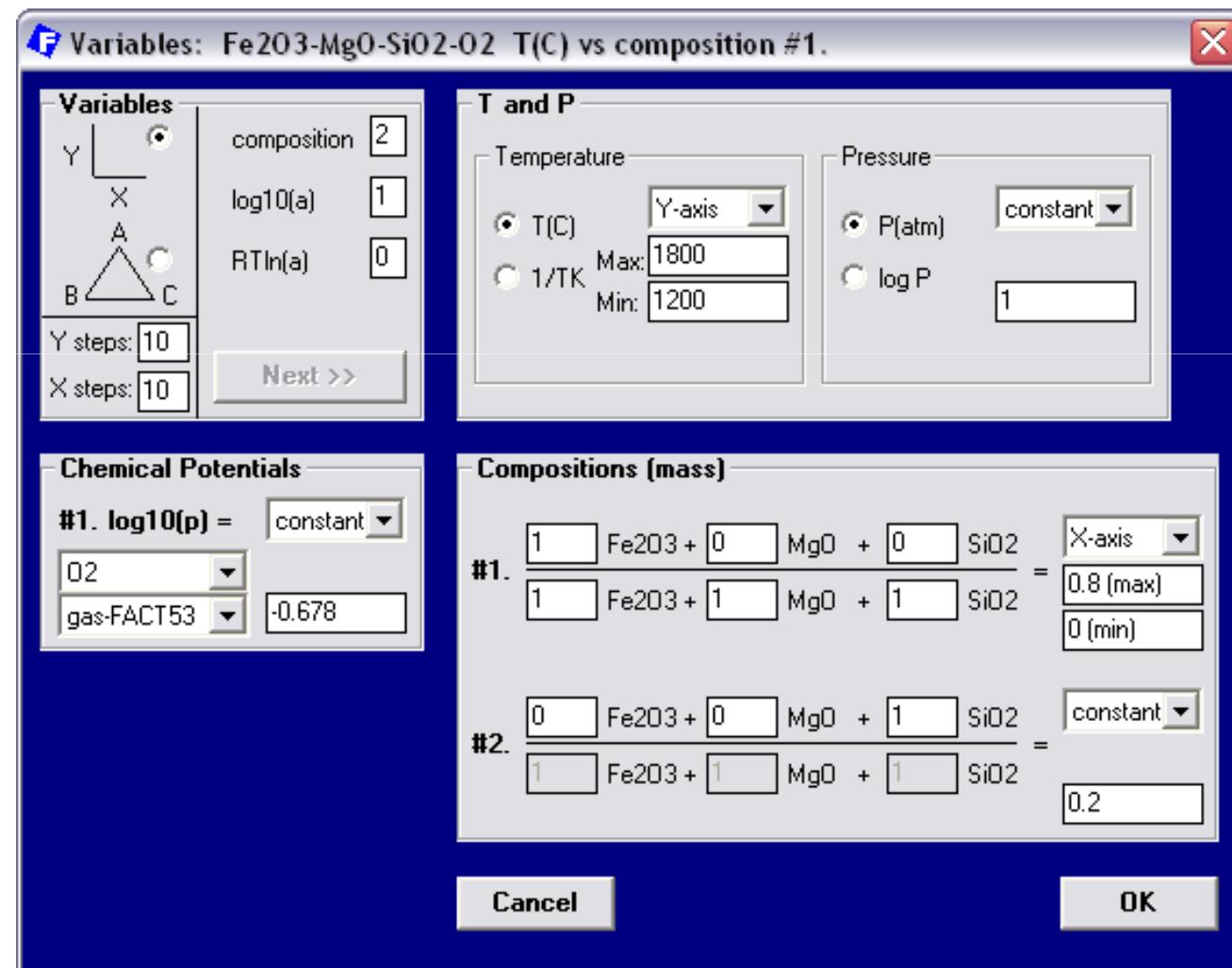
# (1) Components



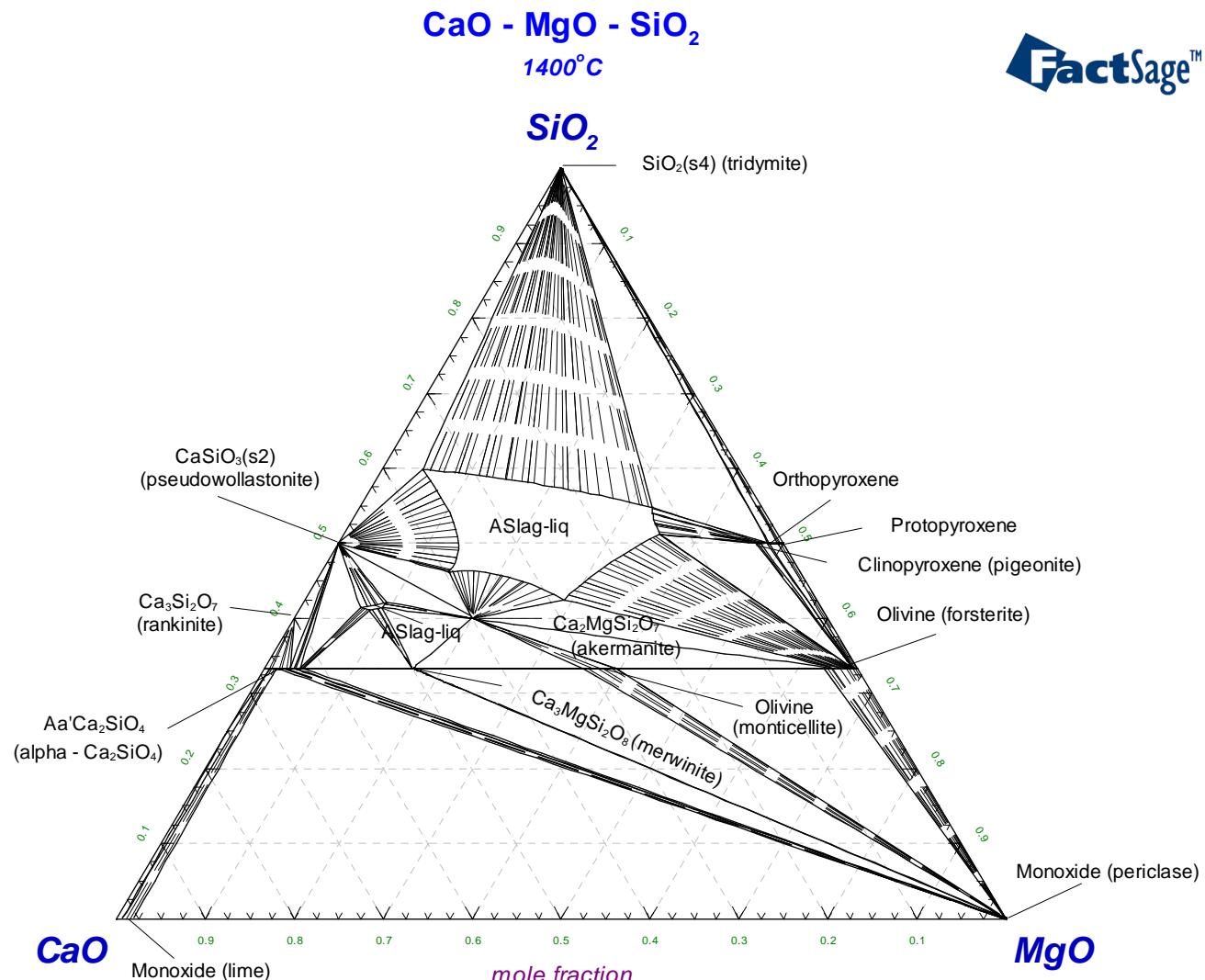
## (2) Species Selection



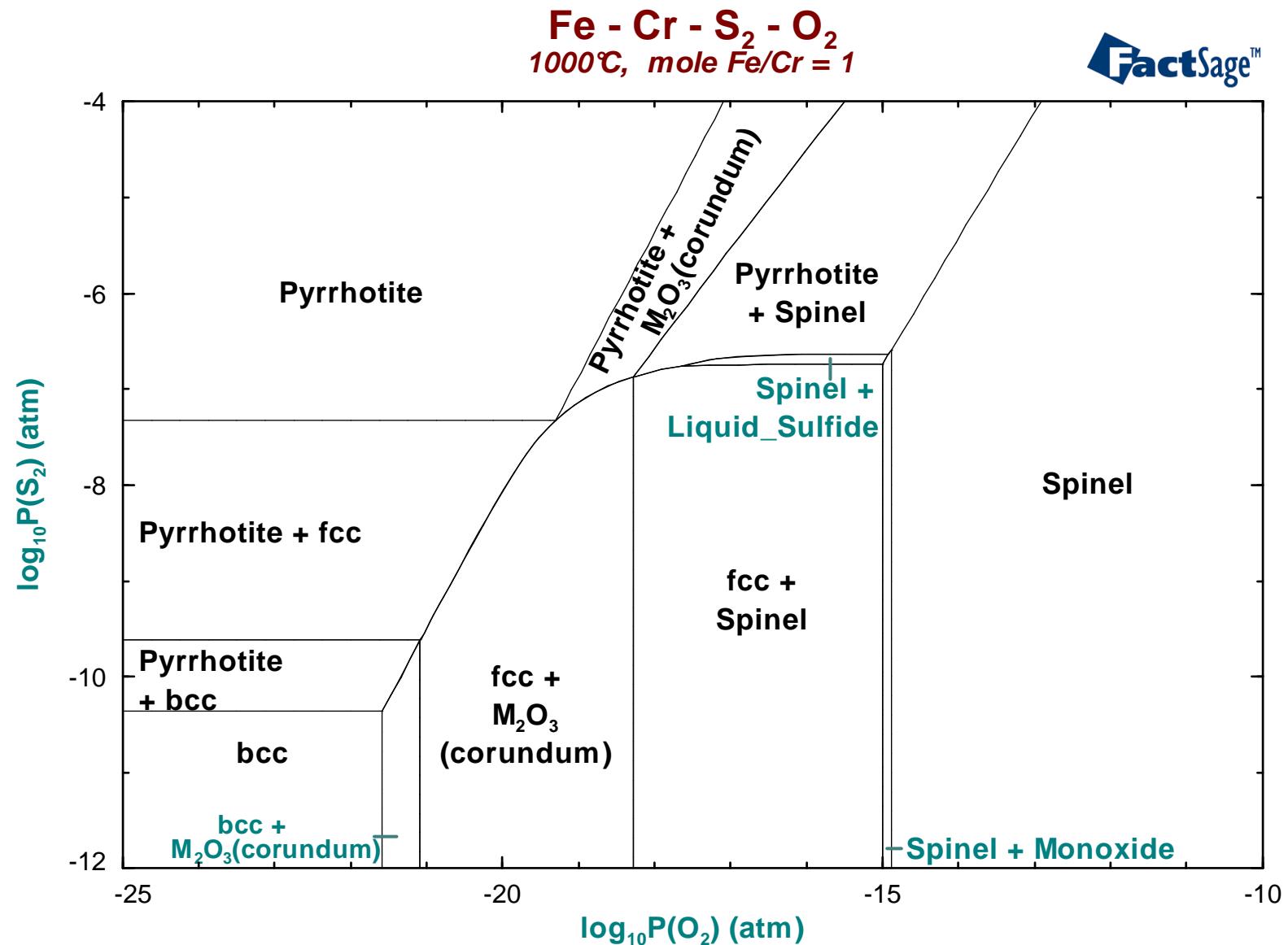
# (3) Defining Variables



# CaO - MgO - SiO<sub>2</sub> , 1400 °C



Calculations using the Oxide Database in  
Conjunction with other Databases (such as  
Databases for Metallic Phases, Gases, Sulfides, etc.)



Equilibrium phase composition generated by placing cursor at the point  $P(S_2) = 10^{-7}$ ,  $P(O_2) = 10^{-15}$  in the preceding diagram and clicking

log10(p(S<sub>2</sub>)) (atm) = -7.00, log10(p(O<sub>2</sub>)) (atm) = -15 1000.00 C  
=====

0.00 mol (0.99294E-07 S<sub>2</sub>  
+ 0.33664E-07 SO<sub>2</sub>  
+ 0.49582E-08 SO  
+ .  
. .  
+ 0.10000E-14 O<sub>2</sub>  
+ .  
. .  
(1 atm, gas)

+ 0.32583 mol Spinel  
Mole fraction of sublattice constituents in Spinel:  
Fe[2+] 0.87607 Stoichiometry = 1.0000  
Fe[3+] 0.12392  
Cr[3+] 0.30106E-05  
Cr[2+] 0.34690E-05  
-----  
Fe[2+] 0.61961E-01 Stoichiometry = 2.0000  
Fe[3+] 0.17195  
Va[o] 0.19186E-08  
Cr[3+] 0.76609  
-----  
+ 0.21232E-01 mol ( 0.94037 FeO  
+ 0.41724E-01 Fe<sub>2</sub>O<sub>3</sub>  
+ 0.17901E-01 Cr<sub>2</sub>O<sub>3</sub>  
( Monoxide)

# Conclusions

- Thermodynamic databases have been developed which contain critically evaluated and modeled data for thousands of compounds and hundreds of multicomponent solutions.
- The evaluated data are generally reproduced by the models within the experimental error limits.
- The models permit extrapolation into regions of temperature and composition where data are unavailable.
- The databases are automatically accessed by user-friendly software that calculates complex multiphase equilibria in large multicomponent systems for a wide variety of input/output constraints.
- The databases contain parameters of models specifically developed for different types of solutions involving sublattices, ordering, etc.